

ROTATION - ELECTRONIC INTERACTION IN  
THE 3p -COMPLEX RYDBERG STATE OF WATER

By

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TO MY PARENTS AND TEACHERS  
WHO INSPIRED ME TO SEEK  
KNOWLEDGE AND WISDOM



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## ABSTRACT

An energy theory is formulated for the rotational energy levels in a p-complex Rydberg state of an asymmetric top molecule of symmetry  $C_{2v}$ . The effective Hamiltonian used consists of the usual rigid rotor Hamiltonian augmented with terms representing electronic spin and orbital angular momentum effects. Criteria for assigning symmetry species to the rotational energy levels, following Hougan's scheme that uses the full molecular group, are established and given in the form of a table. This is particularly suitable when eigenvectors are calculated on a digital computer. Also, an intensity theory for transitions to the Rydberg p-complex singlet states is presented and selection rules in terms of symmetry species of energy states are established. Finally, applications to  $H_2O$  and  $D_2O$  are given.

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## 1. INTRODUCTION

A molecule has a unique structure depending on the atomic masses, electronic distribution, electronic and nuclear spin, inter-particle forces and distances involved. When exposed to an electromagnetic radiation, transitions take place selectively between the energy levels depending upon the frequency of radiation and the selection rules as established by the molecular symmetry and wave function properties. The transitions, characterized by a change in quantum states and identified by the quantum numbers of the interacting energy levels, can be one of the following types.

### (1) PURE ROTATIONAL TRANSITIONS

In this case the transitions occur between two different rotational states of energy in the same electronic and vibrational energy levels. The rotational energies are generally more closely spaced than the vibrational levels and, therefore, the corresponding transitions in rotational levels are of relatively low energy and fall in the microwave region.

### (2) ROTATION-VIBRATION TRANSITIONS

These transitions occur in the infra-red region and the transitions take place between vibrational levels accompanied by a change in rotational states.

### (3) ROVIBRONIC TRANSITIONS

Here, transitions occur from one electronic energy



level to another with a simultaneous change in the vibrational states. Thus the spectrum shows the electronic transitions together with the vibrational and rotational bands. The spectrum lies in the visible and ultraviolet regions.

We are concerned with the rotational energies and dipole transitions to almost degenerate electronic states (say, the p-orbitals) wherein the rotation-electronic matrix elements connecting different rotation-electronic states become significant; the vibrational state, assumed to be the same for all of the almost degenerate electronic states, is not a factor under consideration in our study. The type of molecule considered is an asymmetric top belonging to the  $C_{2v}$  point group.

The basic rotational energy theory of asymmetric top molecules has been investigated by many research workers. The theory was first presented by Witmer (1927) and later by Wang (1929), Klein (1929) and Kramer and Ittmann (1929, 1930). Klein (1929) and later Casimir (1931) have shown that the Wang secular determinant for asymmetric top molecules can be derived by operator techniques thus avoiding the use of an explicit form of a wave function. Ray (1932) introduced asymmetry parameters which by introducing a change of variables greatly facilitated the calculations of energy levels. All the above mentioned theories give the selection rules satisfactorily but none

of these have given a complete classification of the symmetry properties of the wave functions and hence the corresponding energy states. The first effort to this end was made by King, Hainer and Cross (1943, 1949) who have characterized the wave functions according to the Four group  $V(x, y, z) = D_2$ , defined by an identity and the three two-fold rotation operations  $C_2^x, C_2^y, C_2^z$  about the molecule-fixed axes  $x, y, z$  respectively. King, Hainer and Cross (1944) have also calculated the line strengths for the electric dipole transitions in a rigid asymmetric rotor where both the initial and the final states are assumed to have the same asymmetry. This theory does not, however, include the electronic-electronic and rotation-electronic interactions that are present in the case in which we are interested. The presence of these interactions in almost degenerate electronic states is expected to affect the rotational energy levels and the corresponding eigenvectors. Consequently, the energy level pattern and intensity distribution are modified accordingly. A proper theory must therefore account for all the interactions involved so as to predict correctly the rotational energies in an electronic state and calculate the relative intensities for the electric dipole transitions.

Creutzberg and Hougen (1967), using Raynes Hamiltonian (1964) as the basis, have discussed the theory of rotational energy levels in near-symmetric rotor molecules of symmetry

$C_{2v}$ ,  $D_2$  and  $D_{2h}$ . They have considered the effect of spin that results in spin-spin and spin-rotation terms.

The first objective of this thesis is to formulate, for the asymmetric top molecule of symmetry  $C_{2v}$ , an energy theory that can take into account explicitly the interactions, arising from both the spin and the orbital angular momenta, present in the nearly degenerate "p-complex" Rydberg state. The "p-complex" Rydberg states, analogous to the atomic situation, are characterized by a well-defined value of orbital angular momentum equal to unity ( $L=1$ ). The second objective is to formulate an intensity theory, not previously considered, which includes correctly the orbital electronic effects.

We have given in Chapter 2 the well-known rigid rotor theory that includes no interactions. In Chapter 3, the approximate theory for the spin case, given by Creutzberg and Hougen (1967), is adapted for the electronic orbital angular momentum case to obtain the effective rotational constants for  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  rotation-electronic bands of  $H_2O$  as well as  $D_2O$ . These rotational constants, in turn, are used in the theory given in Chapter 2 to calculate the rotational energies and the relative intensities so that the results of the theory in Chapter 4, when applied to  $H_2O$  and  $D_2O$ , may be compared. The numerical details of calculations for  $H_2O$  and  $D_2O$  for the transitions to the p-complex

Rydberg state, based on our theory in Chapter 4, are given in Chapter 5. Finally, a discussion of the results and conclusions are presented in Chapter 6.

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## 2. THE RIGID ROTOR THEORY

### 2.1 RIGID ROTOR HAMILTONIAN

The rotational motion of a molecule in its ground vibronic state may be described, to a good approximation, by a rigid rotor Hamiltonian. We consider, for the sake of generality, an asymmetric top molecule in which case one has the principal moment of inertia  $I_x \neq I_y \neq I_z$  and the corresponding rotational constants  $X \neq Y \neq Z$  about the principal axes of inertia  $x, y, z$  respectively. The classical-mechanical Hamiltonian for a rigid rotor is

$$H = \frac{J_x^2}{2I_x} + \frac{J_y^2}{2I_y} + \frac{J_z^2}{2I_z} \quad (1)$$

where  $J_\alpha$  and  $I_\alpha$  ( $\alpha = x, y, z$ ) respectively represent the rotational angular momenta and moments of inertia about the axes  $\alpha$ , fixed at the centre-of-mass of the molecule under consideration.

By expressing  $J_\alpha$  as operators  $\hat{J}_\alpha$  ( $\alpha = x, y, z$ ) and defining the rotational constants  $X \neq Y \neq Z$  in  $\text{cm}^{-1}$  units as

$$X = \frac{\hbar^2}{hc} \cdot \frac{1}{2I_x} \quad ; \quad Y = \frac{\hbar^2}{hc} \cdot \frac{1}{2I_y} \quad ; \quad Z = \frac{\hbar^2}{hc} \cdot \frac{1}{2I_z} \quad (2)$$

one obtains, on dividing (1) by  $hc$ , the quantum-mechanical Hamiltonian for a rigid rotor in  $\text{cm}^{-1}$  units as

$$\hat{H}_r = \frac{1}{\hbar^2} [ X \hat{J}_x^2 + Y \hat{J}_y^2 + Z \hat{J}_z^2 ] \quad (3)$$

To display diagonal and off-diagonal terms (3) can be rewritten in the form

$$\hat{H}_r = \frac{1}{\hbar^2} \left[ \frac{1}{2} (X+Y) \hat{J}^2 + \left\{ Z - \frac{1}{2} (X+Y) \right\} \hat{J}_z^2 + \frac{1}{2} (X-Y) (\hat{J}_x^2 - \hat{J}_y^2) \right] \quad (4a)$$

or

$$\hat{H}_r = \frac{1}{\hbar^2} \left[ \frac{1}{2} (X+Y) \hat{J}^2 + \left\{ Z - \frac{1}{2} (X+Y) \right\} \hat{J}_z^2 + \frac{1}{4} (X-Y) (\hat{J}_+^2 + \hat{J}_-^2) \right] \quad (4b)$$

where

$$\hat{J}^2 = \hat{J}_x^2 + \hat{J}_y^2 + \hat{J}_z^2 \quad (4c)$$

and

$$\hat{J}_\pm = \hat{J}_x \pm i \hat{J}_y \quad (4d)$$

$\hat{J}_+$  and  $\hat{J}_-$  are respectively the lowering and raising operators of angular momentum in the molecule-fixed frame.

The principal moments of inertia  $I_x$ ,  $I_y$  and  $I_z$  are usually written as  $I_a$ ,  $I_b$  and  $I_c$  where

$$I_a \leq I_b \leq I_c \quad (5a)$$

The corresponding rotational constants  $X$ ,  $Y$  and  $Z$  are written as  $A$ ,  $B$  and  $C$  where

$$A \geq B \geq C \quad (5b)$$

For an almost prolate or oblate rotor it is advantageous to choose the molecule-fixed  $z$ -axis as the  $a$ - or  $c$ -axis respectively, since this choice makes the off-diagonal matrix elements small. The prolate description is commonly used for the water molecule since even in this case of a very highly asymmetric top molecule the off-diagonal matrix elements for  $z=a$  are smaller than those given by choosing  $z=b$  or  $c$ . Nevertheless we have, instead, adopted a different scheme. That is,  $x=c$ ,  $y=a$ , and  $z=b$ . This choice is consistent with the conventional form of the character table for the  $C_{2v}$

point group as well as chemical convention which requires the  $x=c$  axis to be perpendicular to the molecular plane.

Using our choice of axes we now write (4) as

$$\hat{J}^2 = \hat{J}_x^2 + \hat{J}_y^2 + \hat{J}_z^2 = \hat{J}_c^2 + \hat{J}_a^2 + \hat{J}_b^2 \quad (5c)$$

$$\hat{J}_{\pm} = \hat{J}_x \pm i\hat{J}_y = \hat{J}_c \pm i\hat{J}_a \quad (5d)$$

$$\hat{H}_r = \frac{1}{\hbar^2} \left[ \frac{1}{2} (C+A) \hat{J}^2 + \left\{ B - \frac{1}{2} (C+A) \right\} \hat{J}_b^2 + \frac{1}{4} (C-A) (\hat{J}_+^2 + \hat{J}_-^2) \right] \quad (5e)$$

Before proceeding to find the rotational energy matrix and, therefore, the rotational energy levels, it seems natural to look for the appropriate functions of states between which matrix elements of  $\hat{H}_r$  could be formed. The specific forms of functions, the operators and their effect on rotational functions will be mentioned only briefly in the following section.

## 2.2 RIGID-ROTOR FUNCTIONS

Since  $[\hat{J}_q, \hat{J}_\alpha] = 0$  and  $\hat{J}^2$  commutes with space-fixed components  $\hat{J}_q$  ( $q = X, Y, Z$ -axes in space-fixed coordinates) as well as its molecule-fixed components  $\hat{J}_\alpha$ , there exist functions  $|JKM\rangle$  which are simultaneous eigenfunctions of  $\hat{J}^2$ ,  $\hat{J}_z$  and  $\hat{J}_Z$  where  $\hat{J}_Z$  is the  $Z$ -component of  $\hat{J}$  in space-fixed coordinate system. The  $|JKM\rangle$  are simply the symmetric top eigenfunctions, where

J - rotational quantum number and represents the total rotational angular momentum of the molecule.

K - quantum number representing the component  $J_z$  of J and is taken along the symmetry axis of the molecular-fixed frame.

M - quantum number representing the component of total angular momentum along the space-fixed Z-axis.

Note that K and M can each take  $2J + 1$  values  $-J, -J + 1, \dots, J - 1, J$ . The quantum numbers J, K and

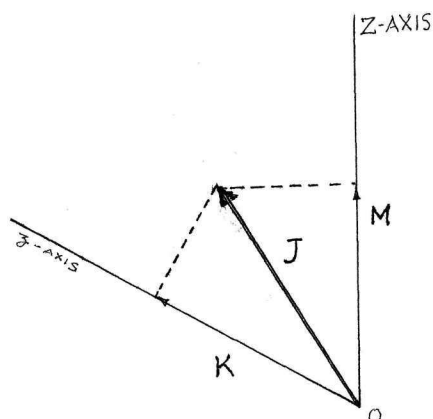


FIG. 1

M are shown schematically in the vector model diagram of angular momenta (FIG. 1) where the inter-relationship of J, K and M is quite obvious.

The functions  $|JKM\rangle$  used in this work as basis functions are well known and are given below.

$$|JKM\rangle = C_{JKM} (\hat{J}_x - i\hat{J}_y)^{J-M} (\hat{J}_z + i\hat{J}_a)^{J-K} |JJJ\rangle \quad (6a)$$

where

$$\hat{J}_x \pm i\hat{J}_y = i\hbar e^{\pm i\varphi} \left( \cot\theta \frac{\partial}{\partial\varphi} \mp i \frac{\partial}{\partial\theta} - \csc\theta \frac{\partial}{\partial\chi} \right) \quad (6b)$$

$$\hat{J}_z \mp i\hat{J}_a = i\hbar e^{\pm i\chi} \left( \csc\theta \frac{\partial}{\partial\varphi} \pm i \frac{\partial}{\partial\theta} - \cot\theta \frac{\partial}{\partial\chi} \right) \quad (6c)$$

$$C_{JKM} = \left( \frac{1}{\hbar} \right)^{2J-K-M} \sqrt{\frac{(J+K)! (J+M)!}{[(2J)!]^2 (J-K)! (J-M)!}}$$



and

$$|JJJ\rangle = \sqrt{\frac{2J+1}{8\pi^2}} e^{iJ(\varphi+\chi)} \left(\cos\frac{\theta}{2}\right)^{2J} \quad (6d)$$

where  $\theta, \varphi, \chi$  are the Euler angles which relate the space-fixed coordinates to the molecule-fixed coordinates.

In a homogeneous space the energy is independent of  $M$ ; therefore we can drop this quantum number in our future notations. That is,  $|JKM\rangle$  will be represented by  $|JK\rangle$  from now on. Thus  $|JK\rangle$  will be taken as a basis functions to yield the asymmetric-top rotational energy stationary states and eigenfunctions on diagonalization of  $\hat{H}_r$ . The effect of operators  $\hat{J}_{\pm} = \hat{J}_c \pm i\hat{J}_a$ ,  $\hat{J}_z \equiv \hat{J}_b$  and  $\hat{J}^2$  on the functions are

$$\hat{J}_{\pm} |JK\rangle = (\hat{J}_c \pm i\hat{J}_a) |JK\rangle = \sqrt{J(J+1) - K(K \mp 1)} \hbar |JK \mp 1\rangle \quad (7)$$

$$\hat{J}_b |JK\rangle = K \hbar |JK\rangle \quad (8)$$

$$\hat{J}^2 |JK\rangle = J(J+1) \hbar^2 |JK\rangle \quad (9)$$

which will be used to yield diagonal and off-diagonal matrix elements of the rigid rotor Hamiltonian. Note that (7) results from the "anomalous" sign of " $i$ " (see [21]).

### 2.3 RIGID ROTOR MATRIX ELEMENTS

Operating the rigid rotor Hamiltonian  $\hat{H}_r$  on  $|JK\rangle$  on the right hand side in (5a) and using the results (7), (8) and (9) gives

$$\begin{aligned}\hat{H}_r |JK\rangle &= \frac{1}{\hbar^2} \left[ \frac{1}{2} (C+A) \hat{J}^2 + \left\{ B - \frac{1}{2} (C+A) \right\} \hat{J}_b^2 + \frac{1}{4} (C-A) (\hat{J}_+^2 + \hat{J}_-^2) \right] |JK\rangle \\ &= \left[ \frac{1}{2} (C+A) [J(J+1)] + \left[ B - \frac{1}{2} (C+A) \right] K^2 \right] |JK\rangle \\ &\quad + \left[ \frac{1}{4} (C-A) \sqrt{[J(J+1) - K(K-1)][J(J+1) - (K-1)(K-2)]} \right] |JK-2\rangle \\ &\quad + \left[ \frac{1}{4} (C-A) \sqrt{[J(J+1) - K(K+1)][J(J+1) - (K+1)(K+2)]} \right] |JK+2\rangle\end{aligned}$$

which on multiplying with  $\langle JK|$ ,  $\langle JK-2|$  and  $\langle JK+2|$  gives the matrix elements

$$\langle JK | \hat{H}_r | JK \rangle = \frac{1}{2} (C+A) [J(J+1)] + \left[ B - \frac{1}{2} (C+A) \right] K^2 \quad (10a)$$

and

$$\langle JK \pm 2 | \hat{H}_r | JK \rangle = \frac{1}{4} (C-A) \sqrt{[J(J+1) - K(K \pm 1)][J(J+1) - (K \pm 1)(K \pm 2)]} \quad (10b)$$

where the orthonormality condition

$$\langle JK' | JK \rangle = \delta_{KK'} = \begin{cases} 1 & \text{if } K' = K \\ 0 & \text{if } K' \neq K \end{cases} \quad (10c)$$

is used for the basis functions to obtain (10a) and (10b).

Although (10a) and (10b) can be used directly to calculate the rotational energy levels, we have used an asymmetry parameter  $\kappa$  [19] because it facilitates the

calculation of the rotational stationary states by using scaled rotational constants, thereby making it possible to carry out solutions, at least in part, for all molecules. On replacing A, B and C respectively with

$$\sigma A + \rho \quad ; \quad \sigma B + \rho \quad ; \quad \sigma C + \rho \quad (11)$$

in the rotational Hamiltonian

$$\hat{H}_r(A, B, C) = \frac{1}{\hbar^2} \left[ A \hat{J}_a^2 + B \hat{J}_b^2 + C \hat{J}_c^2 \right] \quad (12)$$

one obtains

$$\begin{aligned} \hat{H}_r(\sigma A + \rho, \sigma B + \rho, \sigma C + \rho) &= \frac{1}{\hbar^2} \left[ (\sigma A + \rho) \hat{J}_a^2 + (\sigma B + \rho) \hat{J}_b^2 + (\sigma C + \rho) \hat{J}_c^2 \right] \\ &= \sigma \hat{H}_r(A, B, C) + \frac{\rho}{\hbar^2} \hat{J}^2 \end{aligned} \quad (13)$$

$$\text{where } \hat{J}^2 = \hat{J}_a^2 + \hat{J}_b^2 + \hat{J}_c^2.$$

The resulting matrix elements are then

$$\langle JK' | \hat{H}_r(\sigma A + \rho, \sigma B + \rho, \sigma C + \rho) | JK \rangle = \sigma \langle JK' | \hat{H}_r(A, B, C) | JK \rangle + \frac{\rho J(J+1)}{(14)} \delta_{KK'} \quad (14)$$

Following Ray [19], we set

$$\sigma A + \rho = 1 \quad ; \quad \sigma B + \rho = K \quad ; \quad \sigma C + \rho = -1 \quad (15a)$$

which give

$$\sigma = \frac{2}{A-C} \quad ; \quad \rho = -\frac{A+C}{A-C} \quad ; \quad K = \frac{2B-(A+C)}{A-C} \quad (15b)$$

Use of (15a) and (15b) in (14) gives

$$\langle JK' | \hat{H}_r(1, \kappa, -1) | JK \rangle = \frac{2}{A-C} \langle JK' | \hat{H}_r(A, B, C) | JK \rangle - \frac{A+C}{A-C} J(J+1) \delta_{\kappa\kappa'} \quad (16)$$

or

$$\langle JK' | \hat{H}_r(A, B, C) | JK \rangle = \frac{A-C}{2} \langle JK' | \hat{H}_r(1, \kappa, -1) | JK \rangle + \frac{A+C}{2} J(J+1) \delta_{\kappa\kappa'} \quad (17)$$

The scaled matrix  $\langle JK | \hat{H}_r(1, \kappa, -1) | JK \rangle$ , which depends on the asymmetry parameter  $\kappa$ , when diagonalized gives the energy levels

$$E(A, B, C) = \frac{A+C}{2} J(J+1) + \frac{A-C}{2} E(\kappa) \quad (18)$$

where

$$E(\kappa) = \langle JK | \hat{H}_r(1, \kappa, -1) | JK \rangle \quad (19)$$

The parameter  $\kappa$ , which measures the degree of asymmetry, ranges between 1 and -1; i.e., between  $\frac{B+C}{A+B}$  and  $\frac{B+C}{A+C}$ ,  $\kappa$  being -1 for the prolate symmetric top limit while it is 1 for the oblate symmetric top limit and  $\kappa = 0$  for the most asymmetric top limit case.

#### 2.4 LABELLING THE ENERGY LEVELS:

For an asymmetric top rotor, both  $J$ , the total angular momentum and its projection  $M$  along the space-fixed  $Z$ -axis are constants of motion, and, therefore, are good quantum numbers. They can be used to specify the energy states of a rotor. The component of angular

momentum in any direction in the molecule-fixed frame is, however, not constant; be it a classical mechanical motion or a quantum-mechanical one. Thus,

$$[\hat{H}_r, \hat{J}_z] = [\hat{H}_r, \hat{J}_b] \neq 0 \text{ and } K \text{ is not a good quantum number.}$$

$K$  cannot be used adequately to specify the rotational energy states. Thus far, no set of quantum numbers is known for the asymmetric top molecules which conveniently specify the stationary states of the rotor and have a simple physical meaning. Regardless of the inadequacy of  $K$  to be a good quantum number, it is retained to label the energy levels in the form  $J_{K_{-1}K_1}$  (or  $J_{K_a K_c}$ ) where  $K_{-1}$  (or  $K_a$ ) and  $K_1$  (or  $K_c$ ) are the values  $K$  will acquire in the limiting cases of prolate symmetric top and oblate symmetric top. The subscripts  $-1$  and  $1$  appearing with  $K$  are the parametric values of  $K$  under the extreme limits. There is an equivalent scheme of labelling the energy states, represented by  $J_\tau$  where  $\tau = K_{-1} - K_1 = K_a - K_c$ . Assuming the states for a given  $J$  value are listed in order of increasing energy the labels  $K_a = 0, 1, 1, 2, 2, \dots, J, J$ ,  $K_c = J, J, J-1, J-1, \dots, 1, 1, 0$  and thus  $\tau = -J, -J+1, \dots, J-1, J$  are attached to each state, starting from that of lowest energy for a particular value.

In our work, the latter scheme is adopted; that is, the  $J_\tau$  symbol is used for labelling the energy states. The labelling scheme is shown in FIG. 2.

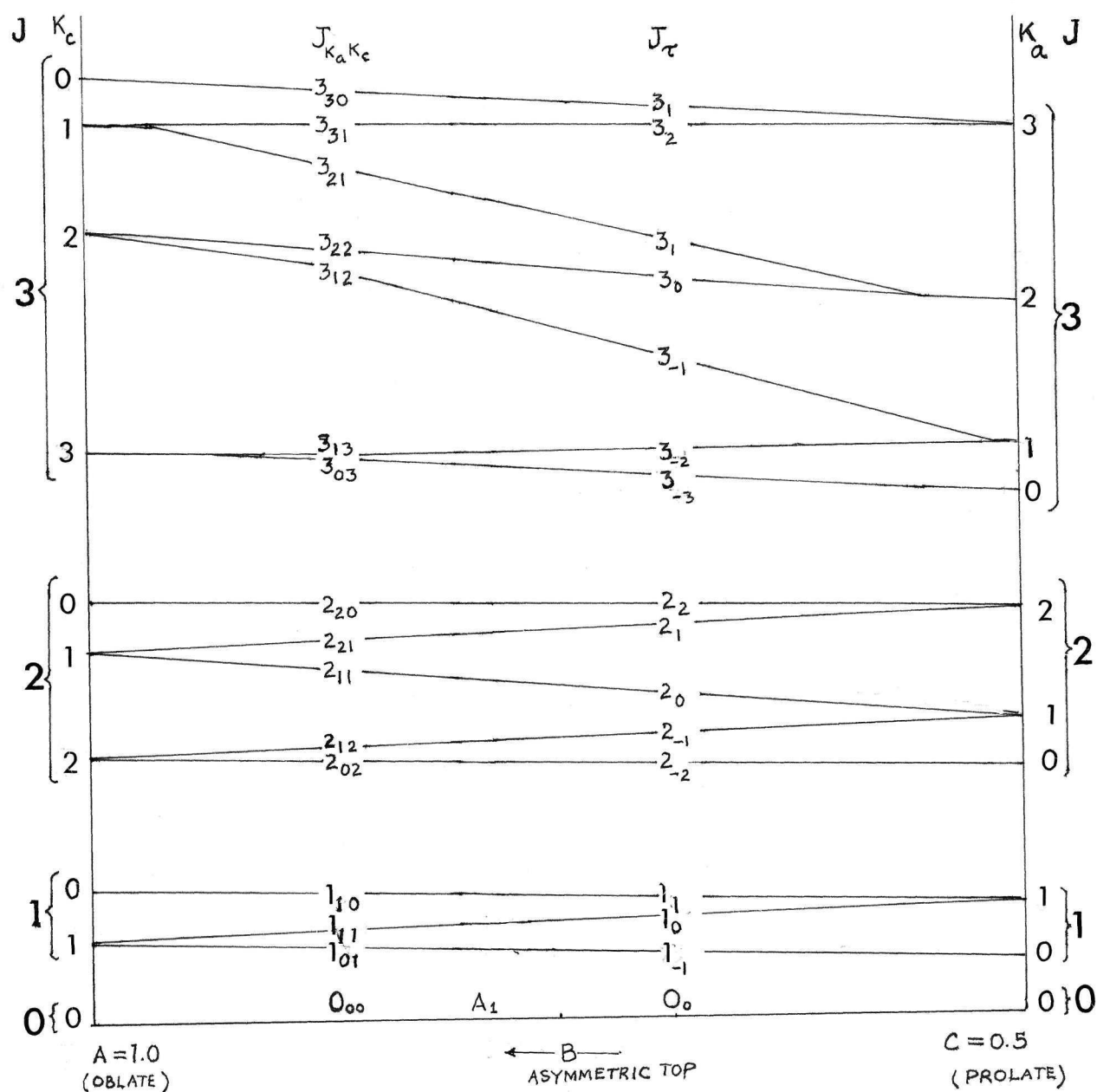


FIG 2. THE TWO LABELLING SCHEMES ( $J_{K_a K_c}$  AND  $J_\tau$ ).

## 2.5 TRANSFORMATION PROPERTIES OF RIGID ROTOR BASIS

### FUNCTIONS:

The transformation properties of rigid rotor basis functions are important from the view point of classification of symmetry of energy levels and determining the combination of states involved in transitions.

Hougen (1963) has given the following effect of symmetry transformations.

$$\hat{C}_{2z} |JK\rangle \equiv \hat{C}_{2b} |JK\rangle = (-1)^K |JK\rangle \quad (20a)$$

$$\hat{\sigma}_v(yz) |JK\rangle \equiv \hat{\sigma}_v(ab) |JK\rangle = (-1)^J |J-K\rangle \quad (20b)$$

$$\hat{\sigma}_v(xz) |JK\rangle \equiv \hat{\sigma}_v(cb) |JK\rangle = (-1)^{J-K} |J-K\rangle \quad (20c)$$

These results will be used in our work.

## 2.6 CLASSIFICATION SCHEMES FOR ENERGY STATES:

There are two schemes which can be used to classify the energy levels, based on either

- (i) molecular subgroup and parity
- or (ii) full molecular point group.

For planar molecules, Hougen [9] has shown that reflection in the molecular plane is equivalent to the parity operation. Then the molecular plane  $\sigma_v(yz)$  when used as an operator on the complete wavefunction, determines the parity of states. Therefore, the scheme (ii), based on the full molecular symmetry group,

embodies within its framework the ability of assigning parity to energy levels. The scheme, first introduced by Hougen [8], will be used in the present work to replace the earlier scheme of representing the energy levels by ++, +-, -+, -- and also +, - for designating the parity of purely rotational states.

Hougen's scheme has the advantage of using the actual molecular point group rather than simply the  $D_2$  group of a rigid rotor. In the earlier scheme (i), one also needs to label the energy states by  $a$  (asymmetric) or  $s$  (symmetric) according as the permutation of nuclei changes sign of the complete wavefunction (excluding nuclear spin) or not. This is done by examining the rotational subgroup. Thus, in Hougen's scheme the full molecular group labels belonging to the same rotational subgroup species have the same statistical weight.

## 2.7 THE ASYMMETRIC TOP RIGID ROTOR EIGENFUNCTIONS AND ASSIGNMENT OF SYMMETRY SPECIES

Let the rigid rotor wavefunction corresponding to the energy level, denoted by  $\tau$ , in the basis  $|JK\rangle$  be given by

$$\psi_r^\tau = \sum_K a_K^\tau |JK\rangle \quad (21)$$

where  $\psi_r^\tau$  is expressed as a linear combination of eigenvectors  $a_K^\tau$  of energy level (labelled as  $\tau$ ) taken



over all possible values of quantum number  $K$  in the basis  $|JK\rangle$ .

In order to determine the symmetry of an energy state we use the elements of the molecular point group as operators on the rotational eigenfunctions in conformity with the transformation properties (20a) and (20b). Then we look for the behaviour of the eigenfunctions with reference to the associated irreducible representations or characters as decided by the even-odd nature of the quantum numbers  $J$  and  $K$ . Thus, from (20a), (20b), (21) and the character table for the  $C_{2v}$  point group (APPENDIX I), we find that

$$\hat{C}_{2z}\psi_r^\tau \equiv \hat{C}_{2z} \sum_K a_K^\tau |JK\rangle = \sum_K (-1)^K a_K^\tau |JK\rangle \quad (22)$$

Since  $\psi_r^\tau = \pm \psi_r^\tau$ , (22) implies that

$$\hat{C}_{2z}\psi_r^\tau = \begin{cases} +\psi_r^\tau & \text{for even } K\text{-values} \\ -\psi_r^\tau & \text{for odd } K\text{-values} \end{cases} \quad (23a)$$

Then the character table indicates that

$$\left. \begin{array}{l} K\text{-EVEN is associated with species } A_1 \text{ or } A_2 \text{ and} \\ K\text{-ODD is associated with species } B_1 \text{ or } B_2 \end{array} \right\} \quad (23b)$$

Also

$$\hat{\sigma}_v(yz)\psi_r^\tau = \hat{\sigma}_v(yz) \sum_K a_K^\tau |JK\rangle = (-1)^J \sum_K a_K^\tau |J-K\rangle \quad (24a)$$

There are two possibilities; either (24a) is equal to  $+\psi_r^\tau$  or  $-\psi_r^\tau$ .

Let us now suppose that

$$a_K^\tau = a_{-K}^\tau \quad (24b)$$

then (24a) becomes

$$\hat{\sigma}_v(yz)\psi_r^\tau = (-1)^J \sum_K a_{-K}^\tau |J-K\rangle = (-1)^J \psi_r^\tau \quad (24c)$$

since  $K$  is merely a summation index.

Similarly, if

$$a_K^\tau = -a_{-K}^\tau \quad (24d)$$

then

$$\hat{\sigma}_v(yz)\psi_r^\tau = -(-1)^J \psi_r^\tau \quad (24e)$$

The results (24a), (24b), (24c), (24d) and (24e) lead to the conclusion that

$$\hat{\sigma}_v(yz)\psi_r^\tau = \pm (-1)^J \psi_r^\tau \quad \text{if} \quad a_K^\tau = \pm a_{-K}^\tau \quad (24f)$$

Again from (24f) and the character table for  $C_{2v}$  point group, we find that

$$\hat{\sigma}_v(yz)\psi_r^\tau = \begin{cases} +\psi_r^\tau & \text{refers to species } A_1 \text{ or } B_2 \\ -\psi_r^\tau & \text{refers to species } A_2 \text{ or } B_1 \end{cases} \quad (24g)$$

We do not use  $\hat{\sigma}_v(xz)$  since it leads to no additional information not already contained in (23b) and (24g).

The results (23a), (23b) and (24f), (24g) lead us to

establish the following criteria (TABLE 1) for the assignment of symmetry species to the rotational energy states.

TABLE 1

CRITERIA FOR ASSIGNING THE FULL MOLECULAR SPECIES TO THE RIGID ROTOR ENERGY STATES OF THE MOLECULES OF SYMMETRY  $C_{2v}$

$J$	$K$	$a_K^\tau = a_{-K}^\tau$		$a_K^\tau = -a_{-K}^\tau$	
		SYMMETRY SPECIES	PARITY	SYMMETRY SPECIES	PARITY
EVEN	EVEN	$A_1$	+	$A_2$	-
EVEN	ODD	$B_2$	+	$B_1$	-
ODD	EVEN	$A_2$	-	$A_1$	+
ODD	ODD	$B_1$	-	$B_2$	+

Note that the parity results are obtained from  $\hat{\sigma}_v(yz)$  alone. That is,  $A_1$  and  $B_2$  levels are of + (i.e. even) parity while  $A_2$  and  $B_1$  levels are of - (i.e. odd) parity.

## 2.8 DIPOLE TRANSITION MOMENTS

Electric dipole transitions are governed by the square of the integral

$$\langle \psi'_{evr} | \mu_Z | \psi''_{evr} \rangle \quad (25)$$

where  $\mu_Z$  is the space-fixed Z-component of the electric dipole moment  $\vec{\mu}$  while  $\psi''_{evr}$  and  $\psi'_{evr}$  are the rovibronic eigenfunctions corresponding to the initial and final states, respectively, involved in the transition.

Under the group operations, any space-fixed polar vector changes sign under improper rotations and is invariant under proper rotations. Then, using the  $C_{2v}$  character table, we see that the irreducible representation for  $\mu_Z$ , denoted by  $\Gamma(\mu_Z)$ , is of species

$$\Gamma(\mu_Z) = A_2 \quad (26)$$

The integral (25) must be totally symmetric in order to exist. This requires, in view of (26),  $\psi''_{evr}$  and  $\psi'_{evr}$  to be of opposite parity. In other words, the direct product of their symmetry species must obey

$$\Gamma(\psi'_{evr}) \times \Gamma(\psi''_{evr}) = A_2 \quad (27)$$

In practice, it is convenient to classify the rovibronic states for a totally symmetric vibronic state. The complete symmetry species for any rovibronic state is then obtained simply by multiplying the rotational species with the vibronic species. This requires

different selection rules for different vibronic transitions, obtained from (27) as follows:

Use of the Born-Oppenheimer approximation allows us to write the full (rovibronic) eigenfunction  $\psi_{evr}$  as a product of vibronic and rotational wavefunctions  $\psi_{ev}$  and  $\psi_r$  respectively. That is,

$$\psi_{evr} = \psi_{ev} \psi_r \quad (28)$$

Then one can write

$$\Gamma(\psi_{evr}) = \Gamma(\psi_{ev}) \times \Gamma(\psi_r) \quad (29)$$

which when used in (27) yields

$$[\Gamma(\psi'_r) \times \Gamma(\psi''_r)] \times [\Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev})] = A_2 \quad (30)$$

giving the rule

$$\Gamma(\psi'_r) \times \Gamma(\psi''_r) = \Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) \times A_2 \quad (31)$$

which sets the criterion for determining the possible transitions between rotational states for fixed symmetry species of vibronic states in the initial and final states of transitions. The possible cases for which transitions might occur between rotation-electronic states will be considered one by one at a later stage after general forms of expressions for the line strength and relative intensity have been developed.

## 2.9 TRANSITION MOMENTS IN THE MOLECULAR-FIXED FRAME

Since the components of the dipole moment must be used in the molecule -fixed frame for a rotating molecule, it is important to know the form of transformation of the space-fixed component  $\mu_z$  to the molecule -fixed frame.

$$\text{Let } f_{z\alpha} = f_{z\alpha}(\theta, \varphi, \chi) \text{ where } \alpha = x, y, z \quad (32)$$

be the functions of Euler angles  $\theta, \varphi$  and  $\chi$  ([8], [13]) which are associated with the molecule -fixed components  $\mu_\alpha$  of  $\mu_z$  according to the equation

$$\mu_z = \sum_{\alpha=x,y,z} f_{z\alpha}(\theta, \varphi, \chi) \mu_\alpha \quad (33)$$

We consider  $\mu_\alpha$  in the form

$$\mu_0 \equiv \mu_z \quad \text{and} \quad \mu_\pm = (\mu_x \pm i\mu_y)/\sqrt{2} \quad (34)$$

so (33) takes the form

$$\mu_z = \sum_r f_{-r} \mu_r \quad ; \quad r=0, \pm 1 \quad (35)$$

where  $f_{-r}$  are appropriate functions of the direction cosines and  $\mu_r$  are the components of a spherical tensor of rank unity. Therefore, the form of the electric dipole transition moments (25) changes to

$$\langle \psi'_{evr} | \sum_r f_{-r} \mu_r | \psi''_{evr} \rangle \quad (36)$$

which will be used in our future development of intensity relations.

## 2.10 EXPRESSIONS FOR LINE STRENGTHS AND RELATIVE INTENSITIES:

The line strength  $[S]_{J'}^{J''}$ , which gives the probability of transition between the states involved is given by the spatial average ( see Lepard [13] ),

$$[S]_{J'}^{J''} = \overline{|\langle \psi'(J') | \mu_z | \psi''(J'') \rangle|^2} = \frac{1}{3} [G]_{J'}^{J''} \quad (37)$$

where

$$[G]_{J'}^{J''} = \left| \sum_{K'', K'} a_{K''}^{\tau''} a_{K'}^{\tau'} \langle e'v'; J'K' | \sum_r f_{-r} \mu_r | e''v''; J''K'' \rangle \right|^2 \quad (38)$$

In (38),  $|ev; JK\rangle$  are the basis functions of the rovibronic eigenfunctions  $\psi_{evr}$  and, in view of the approximation (28), can be written in the form.

$$|ev; JK\rangle = |ev\rangle |JK\rangle \quad (39)$$

Also  $f_{-r}$  are now the reduced operators which no longer depend on the magnetic quantum number  $M$ . Then (38) may be rewritten as

$$[G]_{J'}^{J''} = \left| \sum_{K'', K', r} a_{K''}^{\tau''} a_{K'}^{\tau'} \langle e'v' | \mu_r | e''v'' \rangle \langle J'K' | f_{-r} | J''K'' \rangle \right|^2 \quad (40)$$

Then, assuming that the absorption layer is thin, the expression for the line strength becomes

$$[S]_{J'}^{J''} = \frac{1}{3} \left| \sum_{K'', K', r} a_{K''}^{\tau''} a_{K'}^{\tau'} \langle e'v' | \mu_r | e''v'' \rangle \langle J'K' | f_{-r} | J''K'' \rangle \right|^2 \quad (41)$$

Note that  $r = \Delta K = K' - K'' = 0, \pm 1$  and  $\Delta J = J' - J'' = 0, \pm 1$  (See Lepard [13]).

Then the expression for the relative intensities of transitions may be written as

$$[I]_{J'}^{J''} = \nu g_{J''} (2J''+1) e^{-E/T^*} \frac{1}{3} \left| \sum_{K'', K', r} a_{K''}^{\tau''} a_{K'}^{\tau'} \langle e'v' | \mu_r | e''v'' \rangle \langle J'K' | f_r | J''K'' \rangle \right|^2 \quad (42)$$

where

$\nu$  = Frequency of absorption

$g_{J''}$  = Nuclear statistical weight for the initial state corresponding to the rotational quantum number

$E$  = Energy of the lower state in  $\text{cm}^{-1}$

$T^* = T / \left( \frac{hc}{k} \right) = T / (\text{SECOND RADIATION CONSTANT})$  in which

$T$  = Temperature in absolute units ( $^{\circ}\text{K}$ )

and  $k$  = Boltzmann constant.

The non-vanishing matrix elements given by Johns and Lepard [12] are listed here in TABLE 2. (Note that  $K$  is used here in place of  $\Omega$  ).



TABLE 2  
MATRIX ELEMENTS  $\langle J'K' | f_r | J''K'' \rangle$

$J'$	$K'$	
	$K''$	$K'' \pm 1$
$J''$	$\frac{K''}{\sqrt{J''(J''+1)}}$	$\sqrt{\frac{(J'' \mp K'')(J'' \pm K'' + 1)}{2J''(J''+1)}}$
$J''+1$	$\sqrt{\frac{[(J''+1)^2 - K''^2]}{(J''+1)(2J''+1)}}$	$\mp \sqrt{\frac{(J'' \pm K'' + 1)(J'' \pm K'' + 2)}{2(J''+1)(2J''+1)}}$
$J''-1$	$\sqrt{\frac{[J''^2 - K''^2]}{J''(2J''+1)}}$	$\pm \sqrt{\frac{(J'' \mp K'')(J'' \mp K'' - 1)}{2J''(2J''+1)}}$

Now we proceed to consider the possible cases of transitions that may occur between the rotation-electronic states in conformity with the criterion given in (31). Based on the combination of states and the real and imaginary nature of vibronic integrals as decided by the time reversal operator and symmetry elements of the point group, it is possible to obtain the relations for the line strengths and relative intensities for each possible case using (41) and (42).

CASE (1)  $\Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = A_1$

Since the product of the vibronic states  $\psi'_{ev}$  and  $\psi''_{ev}$  is of symmetry species  $A_1$ , we observe from (31) that one must have

$$\Gamma(\psi'_r) \times \Gamma(\psi''_r) = A_2 \quad (43a)$$

Then, from group theory, the only possible transitions are

$$A_1 \longleftrightarrow A_2 \quad \text{and} \quad B_1 \longleftrightarrow B_2$$

where the species are the full molecular group species for the rotational functions. Such transitions also depend on the existence of vibronic integrals

$$\langle \psi'_{ev} | \mu_\alpha | \psi''_{ev} \rangle \quad (43b)$$

where  $\mu_\alpha$  ( $\alpha = x, y, z$ ) are the molecule-fixed components of the dipole moment. It requires, in the present case, that

$$\Gamma(\mu_\alpha) = \Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = A_1 \quad (43c)$$

Thus the transitions are governed by  $\mu_z$  alone. We, therefore, conclude that the following transitions are allowed between the rotational states

$$\left. \begin{array}{l} A_1 \longleftrightarrow A_2 \quad \text{and} \quad B_1 \longleftrightarrow B_2 \\ \text{FOR } \Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = A_1 \quad \text{and} \quad \Gamma(\mu_z) = A_1 \end{array} \right\} (43d)$$

It is important to know whether the vibronic integral is real or imaginary, because this information simplifies the line strength and relative intensity calculations. This is done by looking at the effect of the time-reversal operator  $\hat{\theta}_t$ , which simply performs complex conjugation, on the vibronic integral.

The vibronic integral is real or imaginary according as the integral remains invariant or changes sign because of the effect of  $\hat{\theta}_t$ . In some cases, additional information is required regarding the effect of symmetry group elements on the vibronic integral.

In view of the fact that

$$\hat{\theta}_t \mu_z \equiv \hat{\theta}_t \mu_o = \mu_o \quad (44a)$$

and

$$\hat{\theta}_t \mu_{\pm} = \mu_{\mp} \quad (44b)$$

and if we assume, for the sake of convenience, that the functions  $\psi'_{ev}$  and  $\psi''_{ev}$  and hence their corresponding basis functions  $|e'v\rangle$  and  $|e''v\rangle$  are real, then

$$\hat{\theta}_t \langle e'v' | \mu_o | e''v'' \rangle = \langle e'v' | \mu_o | e''v'' \rangle$$

That is,

$$\hat{\theta}_t \langle \mu_o \rangle = \langle \mu_o \rangle \equiv \langle \mu_z \rangle \quad (44c)$$

(44c) shows that  $\langle \mu_z \rangle$  is invariant under the time-reversal operation, and, therefore, it is real.

Then from (44c) and (41), one obtains the line strengths

$$[S]_{J'}^{J''} = \frac{1}{3} \left| \sum_{K''} a_{K''}^{\tau''} a_{K''}^{\tau'} \langle e'v' | \mu_o | e''v'' \rangle \langle J'K'' | f_o | J''K'' \rangle \right|^2$$

or

$$[S]_{J'}^{J''} = \frac{\langle \mu_z \rangle^2}{3} \left| \sum_{K''} a_{K''}^{\tau''} a_{K''}^{\tau'} \langle J'K'' | f_o | J''K'' \rangle \right|^2 \quad (45a)$$

and, using (42), the corresponding relative intensities are

$$[I]_{J'}^{J''} = \nu g_{J''} (2J''+1) e^{-E/T^*} \frac{\langle \mu_z \rangle^2}{3} \left| \sum_{K''} a_{K''}^{\tau''} a_{K''}^{\tau'} \langle J'K'' | f_0 | J''K'' \rangle \right|^2 \quad (45b)$$

Here a well established fact that  $\Delta K = 0$  for  $\mu_z$  is used.

The values of  $\langle J'K'' | f_0 | J''K'' \rangle$  can be seen in TABLE 2.

$$\text{CASE (2): } \Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = A_2$$

From (31), we must have in this case

$$\Gamma(\psi'_r) \times \Gamma(\psi''_r) = A_1 \quad (46a)$$

which is possible only if

$$\Gamma(\psi'_r) = \Gamma(\psi''_r) = \text{SAME SPECIES} \quad (46b)$$

However, the requirement

$$\Gamma(\mu_\alpha) = A_2 \quad (46c)$$

shows that CASE (2) is not allowed since  $\mu_x$ ,  $\mu_y$  and  $\mu_z$  belong to the species  $B_1$ ,  $B_2$  and  $A_1$  respectively.

Therefore, transitions between the rotational states having the same symmetry species are forbidden. This conclusion is consistent with the fact that transitions can occur only between the energy states of opposite parity and not between those of the same parity. Thus the line strengths and, consequently, the relative intensities will be zero whenever the CASE (2) is encountered.

CASE (3):  $\Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = B_1$

Similar to the procedure adopted in CASES (1) and (2), we find from (31) that

$$\Gamma(\psi'_r) \times \Gamma(\psi''_r) = B_2 \quad (47a)$$

Then (47a) and the use of group theory leads to the possible transitions between the rotational states

$$A_1 \leftrightarrow B_2 \quad \text{and} \quad A_2 \leftrightarrow B_1$$

Also

$$\Gamma(\mu_x) = \Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = B_1 \quad (47b)$$

in this case. We see from (47b) that transitions are governed by  $\mu_x$ . Hence the allowed transitions between the rotational states are

$$\left. \begin{array}{l} A_1 \leftrightarrow B_2 \quad \text{and} \quad A_2 \leftrightarrow B_1 \\ \text{for } \Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = B_1 \quad \text{and} \quad \Gamma(\mu_x) = B_1 \end{array} \right\} \quad (47c)$$

Now we see the effect of  $\hat{\theta}_t$ , the time-reversal operator, on  $\langle e'v' | \mu_{\pm} | e''v'' \rangle$  while maintaining the assumption that  $|e'v'\rangle$  and  $|e''v''\rangle$  are real basis functions.

Then

$$\hat{\theta}_t \langle e'v' | \mu_{\pm} | e''v'' \rangle = \langle e'v' | \mu_{\mp} | e''v'' \rangle \quad (48a)$$

We see that the effect is not quite clear in the sense that we do not know whether the right hand side of (48a) is  $\langle e'v' | \mu_{\pm} | e''v'' \rangle$  or  $-\langle e'v' | \mu_{\pm} | e''v'' \rangle$ .

To decide it, we go on to see the effect of at least

two of the symmetry elements of the group. Using more than two elements of the group will be redundant for they do not provide additional information in this regard. Thus

$$\hat{\sigma}_v(xz) \langle e'v' | \mu_{\pm} | e''v'' \rangle = \langle e'v' | \mu_{\mp} | e''v'' \rangle \quad (48b)$$

$$\hat{\sigma}_v(yz) \langle e'v' | \mu_{\pm} | e''v'' \rangle = \langle e'v' | \mu_{\mp} | e''v'' \rangle \quad (48c)$$

Since (48b) and (48c) each must be equal to  $\langle e'v' | \mu_{\pm} | e''v'' \rangle$  to be non-vanishing, we obtain

$$\langle e'v' | \mu_{\pm} | e''v'' \rangle = \langle e'v' | \mu_{\mp} | e''v'' \rangle \neq 0 \quad (48d)$$

Use of (48d) in (48a) gives

$$\hat{\theta}_t \langle e'v' | \mu_{\pm} | e''v'' \rangle = \langle e'v' | \mu_{\pm} | e''v'' \rangle = \text{REAL.} \quad (48e)$$

(48e) suggests that the dipole moment component is  $\mu_x$  corresponding to the vibronic integral. Also, from (34) we find that

$$\mu_x = (\mu_+ + \mu_-)/\sqrt{2} \quad (49a)$$

$$\mu_y = (\mu_+ - \mu_-)/\sqrt{2} \quad (49b)$$

Then from (48d), (49a) and (49b) we find that

$$\begin{aligned} \langle e'v' | \mu_{\pm} | e''v'' \rangle &= \langle e'v' | \mu_{\mp} | e''v'' \rangle \\ &= \frac{1}{\sqrt{2}} \langle e'v' | \frac{\mu_+ + \mu_-}{\sqrt{2}} | e''v'' \rangle \\ &= \frac{1}{\sqrt{2}} \langle e'v' | \mu_x | e''v'' \rangle \\ &= \frac{1}{\sqrt{2}} \langle \mu_x \rangle \end{aligned} \quad (50)$$

Then using (50) in (41), we obtain the line strengths

$$[S]_{J'}^{J''} = \frac{1}{6} \langle \mu_x \rangle^2 \left| \sum_{K''} \left\{ a_{K''}^{\tau''} a_{K''-1}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle + a_{K''}^{\tau''} a_{K''+1}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle \right\} \right|^2 \quad (51)$$

and the corresponding relative intensities as follows.

$$[I]_{J'}^{J''} = \nu g_{J''} (2J''+1) e^{-E/T^*} \cdot \frac{1}{6} \langle \mu_x \rangle^2 \left| \sum_{K''} \left\{ a_{K''}^{\tau''} a_{K''-1}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle + a_{K''}^{\tau''} a_{K''+1}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle \right\} \right|^2 \quad (52)$$

Here again the values for the rotation matrices are given in TABLE 2.

CASE (4):  $\Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = B_2$

From (31) we obtain

$$\Gamma(\psi'_r) \times \Gamma(\psi''_r) = B_1 \quad (53a)$$

so, from the group theory, the only possible transitions are

$$A_1 \longleftrightarrow B_1 \quad \text{and} \quad A_2 \longleftrightarrow B_2$$

Also the requirement

$$\Gamma(\mu_x) = B_2 \quad (53b)$$

shows that transitions are governed by  $\mu_y$ , the  $y$ -component of the dipole moment in the molecular-fixed frame. Thus the allowed transitions between rotational

states are

$$\left. \begin{array}{l} A_1 \leftrightarrow B_1 \quad \text{and} \quad A_2 \leftrightarrow B_2 \\ \text{FOR} \quad \Gamma(\psi'_{ev}) \times \Gamma(\psi''_{ev}) = B_2 \quad \text{AND} \quad \Gamma(\mu_y) = B_2 \end{array} \right\} \quad (53c)$$

Now, assuming as before, the vibronic basis functions to be real, the time reversal operation on vibronic integral gives

$$\hat{\theta}_t \langle e'v' | \mu_{\pm} | e''v'' \rangle = \langle e'v' | \mu_{\mp} | e''v'' \rangle \quad (54a)$$

(54a) here is the same as (48a) despite the fact that the combination of vibronic states is different than that in (48a). Again we need to know the symmetry properties of the integral  $\langle e'v' | \mu_{\pm} | e''v'' \rangle$ .

Thus for the allowed transitions (53c) in this case, we have

$$\hat{\sigma}_v(xz) \langle e'v' | \mu_{\pm} | e''v'' \rangle = - \langle e'v' | \mu_{\mp} | e''v'' \rangle \quad (54b)$$

$$\hat{\sigma}_v(yz) \langle e'v' | \mu_{\pm} | e''v'' \rangle = - \langle e'v' | \mu_{\mp} | e''v'' \rangle \quad (54c)$$

Since (54b) and (54c) each must be equal to  $\langle e'v' | \mu_{\pm} | e''v'' \rangle$  in order to be nonvanishing, we obtain

$$\langle e'v' | \mu_{\pm} | e''v'' \rangle = - \langle e'v' | \mu_{\mp} | e''v'' \rangle \neq 0 \quad (54d)$$

Use of (54d) in (54a) gives

$$\hat{\theta}_t \langle e'v' | \mu_{\pm} | e''v'' \rangle = - \langle e'v' | \mu_{\pm} | e''v'' \rangle = \text{IMAGINARY} \quad (54e)$$



(54e) suggests that the transition moment involves  $\mu_y$ , the  $y$ -component of the dipole moment in the molecular-fixed coordinates. In view of the relation (49a), (49b) and (54d), we find that

$$\begin{aligned}
 \langle e'v' | \mu_{\pm} | e''v'' \rangle &= -\langle e'v' | \mu_{\mp} | e''v'' \rangle \\
 &= \frac{1}{2} \langle e'v' | (\mu_{\pm} + \mu_{\pm}) | e''v'' \rangle \\
 &= \frac{1}{2} \langle e'v' | (\mu_{\pm} - \mu_{\mp}) | e''v'' \rangle \\
 &= \pm \frac{i}{\sqrt{2}} \langle e'v' | \mu_y | e''v'' \rangle = \pm i \frac{\langle \mu_y \rangle}{\sqrt{2}} \quad (55)
 \end{aligned}$$

Then using (55) in (41), one obtains the relation of line strengths. Thus

$$[S]_{J'}^{J''} = \frac{\langle \mu_y \rangle^2}{6} \left| \sum_{K''} \left\{ a_{K''}^{\tau''} a_{K''-1}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle - a_{K''}^{\tau''} a_{K''+1}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle \right\} \right|^2 \quad (56)$$

and the relative intensities corresponding to (56) are

$$[I]_{J'}^{J''} = \nu g_{J''} (2J''+1) e^{-E/T^*} \frac{\langle \mu_y \rangle^2}{6} \left| \sum_{K''} \left\{ a_{K''}^{\tau''} a_{K''-1}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle - a_{K''}^{\tau''} a_{K''+1}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle \right\} \right|^2 \quad (57)$$

Thus, it is possible to calculate all the energies and the corresponding relative intensities.

### 3. APPLICATION TO $\tilde{C}^1B_1$ , AND $\tilde{D}^1A_1$ BANDS OF WATER

#### 3.1: CALCULATIONS OF EFFECTIVE ROTATIONAL CONSTANTS

The aim of this chapter is to apply the theory, developed in Chapter 2, to the representative molecules of symmetry  $C_{2v}$  so that the results of this theory and those obtained on the basis of our theory in Chapter 4 may be compared not only with each other but also with the experimentally observed ones.

Here we have considered  $H_2O$  and  $D_2O$  for the studies of rotation-electronic energies and relative transitions from the ground rotation-electronic states  $\tilde{X}^1A_1$ , to the  $3p$ -complex Rydberg state. We define the  $3p$ -orbitals, corresponding to the  $3p$ -complex state, by the orbital functions  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$  as follows:

$$|x\rangle = \frac{1}{\sqrt{2}} [|\Lambda = +1\rangle - |\Lambda = -1\rangle] \equiv \frac{1}{\sqrt{2}} [|1\rangle - |-1\rangle] \quad (58a)$$

$$|y\rangle = \frac{1}{\sqrt{2}} [|\Lambda = +1\rangle + |\Lambda = -1\rangle] \equiv \frac{1}{\sqrt{2}} [|1\rangle + |-1\rangle] \quad (58b)$$

$$|z\rangle = |\Lambda = 0\rangle \equiv |0\rangle \quad (58c)$$

where  $\Lambda = 0, \pm 1$  are the projections (taken along the molecule-fixed  $z$ -axis) of the orbital angular momentum quantum number  $L = 1$ . The axes in Eqs. (58) have been chosen such that the orbital functions  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$  transform like the  $x$ ,  $y$  and  $z$  components respectively of an ordinary polar vector as can be seen from the following explanation.

If  $J$  represents the total angular momentum quantum number and  $K$  its projections along the  $Z$ -axis in the molecule-fixed frame then, according to Hougen [9], the total angular momentum wavefunctions  $|JK\rangle$  for integral quantum numbers transform according to Eqs. (20). Note that the improper rotations were obtained by writing  $\hat{Q} = \hat{R}\hat{i}$  in which  $\hat{Q}$  is the improper rotation,  $\hat{R}$  the proper rotation and  $\hat{i}$  is the inversion operation (all referred to the molecule-fixed frame); improper rotations are also accompanied by the space-fixed inversion operation and thus the effect of  $\hat{Q}$  is identical to that of  $\hat{R}$ . The effect of the  $\hat{\sigma}(xz)$  and  $\hat{\sigma}(yz)$  operations are thus given by the  $\hat{C}_{2y}$  and  $\hat{C}_{2x}$  operations respectively.

Electronic orbital functions transform under rotations in the same way as the total angular momentum but the orbital functions are also affected by spatial transformations. Therefore, the effect of inversion  $\hat{i}$  in the molecule-fixed frame must be taken into consideration in the case of improper rotations. For  $\hat{i}$ , we know that the spherical harmonics for a single electron are altered by

$$\hat{i}|\ell\lambda\rangle = (-1)^\ell |\ell\lambda\rangle \quad (59)$$

where  $\ell$  is the electronic orbital quantum number and  $\lambda$  is one of the possible projections of  $\ell$ . Then assuming  $|L\Lambda\rangle$  to represent some linear combination of

products of orbital states for each electron, we see that

$$\hat{i} |L\Lambda\rangle = (-1)^{\sum_k \ell_k} |L\Lambda\rangle \quad (60)$$

where the index  $k$  runs over all the values of  $\ell$  corresponding to different states of the electrons under consideration. Recalling that  $\hat{Q} = \hat{R}\hat{i}$  where the effect of  $\hat{R}$  on  $|L\Lambda\rangle$  is identical to that given for  $|JK\rangle$  by Eqs. (20) we now see that

$$\hat{C}_{2z} |L\Lambda\rangle = (-1)^\Lambda |L\Lambda\rangle \quad (61a)$$

$$\hat{S}_v(xz) |L\Lambda\rangle = (-1)^{L-\Lambda+\sum_k \ell_k} |L-\Lambda\rangle \quad (61b)$$

$$\hat{S}_v(yz) |L\Lambda\rangle = (-1)^{L+\sum_k \ell_k} |L-\Lambda\rangle \quad (61c)$$

In practice, we are concerned with states arising from a single electron. In such a case  $L = \sum_k \ell_k \equiv \ell$  and our Eqs. (61) simplify to

$$\hat{C}_{2z} |L\Lambda\rangle = (-1)^\Lambda |L\Lambda\rangle \quad (62a)$$

$$\hat{S}_v(xz) |L\Lambda\rangle = (-1)^\Lambda |L-\Lambda\rangle \quad (62b)$$

$$\hat{S}_v(yz) |L\Lambda\rangle = |L-\Lambda\rangle \quad (62c)$$

Using the transformations given by Eqs. (62) on the  $p$ -orbital functions defined by Eqs. (58), we find that the functions  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$  transform like the  $x$ ,  $y$ ,  $z$  components respectively of an ordinary polar vector. Then  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$  have the symmetry

species  $B_1$ ,  $B_2$  and  $A_1$  respectively. In the ground state, the molecular core of  $H_2O$  (or  $D_2O$ ) is of symmetry  $B_1$  while the valence electron is a  $b_1$ -electron. Since a transition from the ground state to the excited  $3p$ -orbital states is brought about by the promotion of a  $b_1$  electron, the molecular core in both the ground and the excited state is of symmetry  $1B_1$ . The overall symmetry in each case is the product of the core symmetry and that of the electronic state symmetry. This yields the overall symmetry  $1B_1 \times 1B_1 = 1A_1$  for the ground state while for the components of the  $3p$ -orbital,  $1B_1 \times (1B_1, 1B_2, 1A_1) = (1A_1, 1A_2, 1B_1)$  correspond to the orbital functions ( $|\chi\rangle, |\psi\rangle, |\zeta\rangle$ ).

In order to carry out the numerical calculations of energies of the rotational states of  $H_2O$  and  $D_2O$  in different electronic states, one needs to know the numerical values of the rotational constants for each molecule in the ground rotation-electronic states  $\tilde{X}^1A_1$ , and the excited rotation-electronic states  $\tilde{C}^1B_1$ , and  $\tilde{D}^1A_1$ . The rotational constants of the  $\tilde{X}^1A_1$  state of  $H_2O$  and  $D_2O$  (Herzberg [7] and Benedict et.al.[2]) and the effective rotational constants of the  $\tilde{C}^1B_1$  rotation-electronic states of  $H_2O$  and  $D_2O$  (Johns [11]) are known. However, in order to obtain the rotation-electronic energies in the  $\tilde{D}^1A_1$  state of  $H_2O$  (or  $D_2O$ ), one needs to know the numerical values of the effective

rotational constants corresponding to the  $\tilde{D}^1A_1$  states of these molecules. Therefore, we need to establish the mathematical relations which connect the effective rotational constants  $A_{eff}$ ,  $B_{eff}$  and  $C_{eff}$  to their corresponding deperturbed (or  $\ell$  - uncoupled) rotational constants  $A$ ,  $B$  and  $C$ , consistent with our choice of axes  $a$ ,  $b$ , and  $c$ . We have chosen the  $b$  and  $c$  axes so that  $b = y$  is the two-fold rotation axis and  $c \equiv x$  is the axis perpendicular to the molecular plane, in accordance with the convention for an asymmetric-top molecule of  $C_{2v}$  symmetry.

To evaluate the relations for the effective rotational constants corresponding to the three rotation-electronic states, we consider the Hamiltonian

$$\hat{H} = \left\{ C (\hat{J}_x - \hat{L}_x)^2 + A (\hat{J}_y - \hat{L}_y)^2 + B (\hat{J}_z - \hat{L}_z)^2 \right\} \quad (63) \\ + \left\{ \mathcal{E}_x (1 - \hat{L}_x^2) + \mathcal{E}_y (1 - \hat{L}_y^2) + \mathcal{E}_z (1 - \hat{L}_z^2) \right\}$$

where the first bracket represents the rotational Hamiltonian while the second bracket represents the non-rotating Hamiltonian.  $\mathcal{E}_x$ ,  $\mathcal{E}_y$  and  $\mathcal{E}_z$  are the electronic energies for the states  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$  respectively.  $\hat{J}_\alpha$  ( $\alpha = x, y, z$ ) are the components of the total angular momentum  $\hat{J}$ , and

$\hat{L}_\alpha$  ( $\alpha = x, y, z$ ) are the components of the orbital angular momentum  $\hat{L}$ . It may be pointed out that the terms  $\mathcal{E}_\alpha (1 - \hat{L}_\alpha^2)$  are introduced in the Hamiltonian such that the resulting energies  $\mathcal{E}_\alpha$  ( $\alpha = x, y, z$ )

corresponding to the three orbital electronic states do not interact with one another. The choice of  $\hat{C}_\alpha(1-L_\alpha)$  is rather artificial because the wavefunctions of the three orbital electronic states considered in this work are such as to lead to the same electronic energies as would have been obtained by merely adding the electronic energies.

Rearrangement of Eq. (63) leads to the result

$$\hat{H} = \{ \hat{H}_r + \hat{H}_{el} + (A+B+C) \} + \hat{H}_{re} \equiv \hat{H}_{diag} + \hat{H}_{re} \quad (64)$$

where

$$\hat{H}_r = A \hat{J}_y^2 + B \hat{J}_z^2 + C \hat{J}_x^2 \quad (65a)$$

$$\hat{H}_{el} = (\mathcal{E}_x - C)(1 - \hat{L}_x^2) + (\mathcal{E}_y - A)(1 - \hat{L}_y^2) + (\mathcal{E}_z - B)(1 - \hat{L}_z^2) \quad (65b)$$

$$\hat{H}_{re} = -2A \hat{J}_y \hat{L}_y - 2B \hat{J}_z \hat{L}_z - 2C \hat{J}_x \hat{L}_x \quad (65c)$$

The Hamiltonians  $\hat{H}_r$ ,  $\hat{H}_{el}$  and  $\hat{H}_{re}$  represent purely rotational, purely electronic and rotation-electronic interaction parts of  $\hat{H}$  respectively. Note that  $\hat{H}$  has the matrix elements that are purely diagonal in the electronic quantum numbers. The off-diagonal matrix elements, given by  $\hat{H}_{re}$ , may be treated as a perturbation.

The orbital electronic functions  $|\alpha\rangle$  ( $\alpha = x, y, z$ ) on being operated by the orbital angular momentum components  $\hat{L}_\alpha$  ( $\alpha = x, y, z$ ) behave as follows

$$\hat{L}_x|x\rangle = 0 \quad ; \quad \hat{L}_y|x\rangle = i|z\rangle \quad ; \quad \hat{L}_z|x\rangle = |y\rangle \quad (66a)$$

$$\hat{L}_x|y\rangle = |z\rangle \quad ; \quad \hat{L}_y|y\rangle = 0 \quad ; \quad \hat{L}_z|y\rangle = |x\rangle \quad (66b)$$

$$\hat{L}_x|z\rangle = |y\rangle \quad ; \quad \hat{L}_y|z\rangle = -i|x\rangle \quad ; \quad \hat{L}_z|z\rangle = 0 \quad (66c)$$

where  $i \equiv \sqrt{-1}$ . If we represent the rotation functions by  $|R\rangle \equiv |JK\rangle$ , then we can write the entire wave-function as

$$|JK\alpha\rangle \equiv |R\alpha\rangle = |R\rangle|\alpha\rangle \quad (67)$$

for the rotation-electronic states. Thus, in view of Eqs. (67), we see from Eq. (64) that the matrix elements for a definite electronic state  $|\alpha\rangle$ , to second order, are

$$\langle R'\alpha | \hat{H} | R\alpha \rangle = \langle R'\alpha | \hat{H}_{diag} | R\alpha \rangle + \sum_{R'', \alpha'' \neq \alpha} \frac{\langle R'\alpha | \hat{H}_{re} | R''\alpha'' \rangle \langle R''\alpha'' | \hat{H}_{re} | R\alpha \rangle}{\mathcal{E}_{R\alpha}^{(0)} - \mathcal{E}_{R''\alpha''}^{(0)}} \quad (68a)$$

Since the first-order contribution, given by  $\langle R'\alpha | \hat{H}_{re} | R\alpha \rangle$  vanishes. The first term,  $\langle R'\alpha | \hat{H}_{diag} | R\alpha \rangle$ , gives the zero-order contribution to the total energy; that is,

$$\mathcal{E}_{R\alpha}^{(0)} = \langle R\alpha | \hat{H}_{diag} | R\alpha \rangle \quad (68b)$$

In Eq. (68a), we have assumed that the electronic spacing is much larger than the spacing of the rotational energy levels. That is,

$$\mathcal{E}_{R\alpha}^{(0)} - \mathcal{E}_{R''\alpha''}^{(0)} \simeq \mathcal{E}_{\alpha}^{(0)} - \mathcal{E}_{\alpha''}^{(0)} \quad (68c)$$

This approximation is reasonable because the purely rotational separations involving the rotational constants



A, B and C, are insignificant when compared with the electronic separations. The first term of Eq. (68a) has the matrix elements

$$\langle R'\alpha | \hat{H}_{diag} | R\alpha \rangle = \langle R' | \hat{H}_r | R \rangle + [\langle \alpha | \hat{H}_{el} | \alpha \rangle + (A+B+C)] \delta_{R'R} \quad (69)$$

If we define the effective electronic energy contribution by

$$\mathcal{E}_{eff\alpha} = [\langle \alpha | \hat{H}_{el} | \alpha \rangle + (A+B+C)] \quad (70)$$

we can write Eq. (69) in the form

$$\langle R'\alpha | \hat{H}_{diag} | R\alpha \rangle = \langle R' | \hat{H}_r | R \rangle + \mathcal{E}_{eff\alpha} \delta_{R'R} \quad (71)$$

Then, the zero-order energy contribution is

$$\mathcal{E}_{R\alpha}^{(0)} = \langle R | \hat{H}_r | R \rangle + \mathcal{E}_{eff\alpha} \quad (72)$$

where we find, using Eqs. (66), that

$$\mathcal{E}_{effx} = (\mathcal{E}_x - C) + (A+B+C) \quad (73a)$$

$$\mathcal{E}_{effy} = (\mathcal{E}_y - A) + (A+B+C) \quad (73b)$$

$$\mathcal{E}_{effz} = (\mathcal{E}_z - B) + (A+B+C) \quad (73c)$$

We note from (72) that

$$\mathcal{E}_{R\alpha}^{(0)} - \mathcal{E}_{R''\alpha''}^{(0)} = [\mathcal{E}_{eff\alpha} - \mathcal{E}_{eff\alpha''}] + [\langle R | \hat{H}_r | R \rangle - \langle R'' | \hat{H}_r | R'' \rangle] \quad (74)$$

Because of our earlier assumption that the rotational states are very closely spaced compared to the electronic states we can ignore the second bracket on the right hand side of Eq. (74). Then from Eqs. (74) and (69), we have

$$\mathcal{E}_{R\alpha}^{(0)} - \mathcal{E}_{R\alpha''}^{(0)} \simeq \mathcal{E}_{\alpha}^{(0)} - \mathcal{E}_{\alpha''}^{(0)} \equiv \mathcal{E}_{\text{eff}\alpha} - \mathcal{E}_{\text{eff}\alpha''} \quad (75)$$

Thus, using the result in Eq. (75) we can rewrite Eq. (68a) as follows

$$\langle R\alpha | \hat{H} | R\alpha \rangle = \langle R\alpha | \hat{H}_{\text{diag}} | R\alpha \rangle + \sum_{R'', \alpha'' \neq \alpha} \frac{\langle R\alpha | \hat{H}_{\text{re}} | R''\alpha'' \rangle \langle R''\alpha'' | \hat{H}_{\text{re}} | R\alpha \rangle}{\mathcal{E}_{\text{eff}\alpha} - \mathcal{E}_{\text{eff}\alpha''}} \quad (76)$$

Since for the states  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$ , we have

$$\langle R'x | \hat{H}_{\text{re}} | R''y \rangle \langle R''y | \hat{H}_{\text{re}} | Rx \rangle = \langle R'y | \hat{H}_{\text{re}} | R''x \rangle \langle R''x | \hat{H}_{\text{re}} | Ry \rangle = 4B^2 \langle R' | \hat{J}_z^2 | R \rangle \quad (77a)$$

$$\langle R'x | \hat{H}_{\text{re}} | R''z \rangle \langle R''z | \hat{H}_{\text{re}} | Rx \rangle = \langle R'z | \hat{H}_{\text{re}} | R''x \rangle \langle R''x | \hat{H}_{\text{re}} | Rz \rangle = 4A^2 \langle R' | \hat{J}_y^2 | R \rangle \quad (77b)$$

$$\langle R'y | \hat{H}_{\text{re}} | R''z \rangle \langle R''z | \hat{H}_{\text{re}} | Ry \rangle = \langle R'z | \hat{H}_{\text{re}} | R''y \rangle \langle R''y | \hat{H}_{\text{re}} | Rz \rangle = 4C^2 \langle R' | \hat{J}_x^2 | R \rangle \quad (77c)$$

we get from Eqs. (71), (76) and (77)

$$\langle R'x | \hat{H} | Rx \rangle = \langle R' | \hat{H}_r | R \rangle + \mathcal{E}_{\text{eff}x} \delta_{RR'} + \frac{4B^2 \langle R' | \hat{J}_z^2 | R \rangle}{\mathcal{E}_{\text{eff}x} - \mathcal{E}_{\text{eff}y}} + \frac{4A^2 \langle R' | \hat{J}_y^2 | R \rangle}{\mathcal{E}_{\text{eff}x} - \mathcal{E}_{\text{eff}z}} \quad (78a)$$

$$\langle R'y | \hat{H} | Ry \rangle = \langle R' | \hat{H}_r | R \rangle + \mathcal{E}_{\text{eff}y} \delta_{RR'} + \frac{4B^2 \langle R' | \hat{J}_z^2 | R \rangle}{\mathcal{E}_{\text{eff}y} - \mathcal{E}_{\text{eff}x}} + \frac{4C^2 \langle R' | \hat{J}_x^2 | R \rangle}{\mathcal{E}_{\text{eff}y} - \mathcal{E}_{\text{eff}z}} \quad (78b)$$

$$\langle R'z | \hat{H} | Rz \rangle = \langle R' | \hat{H}_r | R \rangle + \mathcal{E}_{\text{eff}z} \delta_{RR'} + \frac{4A^2 \langle R' | \hat{J}_y^2 | R \rangle}{\mathcal{E}_{\text{eff}z} - \mathcal{E}_{\text{eff}x}} + \frac{4C^2 \langle R' | \hat{J}_x^2 | R \rangle}{\mathcal{E}_{\text{eff}z} - \mathcal{E}_{\text{eff}y}} \quad (78c)$$

Collecting coefficients of  $\hat{J}_x^2$ ,  $\hat{J}_y^2$  and  $\hat{J}_z^2$  with the aid of Eq. (65a), we find that

$$\langle R'\alpha | \hat{H} | R\alpha \rangle = \langle R' | (\hat{H}_{eff})_\alpha | R \rangle + \mathcal{E}_{eff\alpha} \delta_{RR'}, \quad (79)$$

where

$$(\hat{H}_{eff})_\alpha = (A_{eff} \hat{J}_y^2 + B_{eff} \hat{J}_z^2 + C_{eff} \hat{J}_x^2)_\alpha \quad ; \quad (\alpha = x, y, z) \quad (80)$$

and the effective rotational constants for each state  $|\alpha\rangle \equiv |x\rangle$ ,  $|y\rangle$  and  $|z\rangle$  are given by the following equations.

For electronic state  $|x\rangle$ :

$$A_{eff} = A \left[ 1 + \frac{4A}{\mathcal{E}_{effx} - \mathcal{E}_{effz}} \right] \quad (81a)$$

$$B_{eff} = B \left[ 1 + \frac{4B}{\mathcal{E}_{effx} - \mathcal{E}_{effy}} \right] \quad (81b)$$

$$C_{eff} = C \quad (81c)$$

For electronic state  $|y\rangle$ :

$$A_{eff} = A \quad (82a)$$

$$B_{eff} = B \left[ 1 + \frac{4B}{\mathcal{E}_{effy} - \mathcal{E}_{effx}} \right] \quad (82b)$$

$$C_{eff} = C \left[ 1 + \frac{4C}{\mathcal{E}_{effy} - \mathcal{E}_{effz}} \right] \quad (82c)$$

For electronic state  $|z\rangle$ :

$$A_{eff} = A \left[ 1 + \frac{4A}{\mathcal{E}_{effz} - \mathcal{E}_{effx}} \right] \quad (83a)$$

$$B_{eff} = B \quad (83b)$$

$$C_{eff} = C \left[ 1 + \frac{4C}{\mathcal{E}_{effz} - \mathcal{E}_{effy}} \right] \quad (83c)$$

On comparing the results given here by Eqs.(81), (82) and (83) with Eqs. (6x), (6y) and (6z) given by Creutzberg and Hougen [5] for the analogous spin problem, later adapted by Johns [11] for this orbital problem, we find the following correspondence between the spin state functions and the orbital electronic functions.

TABLE 3  
CORRESPONDENCE BETWEEN THE SPIN FUNCTIONS  
(ADOPTED EARLIER) AND ELECTRONIC FUNCTIONS

Elec- tronic State	J.W.C. JOHNS	PRESENT WORK		Selection Rule From Symmetry (Allowed/ Forbidden)
	Spin Function	Elec- tronic Function	Component of Dipole Active in Transition	
$\tilde{C}^1B_1$	$ x\rangle$	$ z\rangle$	$\mu_x$	Allowed
$\tilde{D}^1A_1$	$ y\rangle$	$ x\rangle$	$\mu_z$	Allowed
$^1A_2$	$ z\rangle$	$ y\rangle$	$\mu_y$	Forbidden

The difference arises because of the fact that the components of orbital functions behave like the ordinary polar vectors rather than the components of axial vectors; the latter is the characteristic of the spin functions. Also we have chosen  $x$ ,  $y$ ,  $z$  axes of principal moments of inertia as  $c$ ,  $a$ ,  $b$  respectively; which is different from the earlier choice of  $b$ ,  $c$ ,  $a$  respectively as is evident by comparing FIG. 3 (a) and 3(b).

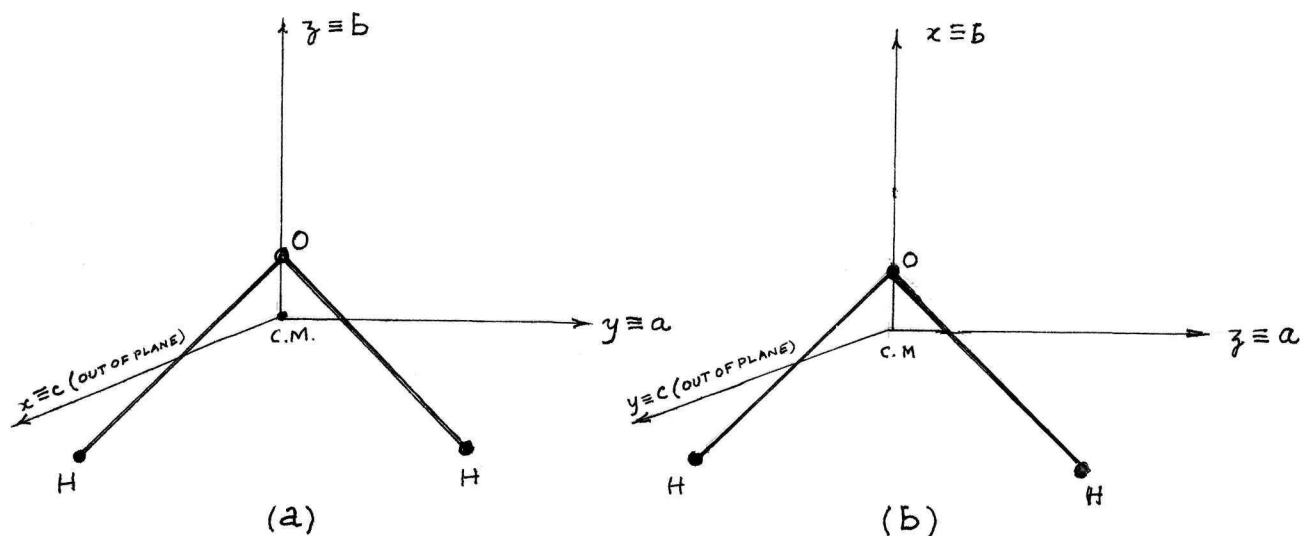


FIG. 3. (a) Represents our choice of axes  
 (b) Represents choice of axes adopted by  
 Johns for  $\text{H}_2\text{O}$  molecules.

Therefore, by replacing in Eqs. (6x), (6y) and (6z) of  
 Creutzberg and Hougen

$$\left. \begin{array}{lll} E_x \rightarrow \mathcal{E}_{\text{eff}z} & ; & E_y \rightarrow \mathcal{E}_{\text{eff}x} & ; & E_z \rightarrow \mathcal{E}_{\text{eff}y} \\ A \rightarrow B & ; & B \rightarrow C & ; & C \rightarrow A \end{array} \right\} \quad (84)$$

Eq. (6x), also given by Johns [41], reduces to Eq. (83);

Eq. (6y) reduces to Eq. (81) and Eq. (6z) to Eq. (82).

Notice that we must use the effective values of electronic energy  $\mathcal{E}_{\text{eff}\alpha}$  ( $\alpha = x, y, z$ ) in the expressions (81), (82) and (83) instead of the "deperturbed" values,  $E_\alpha$ , used by Creutzberg and Hougen [5]. Note that Eq. (82) is not needed since the transitions to the  $|y\rangle$  electronic state (CASE (2) of Chapter 2) are forbidden.

To calculate the effective rotational constants for the rotational band in the  $\tilde{D}^1A_1$  electronic state (that is,  $|x\rangle$  state) the following method has been adopted:

(1): The experimental values of effective rotational constants  $A_{eff}$ ,  $B_{eff}$  and  $C_{eff}$  for  $\tilde{C}^1B_1$  rotational-electronic states of  $H_2O$  (or  $D_2O$ ) (Johns [11]) are used in Eqs. (83) and the corresponding deperturbed rotational constants  $A$ ,  $B$  and  $C$  obtained, where the differences in the effective electronic energies ( $\mathcal{E}_{eff_z} - \mathcal{E}_{eff_x}$ ) and ( $\mathcal{E}_{eff_z} - \mathcal{E}_{eff_y}$ ) used here are given by Johns [11]. Thus,

For  $H_2O$ :

$$\left. \begin{aligned} \mathcal{E}_{eff_z} - \mathcal{E}_{eff_x} &= -1434 \text{ cm}^{-1} \\ \mathcal{E}_{eff_z} - \mathcal{E}_{eff_y} &= 3587 \text{ cm}^{-1} \end{aligned} \right\} \quad (85a)$$

For  $D_2O$ :

$$\left. \begin{aligned} \mathcal{E}_{eff_z} - \mathcal{E}_{eff_x} &= -1323 \text{ cm}^{-1} \\ \mathcal{E}_{eff_z} - \mathcal{E}_{eff_y} &= 2198 \text{ cm}^{-1} \end{aligned} \right\} \quad (85b)$$

The deperturbed ( $\ell$  - uncoupled) rotational constants for  $H_2O$  and  $D_2O$  so obtained are listed in TABLE 4.

TABLE 4  
ROTATIONAL CONSTANTS AND BAND ORIGINS OF  
 $\tilde{X}^1A_1$ ,  $\tilde{C}^1B_1$  AND  $\tilde{D}^1A_1$  STATES OF  $H_2O$  AND  $D_2O$ .

I Notation	II Constants for $H_2O$ ( $cm^{-1}$ )	III Constants for $D_2O$ ( $cm^{-1}$ )
	<u><math>\tilde{X}^1A_1</math> States</u>	<u><math>\tilde{X}^1A_1</math> States</u>
$\nu_0$	0.0	0.0
A	27.877	15.38
B	14.512	7.27
C	9.285	4.85
	<u><math>\tilde{C}^1B_1</math> States</u>	<u><math>\tilde{C}^1B_1</math> States</u>
$\nu_0'$	80624.7	80751.9
$A_{eff}$	25.90	14.64
$B_{eff}$	12.64	6.31
$C_{eff}$	8.55	4.42
	<u><math>\tilde{D}^1A_1</math> States</u>	<u><math>\tilde{D}^1A_1</math> States</u>
$\nu_0'$	82058.7	82074.9
$A_{eff}$	30.30 (2537)*	16.06 (2387)*
$B_{eff}$	12.76 (7281)*	6.355(2325)*
$C_{eff}$	8.47	4.38
	<u>For Deperturbed States</u>	<u>For Deperturbed States</u>
$A'$	28.10	15.35
$B'$	12.64	6.31
$C'$	8.47	4.38

\* NOTE THAT THE NUMBERS APPEARING IN SMALL BRACKETS INDICATE ADDITIONAL DIGITS UP TO SIX OR SEVEN DECIMAL PLACE ACCURACY FOR THE EFFECTIVE ROTATIONAL CONSTANTS IN  $\tilde{D}^1A_1$  STATES, USED IN CALCULATIONS.

Johns[11] has obtained the same results for A, B and C for H<sub>2</sub>O and D<sub>2</sub>O using Eq. (6x) of Creutzberg and Hougen, as expected, because a difference in the choice of axes should not affect the rotational constants.

(2): The deperturbed rotational constants obtained in step (1) (given in TABLE 4) and the differences in various orbital states (obtained from Eqs.(85)) for H<sub>2</sub>O and D<sub>2</sub>O

For H<sub>2</sub>O:

$$\left. \begin{aligned} \mathcal{E}_{effx} - \mathcal{E}_{effz} &= 1434 \text{ cm}^{-1} \\ \mathcal{E}_{effx} - \mathcal{E}_{effy} &= (\mathcal{E}_{effz} - \mathcal{E}_{effy}) - (\mathcal{E}_{effz} - \mathcal{E}_{effx}) = 5021 \text{ cm}^{-1} \end{aligned} \right\} (86a)$$

For D<sub>2</sub>O:

$$\left. \begin{aligned} \mathcal{E}_{effx} - \mathcal{E}_{effz} &= 1323 \text{ cm}^{-1} \\ \mathcal{E}_{effx} - \mathcal{E}_{effy} &= (\mathcal{E}_{effz} - \mathcal{E}_{effy}) - (\mathcal{E}_{effz} - \mathcal{E}_{effx}) = 3521 \text{ cm}^{-1} \end{aligned} \right\} (86b)$$

are used for H<sub>2</sub>O and D<sub>2</sub>O to calculate their effective rotational constants  $A_{eff}$ ,  $B_{eff}$  and  $C_{eff}$  for the rotational band of the electronic state  $\tilde{D}^1A_1$ . The results thus obtained are given in TABLE 4.

The effective rotational constants for H<sub>2</sub>O and D<sub>2</sub>O for the bands  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  are used in calculating the energies of rotational levels as described in Section 3.3.

### 3.2 CALCULATIONS OF BAND ORIGINS OF $\tilde{D}^1A_1$ BANDS OF H<sub>2</sub>O AND D<sub>2</sub>O

Since the numerical values of the separation between



the electronic states  $|x\rangle (\equiv \tilde{D}^1A_1)$  and  $|z\rangle (\equiv \tilde{C}^1B_1)$ , and also the band origins of the  $|z\rangle (\equiv \tilde{C}^1B_1)$  electronic state of  $H_2O$  and  $D_2O$  are known (Johns [11] and [2]), the band origin of the  $\tilde{D}^1A_1$  electronic state for each  $H_2O$  and  $D_2O$  have been evaluated as follows.

For  $H_2O$ :

The band origin of the  $\tilde{C}^1B_1$  state is

$$\nu'_0(\tilde{C}^1B_1) \equiv \mathcal{E}_{eff_z} = 80624.7 \text{ cm}^{-1}$$

and since

$$\mathcal{E}_{eff_x} - \mathcal{E}_{eff_z} = 1434 \text{ cm}^{-1}$$

the band origin of the  $\tilde{D}^1A_1$  state of  $H_2O$  is

$$\nu'_0(\tilde{D}^1A_1) \equiv \mathcal{E}_{eff_x} = 82058.7 \text{ cm}^{-1}$$

For  $D_2O$ :

The band origin of the  $\tilde{C}^1B_1$  state is

$$\nu'_0(\tilde{C}^1B_1) \equiv \mathcal{E}_{eff_z} = 80751.9 \text{ cm}^{-1}$$

and since

$$\mathcal{E}_{eff_x} - \mathcal{E}_{eff_z} = 1323 \text{ cm}^{-1}$$

the band origin of the  $\tilde{D}^1A_1$  state of  $D_2O$  is

$$\nu'_0(\tilde{D}^1A_1) \equiv \mathcal{E}_{eff_x} = 82074.9 \text{ cm}^{-1}$$

All these results are given in TABLE 4.

### 3.3 COMPUTATIONAL DETAILS OF ENERGIES

In order to carry out the numerical calculations of energies of the rotational states of  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  a computer programme has been developed which uses Eq.(17) to evaluate and store in the computer memory the matrix elements of a  $(2J+1) \times (2J+1)$  matrix for each of the rotational quantum numbers from  $J = 0$  through  $J = 11$ . The matrix so obtained for each single rotational quantum number  $J$  is diagonalized using a sub-routine. The eigenvalues (which are merely the rotational energies) and their corresponding eigenvectors have been generated. The energies are rearranged in order of decreasing energy for each rotational quantum number  $J$  to facilitate the assignment of the label  $\tau$  to each energy state. Thus, for  $J = 2$ , the energy levels have been identified by  $J_\tau = 2_2, 2_1, 2_0, 2_{-1}$  and  $2_{-2}$ , arranged in decreasing order of energy; there being  $(2J+1)$  energy states for a single  $J$ . In this way the rotational energies of the ground electronic state  $\tilde{X}^1A_1$  and those of the excited states  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$ , have been calculated using the ground state rotational constants and the effective rotational constants for the bands  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$ . The constants are given in TABLE 4. The values of band origins  $\nu'_0 = 80624.7 \text{ cm}^{-1}$  and  $\nu'_0 = 82058.7 \text{ cm}^{-1}$  for  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  electronic bands of  $\text{H}_2\text{O}$  respectively are added to the rotational

energies calculated above for  $\text{H}_2\text{O}$  so as to obtain the true energies of the rotation-electronic states. Similarly, for  $\text{D}_2\text{O}$  the band origins  $\nu'_0 = 80751.9 \text{ cm}^{-1}$  and  $\nu'_0 = 82074.9 \text{ cm}^{-1}$  are added to the rotational energies of the  $\tilde{\text{C}}^1\text{B}_1$  and  $\tilde{\text{D}}^1\text{A}_1$  electronic bands respectively to obtain the true rotation-electron energies. Since both  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  are considered as rigid rotors in the ground electronic state  $\tilde{\text{X}}^1\text{A}_1$ , where the zero point energy of molecular vibration is ignored, the band origin is assigned a zero frequency ( $\nu_0 = 0$ ). The computed values of energies for the rotational states of the electronic bands  $\tilde{\text{X}}^1\text{A}_1$ ,  $\tilde{\text{C}}^1\text{B}_1$  and  $\tilde{\text{D}}^1\text{A}_1$ , for  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  are given in TABLES II.1 and II.2, respectively (APPENDIX II) up to the rotational quantum number  $J = 11$ .

### 3.4 THE NUCLEAR STATISTICAL WEIGHT

Since the transition intensities are affected by the nuclear spin of the nuclei in a molecule, we have considered their role in our calculations of relative intensities.

The eigenfunctions of homonuclear molecules are categorized as symmetric or antisymmetric depending on whether or not the eigenfunctions remain invariant on interchanging the coordinates of the nuclei. Let  $I$  be the nuclear spin of each nucleus, then if the identical nuclei are Bosons, there are  $(I + 1) \cdot (2I + 1)$

symmetric and  $I \cdot (2I + 1)$  antisymmetric eigenfunctions of the molecule with respect to interchange of nuclei. The reverse is true of Fermions, where the weight of antisymmetric states is  $(I + 1) \cdot (2I + 1)$  and that of symmetric ones is  $I \cdot (2I + 1)$ . Then the ratio,  $\xi$ , of the weights of symmetric to antisymmetric states in case of Bosons or the weights of antisymmetric to symmetric states in the case of Fermions, is given by

$$\xi = \frac{(I + 1)}{I} = \left( \frac{\text{Symmetric States}}{\text{Antisymmetric States}} \right)_{\text{Bosons}} = \left( \frac{\text{Antisymmetric States}}{\text{Symmetric States}} \right)_{\text{Fermions}} \quad (87)$$

Thus for an  $\text{H}_2\text{O}$  molecule, since the exchange of position coordinates occurs between the two H - atoms, each of nuclear spin  $I = 1/2$  (in units of  $\hbar$ ),  $s : a = 1 : 3$  while for a  $\text{D}_2\text{O}$  molecule in which deuterons are the Bosons, with nuclear spin  $I = 1$ ,  $s : a = 2 : 1$ . Here  $s$  and  $a$  denote symmetric state and antisymmetric state respectively. Thus the statistical weight of an antisymmetric state is three times that of a symmetric state in  $\text{H}_2\text{O}$  whereas the weight of a symmetric state is twice that of an antisymmetric state in  $\text{D}_2\text{O}$ . Consequently, the intensity ratios will be  $1 : 3$  in  $\text{H}_2\text{O}$  and  $2 : 1$  in  $\text{D}_2\text{O}$  for  $s : a$ .

Now a  $\hat{C}_{2z}$  operation gives a pure exchange of two nuclei. Then from the character table of  $C_{2v}$  point group (APPENDIX I) we see that  $A_1$  and  $A_2$  are each of

character +1 while  $B_1$  and  $B_2$  each has a character -1 under  $\hat{C}_{2z}$  operation. Thus energy levels of species  $A_1$ ,  $A_2$  are symmetric while  $B_1$ ,  $B_2$  are anti-symmetric. Also the  $\hat{\sigma}(yz)$  operation gives pure inversion so  $A_1$ ,  $B_1$  are of + parity and  $A_2$ ,  $B_2$  are of - parity. Thus, we can summarize our results as follows:

Species	Parity	S/a	Statistical Weight	
			H <sub>2</sub> O	D <sub>2</sub> O
$A_1$	+	S	1	2
$A_2$	-	S	1	2
$B_1$	-	a	3	1
$B_2$	+	a	3	1

### 3.5 COMPUTATIONAL DETAILS OF RELATIVE TRANSITION INTENSITIES.

The numerical computation has been carried out for two cases of transitions that are permitted by the symmetry requirement of the matrix elements. The permissible cases are

- (i)  $\tilde{X}^1A_1 - \tilde{C}^1B_1$  Transitions (Case (3) of Chapter 2).
- (ii)  $\tilde{X}^1A_1 - \tilde{D}^1A_1$  Transitions (Case (1) of Chapter 2).

The computational details for each case are exactly the same except for the difference in the subroutine which changes the symmetry codes of the upper levels appropriate to the bands involved in the transitions. For example, for the Case (i) which involves a transition between the rotational states of  $\tilde{X}^1A_1$  and  $\tilde{C}^1B_1$

electronic states, the only possible transitions between the rotational states (identified by their rotational symmetry species) are

$$A_1 \leftrightarrow B_2 \quad \text{and} \quad A_2 \leftrightarrow B_1$$

where the dipole component active in the transitions is  $\mu_x$  which has the symmetry species  $\Gamma(\mu_x) = B_1$ .

Similarly, for the case (ii) which involves the transitions between the bands  $\tilde{X}^1A_1$  and  $\tilde{D}^1A_1$ , the possible combinations of rotational states are

$$A_1 \leftrightarrow A_2 \quad \text{and} \quad B_1 \leftrightarrow B_2$$

where in this case, the dipole component  $\mu_z$  is active. The symmetry species is  $\Gamma(\mu_z) = A_1$ .

In each case, eigenvalues and eigenvectors are calculated for both the ground rotation-electronic states  $\tilde{X}^1A_1$  and the excited electronic states  $\tilde{C}^1B_1$  (or  $\tilde{D}^1A_1$  in the case (ii)) and stored in the computer memory as was done in section 3.3. By calling a subroutine, each energy level is assigned a symmetry species (in the form of a code) consistent with the criteria established earlier (in Chapter 2, TABLE 1). At any instant, the symmetry codes so assigned to the energy states are stored for a given quantum number  $J = J''$  of rotation in the  $\tilde{X}^1A_1$  state and for  $J' = J'' - 1$ ,  $J''$  and  $J'' + 1$  in the excited electronic state  $\tilde{C}^1B_1$  (or  $\tilde{D}^1A_1$ ). Thus, for example, in our case, we reserved the code 1

to represent the symmetry species  $A_1$ ; 2 for  $A_2$ ; 3 for  $B_1$  and 4 for  $B_2$ . Subject to the allowed combination of states in transitions, the symmetry codes of the excited states for  $J' = J'' - 1$ ,  $J''$  and  $J'' + 1$ , stored earlier, are changed only to those of initial states for which combinations of states are allowed. That is, if the transitions  $A_1 \leftrightarrow B_2$  and  $A_2 \leftrightarrow B_1$  are allowed (say), the codes for the upper state species  $A_1$ ,  $A_2$ ,  $B_1$  and  $B_2$  must be changed to those of  $B_2$ ,  $B_1$ ,  $A_2$  and  $A_1$  respectively. This is done by calling a subroutine consistent with the selection rules. This technique, in effect, assigns the same code to those initial and final states which are permitted to combine by the selection rule. Thus, whenever the codes in the initial state and the final state match, the programme allows one to calculate the line strength and the relative transition intensity using (51) and (52) respectively for the  $\tilde{C}^1B_1$  electronic band and (45a) and (45b) for the rotational transitions to the  $\tilde{D}^1A_1$  electronic band. The nuclear statistical weight is attached to the relative intensity as described earlier in Section 3.4. It may be pointed out here that the frequencies  $\nu$  in the relative transition intensity relations (52) and (45b) are not taken into account in our calculation, because it varies very slowly from one line position to another. Also we have used the following in the calculations.

$$\langle \mu_x \rangle = \langle \mu_z \rangle = 1$$

$$T = 293^\circ \text{ K}$$

$$\left( \frac{hc}{k} \right) = 1.438786 \text{ }^\circ\text{K-cm. (Taken from [4] )}$$

Thus, the resulting line strengths and relative transition intensities calculated for up to  $J = 10$  are obtained. The results so obtained for the relative transition intensities for the  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  bands in  $H_2O$  and  $D_2O$  are given in TABLES III.1, III.2, III.3 and III.4 in APPENDIX III.

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#### 4. ROTATION-ELECTRONIC INTERACTION THEORY

##### 4.1 THE ROLE OF ROTATION-ELECTRONIC INTERACTION

In our theory presented in this chapter, it is assumed that the ground state rotational energies are governed, to a good approximation, by the rigid rotor theory. Therefore, the rotational energies in the  $\tilde{X}^1A_1$  electronic state can be obtained by using the rigid rotor theory described in Chapter 2.

In the excited states, however, the coupling of electronic angular momentum with rotation results in interaction terms, between the various angular momenta, in the Hamiltonian. Creutzberg and Hougen [5] have discussed the case of purely spin angular momenta for an approximately symmetric-top  $C_{2v}$  molecule which results in spin-spin and spin-rotation terms. Their treatment is based on a Hamiltonian given by Raynes [20]. The purely orbital case with which we are concerned may be treated in the same way; this results in orbit-orbit and orbit-rotation terms. In general, where both effects are present, spin-orbit terms are also present.

Our primary objective here is to develop a theory capable of interpreting the rotation-electronic spectra involving transitions to the Rydberg "L - complex" states. In such a case, the electron involved in the transition jumps to a loosely bound outer orbital, characterized by a specific value of the orbital angular momentum quantum number  $\ell$ . The analogous

atomic situation thus gives rise to a  $(2\ell + 1)$  degenerate electronic state. In the molecular case, however, this degeneracy is removed by the deviation from spherical symmetry of the molecular ion core. The various states within these  $(2\ell + 1)$  states also become mixed as a result of rotation-electronic interaction and consequently, may cause perturbations to the energy level pattern and to the intensity distribution within the rotational branches. Traditional method of reducing spectra may, therefore, need to be supplemented with or replaced by the calculations of the type considered here.

The energy level theory, given in this chapter, is based on a Hamiltonian which includes spin as well as orbital effects and thus also includes the spin theory given by Creutzberg and Hougen [5]. The intensity theory, not previously dealt with, is not as general since it is given here only for a  $\beta$ -complex. Nevertheless, modifications for other cases (including spin) should be reasonably straightforward.

#### 4.2 THE ROTATION-ELECTRONIC HAMILTONIAN

We consider an effective Hamiltonian in the form

$$\hat{H}_{eff} = \hat{H}_{rot} + \hat{H}_{oo} + \hat{H}_{ss} + \hat{H}_{so} + \hat{H}_{sr} + \hat{H}_{or} \quad (88)$$

The complete Hamiltonian also contains a vibronic contribution which we assume to be a purely diagonal contribution,  $E_{vibronic} = E_e + E_{vib}$ , where  $E_e$  is the

purely electronic energy while  $E_{\text{vib}}$  is the simple harmonic oscillator vibrational energy. In (88),  $\hat{H}_{\text{rot}}$  represents the rigid rotor Hamiltonian while  $\hat{H}_{\text{OO}}$ ,  $\hat{H}_{\text{SS}}$ ,  $\hat{H}_{\text{SO}}$ ,  $\hat{H}_{\text{SR}}$  and  $\hat{H}_{\text{OR}}$  represent the orbit-orbit, spin-spin, spin-orbit, spin-rotation and orbit-rotation Hamiltonians, respectively.

We now assume that  $\hat{H}_{\text{eff}}$  may be rewritten as

$$\hat{H}_{\text{eff}} = \sum_i C_i \hat{O}_i \quad (89)$$

where the summation runs over the terms listed in Table 5 (page 70). The coefficients  $C_i$  are the constants corresponding to the operators  $\hat{O}_i$  and are summarized in TABLE 5. It may be mentioned that the subscripts LL, SS, LS, LR, and SR on the various constants  $C_i$  (TABLE 5) refer to the fact that they belong to the orbit-orbit, spin-spin, orbit-spin, orbit-rotation and spin-rotation interaction terms. Note that  $C_i$  are in  $\text{cm}^{-1}$  units and  $\hat{O}_i$  are dimensionless.

From TABLE 5, it is obvious that the total angular momentum  $\vec{J}$ , the orbital angular momentum  $\vec{L}$ , and the spin angular momentum  $\vec{S}$  are each highly non-diagonal. Therefore, we must have a convenient representation of the effective Hamiltonian  $\hat{H}_{\text{eff}}$  in a form that separates out the diagonal and off-diagonal matrix elements. To obtain such a form, we have introduced the raising and lowering operators for  $\hat{J}$ ,  $\hat{L}$  and  $\hat{S}$ . If  $\hat{J}_+$ ,  $\hat{L}_-$  and  $\hat{S}_-$  are the lowering operators and

TABLE 5. THE ANGULAR MOMENTUM OPERATORS  $\hat{O}_i$  AND THE CORRESPONDING COEFFICIENTS  $C_i$ .

Hamiltonian	$C_i$	$\hat{O}_i$
$\hat{H}_{rot}$	$\left\{ \begin{array}{l} (\frac{A+C}{2}) \\ -(\frac{A+C}{2} - B) \\ -(\frac{A-C}{2}) \end{array} \right.$	$\left\{ \begin{array}{l} (\hat{J} - \hat{L} - \hat{S})^2 \\ (\hat{J}_z - \hat{L}_z - \hat{S}_z)^2 \\ [(\hat{J}_x - \hat{L}_x - \hat{S}_x)^2 - (\hat{J}_y - \hat{L}_y - \hat{S}_y)^2] \end{array} \right.$
$\hat{H}_{00}$	$\left\{ \begin{array}{l} \lambda_{LL} \\ \delta_{LL} \end{array} \right.$	$\left\{ \begin{array}{l} (3\hat{L}_z^2 - \hat{L}^2) \\ (\hat{L}_x^2 - \hat{L}_y^2) \end{array} \right.$
$\hat{H}_{ss}$	$\left\{ \begin{array}{l} \lambda_{ss} \\ \delta_{ss} \end{array} \right.$	$\left\{ \begin{array}{l} (3\hat{S}_z^2 - \hat{S}^2) \\ (\hat{S}_x^2 - \hat{S}_y^2) \end{array} \right.$
$\hat{H}_{so}$	$\left\{ \begin{array}{l} \gamma_{LS} \\ \lambda_{LS} \\ \delta_{LS} \end{array} \right.$	$\left\{ \begin{array}{l} (\hat{L} \cdot \hat{S}) \\ (3\hat{L}_z\hat{S}_z - \hat{L} \cdot \hat{S}) \\ (\hat{L}_x\hat{S}_x - \hat{L}_y\hat{S}_y) \end{array} \right.$
$\hat{H}_{OR}$	$\left\{ \begin{array}{l} \gamma_{LR} \\ \lambda_{LR} \\ \delta_{LR} \end{array} \right.$	$\left\{ \begin{array}{l} [(\hat{J} - \hat{L} - \hat{S}) \cdot \hat{L}] \\ [3(\hat{J}_z - \hat{L}_z - \hat{S}_z)\hat{L}_z - (\hat{J} - \hat{L} - \hat{S}) \cdot \hat{L}] \\ [(\hat{J}_x - \hat{L}_x - \hat{S}_x)\hat{L}_x - (\hat{J}_y - \hat{L}_y - \hat{S}_y)\hat{L}_y] \end{array} \right.$
$\hat{H}_{SR}$	$\left\{ \begin{array}{l} \gamma_{SR} \\ \lambda_{SR} \\ \delta_{SR} \end{array} \right.$	$\left\{ \begin{array}{l} [(\hat{J} - \hat{S} - \hat{L}) \cdot \hat{S}] \\ [3(\hat{J}_z - \hat{L}_z - \hat{S}_z)\hat{S}_z - (\hat{J} - \hat{L} - \hat{S}) \cdot \hat{S}] \\ [(\hat{J}_x - \hat{L}_x - \hat{S}_x)\hat{S}_x - (\hat{J}_y - \hat{L}_y - \hat{S}_y)\hat{S}_y] \end{array} \right.$

TABLE 6. OPERATORS AND THEIR CORRESPONDING COEFFICIENTS

Operator $\hat{O}_i$	Coefficient $C_i$
$\hat{J}^2$	$\frac{1}{2}(A+C)$
$\hat{J}_z^2$	$- \left[ \left( \frac{A+C}{2} \right) - B \right]$
$\hat{J}_x^2 - \hat{J}_y^2 = \frac{1}{2} (\hat{J}_+^2 + \hat{J}_-^2)$	$-\frac{1}{2}(A-C)$
$\hat{L}^2$	$\frac{1}{2}(A+C) - \lambda_{LL} - \gamma_{LR} + \lambda_{LR}$
$\hat{L}_z^2$	$- \left[ \frac{1}{2}(A+C) - B \right] + 3\lambda_{LL} - 3\lambda_{LR}$
$\hat{L}_x^2 - \hat{L}_y^2 = \frac{1}{2} (\hat{L}_+^2 + \hat{L}_-^2)$	$-\frac{1}{2}(A-C) + \delta_{LL} - \delta_{LR}$
$\hat{S}^2$	$\frac{1}{2}(A+C) - \lambda_{SS} - \gamma_{SR} + \lambda_{SR}$
$\hat{S}_z^2$	$- \left[ \frac{A+C}{2} - B \right] + 3\lambda_{SS} - 3\lambda_{SR}$
$\hat{S}_x^2 - \hat{S}_y^2 = \frac{1}{2} (\hat{S}_+^2 + \hat{S}_-^2)$	$- \left( \frac{A-C}{2} \right) + \delta_{SS} - \delta_{SR}$
$\hat{J}_z \hat{L}_z$	$-2B + \gamma_{LR} + 2\lambda_{LR}$
$\hat{J}_x \hat{L}_x + \hat{J}_y \hat{L}_y = \frac{1}{2} (\hat{J}_+ \hat{L}_- + \hat{J}_- \hat{L}_+)$	$-(A+C) + \gamma_{LR} - \lambda_{LR}$
$\hat{J}_x \hat{L}_x - \hat{J}_y \hat{L}_y = \frac{1}{2} (\hat{J}_+ \hat{L}_+ - \hat{J}_- \hat{L}_-)$	$(A-C) + \delta_{LR}$
$\hat{J}_z \hat{S}_z$	$-2B + \gamma_{SR} + 2\lambda_{SR}$
$\hat{J}_x \hat{S}_x + \hat{J}_y \hat{S}_y = \frac{1}{2} (\hat{J}_+ \hat{S}_- + \hat{J}_- \hat{S}_+)$	$-(A+C) + \gamma_{SR} - \lambda_{SR}$
$\hat{J}_x \hat{S}_x - \hat{J}_y \hat{S}_y = \frac{1}{2} (\hat{J}_+ \hat{S}_+ - \hat{J}_- \hat{S}_-)$	$(A-C) + \delta_{SR}$
$\hat{L}_z \hat{S}_z$	$2B + \gamma_{LS} - \gamma_{LR} - \gamma_{SR} + 2(\lambda_{LS} - \lambda_{LR} - \lambda_{SR})$
$\hat{L}_x \hat{S}_x + \hat{L}_y \hat{S}_y = \frac{1}{2} (\hat{L}_+ \hat{S}_- + \hat{L}_- \hat{S}_+)$	$(A+C) + \gamma_{LS} - \gamma_{LR} - \gamma_{SR} - (\lambda_{LS} - \lambda_{LR} - \lambda_{SR})$
$\hat{L}_x \hat{S}_x - \hat{L}_y \hat{S}_y = \frac{1}{2} (\hat{L}_+ \hat{S}_+ - \hat{L}_- \hat{S}_-)$	$-(A-C) + \delta_{LS} - \delta_{LR} - \delta_{SR}$

$\hat{J}_-, \hat{L}_+, \hat{S}_+$  are the raising operators defined by

$$\hat{J}_{\pm} = \hat{J}_x \pm i\hat{J}_y \quad ; \quad \hat{L}_{\pm} = \hat{L}_x \pm i\hat{L}_y \quad ; \quad \hat{S}_{\pm} = \hat{S}_x \pm i\hat{S}_y \quad (90)$$

then the resulting operators  $\hat{O}_i$  and their corresponding coefficients  $C_i$  in  $\hat{H}_{\text{eff}}$  take the form shown in TABLE 6. Note that the commutation relations for the components of  $\hat{J}$ , expressed in the molecular frame, involve the anomalous sign of  $i \equiv \sqrt{-1}$ . (See Van Vleck [21]). As a consequence,  $\hat{J}_+$  becomes the lowering rather than the raising operator.

### 4.3 FORM OF FUNCTIONS AND MATRIX ELEMENTS

Using a method similar to Kopp and Hougen [17] we choose wavefunctions of the form

$$|JK; \Lambda \Sigma\rangle \equiv |JK\rangle |L\Lambda\rangle |S\Sigma\rangle \quad (91)$$

appropriate to Hunds case (a) where all the angular momenta are well-defined. Here the basis functions  $|JK; \Lambda \Sigma\rangle$  are simple products of the total angular momentum part  $|JK\rangle$ , an electronic orbital part  $|L\Lambda\rangle$ , an electronic spin part  $|S\Sigma\rangle$  and a vibrational part  $|v\rangle$ , not explicitly shown.  $J, L$  and  $S$  are the quantum numbers associated with the resultant  $\hat{J}$ , resultant  $\hat{L}$  and resultant  $\hat{S}$  operators, respectively. The projections  $K, \Lambda$  and  $\Sigma$  along the  $\hat{J}$ -axis of the molecule-fixed frame are considered as signed quantities.

The phases of  $|JK\rangle$ ,  $|L\Lambda\rangle$  and  $|S\Sigma\rangle$  are chosen so that  $|JK\rangle$  and  $|L\Lambda\rangle$  transform according to (20) and (62) respectively while  $|S\Sigma\rangle$ , having the same transformation properties as  $|JK\rangle$ , follows the following transformations.

$$\hat{C}_{2\hat{J}}|S\Sigma\rangle = (-1)^\Sigma |S\Sigma\rangle \quad (92a)$$

$$\hat{\sigma}_v(x\hat{J})|S\Sigma\rangle = (-1)^{S-\Sigma} |S-\Sigma\rangle \quad (92b)$$

$$\hat{\sigma}_v(y\hat{J})|S\Sigma\rangle = (-1)^S |S-\Sigma\rangle \quad (92c)$$

Then the operators given by (90) and the operators

$\hat{J}^2$ ,  $\hat{J}_z$ ,  $\hat{L}^2$ ,  $\hat{L}_z$ ,  $\hat{S}^2$  and  $\hat{S}_z$  have the following effects on their wavefunctions:

$$\hat{J}_{\pm} |JK\rangle = (\hat{J}_x \pm i\hat{J}_y) |JK\rangle = \sqrt{J(J+1) - K(K \mp 1)} |JK \mp 1\rangle \quad (93a)$$

$$\hat{L}_{\pm} |L\Lambda\rangle = (\hat{L}_x \pm i\hat{L}_y) |L\Lambda\rangle = \sqrt{L(L+1) - \Lambda(\Lambda \pm 1)} |L\Lambda \pm 1\rangle \quad (93b)$$

$$\hat{S}_{\pm} |S\Sigma\rangle = (\hat{S}_x \pm i\hat{S}_y) |S\Sigma\rangle = \sqrt{S(S+1) - \Sigma(\Sigma \pm 1)} |S\Sigma \pm 1\rangle \quad (93c)$$

$$\hat{J}^2 |JK\rangle = J(J+1) |JK\rangle \quad (93d)$$

$$\hat{L}^2 |L\Lambda\rangle = L(L+1) |L\Lambda\rangle \quad (93e)$$

$$\hat{S}^2 |S\Sigma\rangle = S(S+1) |S\Sigma\rangle \quad (93f)$$

$$\hat{J}_z |JK\rangle = K |JK\rangle \quad (93g)$$

$$\hat{L}_z |L\Lambda\rangle = \Lambda |L\Lambda\rangle \quad (93h)$$

$$\hat{S}_z |S\Sigma\rangle = \Sigma |S\Sigma\rangle \quad (93i)$$

The results (93) are used to yield the matrix elements, obtained by using the basis functions  $|JK; \Lambda \Sigma\rangle$ .

The resulting diagonal and off-diagonal matrix elements so obtained are shown in TABLE 7. For the molecular systems with zero resultant spin ( $S = 0$ ), the diagonal and off-diagonal matrix elements become very much simplified; in fact, some of the off-diagonal matrix elements reduce to zero. Then for the zero spin case, since  $\delta_{SS}$ ,  $\delta_{LS}$ ,  $\delta_{SR}$ ,  $\gamma_{LS}$ ,  $\gamma_{SR}$ ,  $\lambda_{SS}$ ,  $\lambda_{LS}$ ,  $\lambda_{SR}$ , all reduce to zero, the energy matrix elements in TABLE 7 reduce to the form shown in TABLE 8. Thus



these results (TABLE 8) can be used directly to calculate the eigenvalues and eigenvectors for singlet states.

#### 4.4 THE EIGENFUNCTIONS AND ASSIGNMENT OF SYMMETRY SPECIES TO ROTATIONAL ENERGY LEVELS

If  $\Psi^\tau$  is to represent the total wavefunction of a rotation-electronic state of energy  $E^\tau$ , then

$$\begin{aligned}\Psi^\tau &= \sum_{K, \Lambda, \Sigma} a_{K, \Lambda, \Sigma}^\tau |JK; \Lambda\Sigma\rangle \\ &= \sum_{K, \Lambda, \Sigma} a_{K, \Lambda, \Sigma}^\tau |JK\rangle |L\Lambda\rangle |S\Sigma\rangle\end{aligned}\quad (94)$$

where  $a_{K, \Lambda, \Sigma}^\tau$  are the eigenvectors of the basis functions  $|JK; \Lambda\Sigma\rangle$ , obtained for an energy level by diagonalizing the energy matrix.

TABLE 7

## ENERGY MATRIX ELEMENTS

$$\langle K', \Lambda', \Sigma' | K, \Lambda, \Sigma \rangle \equiv \langle J K'; \Lambda' \Sigma' | \hat{H}_{eff} | J K; \Lambda \Sigma \rangle$$

DIAGONAL ELEMENTS :

$$\begin{aligned} \langle K, \Lambda, \Sigma | K, \Lambda, \Sigma \rangle = & \frac{1}{2} (A+C) [J(J+1)] + \left[ \frac{A+C}{2} - \lambda_{LL} - \gamma_{LR}' + \lambda_{LR} \right] [L(L+1)] \\ & + \left[ \frac{A+C}{2} - \lambda_{SS} - \gamma_{SR}' + \lambda_{SR} \right] [S(S+1)] \\ & - \left[ \frac{A+C}{2} - B \right] K^2 + \left[ - \left( \frac{A+C}{2} - B \right) + 3\lambda_{LL} - 3\lambda_{LR} \right] \Lambda^2 \\ & + \left[ - \left( \frac{A+C}{2} - B \right) + 3\lambda_{SS} - 3\lambda_{SR} \right] \Sigma^2 \\ & + \left[ -2B + \gamma_{LR}' + 2\lambda_{LR} \right] K\Lambda + \left[ -2B + \gamma_{SR}' + 2\lambda_{SR} \right] K\Sigma \\ & + \left[ 2B + \gamma_{LS}' - \gamma_{LR}' - \gamma_{SR}' + 2(\lambda_{LS} - \lambda_{LR} - \lambda_{SR}) \right] \Lambda\Sigma \end{aligned}$$

OFF-DIAGONAL ELEMENTS :

$$\begin{aligned} \langle K \pm 2, \Lambda, \Sigma | K, \Lambda, \Sigma \rangle &= -\frac{1}{4} (A-C) \langle K \pm 2 | K \pm 1 \rangle \langle K \pm 1 | K \rangle \\ \langle K \pm 1, \Lambda \pm 1, \Sigma | K, \Lambda, \Sigma \rangle &= \frac{1}{2} [ - (A+C) + \gamma_{LR}' - \lambda_{LR} ] \langle K \pm 1 | K \rangle \langle \Lambda \pm 1 | \Lambda \rangle \\ \langle K \pm 1, \Lambda, \Sigma \pm 1 | K, \Lambda, \Sigma \rangle &= \frac{1}{2} [ - (A+C) + \gamma_{SR}' - \lambda_{SR} ] \langle K \pm 1 | K \rangle \langle \Sigma \pm 1 | \Sigma \rangle \\ \langle K \pm 1, \Lambda \mp 1, \Sigma | K, \Lambda, \Sigma \rangle &= \frac{1}{2} [ (A-C) + \delta_{LR} ] \langle K \pm 1 | K \rangle \langle \Lambda \mp 1 | \Lambda \rangle \\ \langle K \pm 1, \Lambda, \Sigma \mp 1 | K, \Lambda, \Sigma \rangle &= \frac{1}{2} [ (A-C) + \delta_{SR} ] \langle K \pm 1 | K \rangle \langle \Sigma \mp 1 | \Sigma \rangle \\ \langle K, \Lambda \pm 2, \Sigma | K, \Lambda, \Sigma \rangle &= \frac{1}{2} \left[ -\frac{1}{2} (A-C) + \delta_{LL} - \delta_{LR} \right] \langle \Lambda \pm 2 | \Lambda \pm 1 \rangle \langle \Lambda \pm 1 | \Lambda \rangle \\ \langle K, \Lambda, \Sigma \pm 2 | K, \Lambda, \Sigma \rangle &= \frac{1}{2} \left[ -\frac{1}{2} (A-C) + \delta_{SS} - \delta_{SR} \right] \langle \Sigma \pm 2 | \Sigma \pm 1 \rangle \langle \Sigma \pm 1 | \Sigma \rangle \\ \langle K, \Lambda \pm 1, \Sigma \pm 1 | K, \Lambda, \Sigma \rangle &= \frac{1}{2} [ - (A-C) + \delta_{LS} - \delta_{LR} - \delta_{SR} ] \langle \Lambda \pm 1 | \Lambda \rangle \langle \Sigma \pm 1 | \Sigma \rangle \\ \langle K, \Lambda \pm 1, \Sigma \mp 1 | K, \Lambda, \Sigma \rangle &= \frac{1}{2} [ (A+C) + \gamma_{LS}' - \gamma_{LR}' - \gamma_{SR}' - (\lambda_{LS} - \lambda_{LR} - \lambda_{SR}) ] \cdot \\ &\quad \cdot \langle \Lambda \pm 1 | \Lambda \rangle \langle \Sigma \mp 1 | \Sigma \rangle \end{aligned}$$

Note that for short-hand notation we have defined the following in TABLE 7.

$$\langle K' | K \rangle \equiv \sqrt{J(J+1) - KK'}$$

$$\langle \Lambda' | \Lambda \rangle \equiv \sqrt{L(L+1) - \Lambda\Lambda'}$$

$$\langle \Sigma' | \Sigma \rangle \equiv \sqrt{S(S+1) - \Sigma\Sigma'}$$

TABLE 8 ENERGY MATRIX ELEMENTS (SPIN = 0)

$$\langle K', \Lambda', \Sigma' | K, \Lambda, \Sigma \rangle \equiv \langle JK'; \Lambda' \Sigma' | \hat{H}_{eff} | JK; \Lambda \Sigma \rangle$$

Diagonal Elements:

$$\begin{aligned} \langle K, \Lambda, \Sigma | K, \Lambda, \Sigma \rangle = & \frac{1}{2} (A+C) [J(J+1)] \\ & + \left[ \frac{A+C}{2} - \lambda_{LL} - \gamma_{LR} + \lambda_{LR} \right] [L(L+1)] \\ & - \left[ \frac{A+C}{2} - B \right] K^2 - \left[ \left( \frac{A+C}{2} - B \right) - 3\lambda_{LL} + 3\lambda_{LR} \right] \Lambda^2 \\ & + \left[ -2B + \gamma_{LR} + 2\lambda_{LR} \right] K\Lambda \end{aligned}$$

Off-Diagonal Elements:

$$\langle K \pm 2, \Lambda, \Sigma | K, \Lambda, \Sigma \rangle = -\frac{1}{4} (A-C) \langle K \pm 2 | K \pm 1 \rangle \langle K \pm 1 | K \rangle$$

$$\langle K \pm 1, \Lambda \pm 1, \Sigma | K, \Lambda, \Sigma \rangle = \frac{1}{2} \left[ -(A+C) + \gamma_{LR} - \lambda_{LR} \right] \langle K \pm 1 | K \rangle \langle \Lambda \pm 1 | \Lambda \rangle$$

$$\langle K \pm 1, \Lambda \mp 1, \Sigma | K, \Lambda, \Sigma \rangle = \frac{1}{2} \left[ (A-C) + \delta_{LR} \right] \langle K \pm 1 | K \rangle \langle \Lambda \mp 1 | \Lambda \rangle$$

$$\langle K, \Lambda \pm 2, \Sigma | K, \Lambda, \Sigma \rangle = \frac{1}{2} \left[ -\frac{1}{2} (A-C) + \delta_{LL} - \delta_{LR} \right] \langle \Lambda \pm 2 | \Lambda \pm 1 \rangle \langle \Lambda \pm 1 | \Lambda \rangle$$

NOTE THAT

$$\langle K' | K \rangle = \sqrt{J(J+1) - KK'}$$

$$\langle \Lambda' | \Lambda \rangle = \sqrt{L(L+1) - \Lambda\Lambda'}$$

$$\langle \Sigma' | \Sigma \rangle = \sqrt{S(S+1) - \Sigma\Sigma'}$$

In view of the transformation properties of  $|JK\rangle$ ,  $|L\Lambda\rangle$  and  $|S\Sigma\rangle$  for the point group  $C_{2v}$ , as is evident from (20a), (62a) and (92a), we find that

$$\hat{C}_{2z} \Psi^\tau = \sum_{K,\Lambda,\Sigma} a_{K,\Lambda,\Sigma}^\tau (-1)^{K+\Omega} |JK; \Lambda\Sigma\rangle \quad (95)$$

where  $\Omega \equiv \Lambda + \Sigma$  is the total electronic projection along the  $z$ -axis of the molecule. (95) shows that under a two-fold rotation of the molecule about the  $z$ -axis,  $\Psi^\tau$  will be invariant if  $K + \Omega$  is even; otherwise the wavefunction will change to  $-\Psi^\tau$ .

That is,

$$\hat{C}_{2z} \Psi^\tau = \Psi^\tau \text{ for EVEN } (K+\Omega)\text{-VALUES} \quad (96a)$$

$$\hat{C}_{2z} \Psi^\tau = -\Psi^\tau \text{ for ODD } (K+\Omega)\text{-VALUES} \quad (96b)$$

which implies (from character table in APPENDIX I) that

$$\text{IF } (K+\Omega) \text{ is EVEN ; } \Psi^\tau \text{ is of species } A_1 \text{ or } A_2 \quad (97a)$$

$$\text{IF } (K+\Omega) \text{ is ODD ; } \Psi^\tau \text{ is of species } B_1 \text{ or } B_2 \quad (97b)$$

In order to further find out the conditions which could establish exactly the symmetry of  $\Psi^\tau$  in (97a) and (97b), we consider another symmetry-element of the point group to which the molecule belongs. We consider the reflection plane  $\hat{\sigma}_v(yz)$ , which is another

element of the point group  $C_{2v}$ . Then from (20b), (62c) and (92c), one finds that

$$\hat{\sigma}_v(yz) |JK; \Lambda\Sigma\rangle = (-1)^{J+S} |J-K\rangle |L-\Lambda\rangle |S-\Sigma\rangle \quad (98)$$

Then,

$$\hat{\sigma}_v(yz) \Psi^\tau = (-1)^{J+S} \sum_{K, \Lambda, \Sigma} a_{K, \Lambda, \Sigma}^\tau |J-K; -\Lambda-\Sigma\rangle \quad (99a)$$

Here we have two possibilities. Either (99a) is  $+\Psi^\tau$  or  $-\Psi^\tau$ . That is,

$$\hat{\sigma}_v(yz) \Psi^\tau = \pm \sum_{K, \Lambda, \Sigma} a_{K, \Lambda, \Sigma}^\tau |JK; \Lambda\Sigma\rangle \equiv \pm \Psi^\tau \quad (99b)$$

In order to satisfy this condition, let us first suppose that

$$a_{K, \Lambda, \Sigma}^\tau = a_{-K, -\Lambda, -\Sigma}^\tau \quad (99c)$$

then (99a) becomes

$$\begin{aligned} \hat{\sigma}_v(yz) \Psi^\tau &= (-1)^{J+S} \sum_{K, \Lambda, \Sigma} a_{-K, -\Lambda, -\Sigma}^\tau |J-K; -\Lambda-\Sigma\rangle \quad (99d) \\ &= (-1)^{J+S} \Psi^\tau \end{aligned}$$

Similarly, if

$$a_{K, \Lambda, \Sigma}^\tau = -a_{-K, \Lambda, -\Sigma}^\tau \quad (99e)$$

then,

$$\hat{\sigma}_v(yz) \Psi^\tau = -(-1)^{J+S} \Psi^\tau \quad (99f)$$

Thus, the results given by (99) lead to the conclusion that

$$\hat{G}_v(\gamma_3)\bar{\Psi}^\tau = \pm (-1)^{J+S}\bar{\Psi}^\tau \quad \text{if} \quad a_{K,\Lambda,\Sigma}^\tau = \pm a_{-K,-\Lambda,-\Sigma}^\tau \quad (99g)$$

Now from (99g) and the character table (APPENDIX I), we find that

$$\hat{G}_v(\gamma_3)\bar{\Psi}^\tau = \begin{cases} +\bar{\Psi}^\tau & \text{refers to species } A_1 \text{ or } B_1 \\ -\bar{\Psi}^\tau & \text{refers to species } A_2 \text{ or } B_1 \end{cases} \quad (99h)$$

Thus, the results (96), (97) and (99g), (99h) establish the criteria for assigning the symmetry species to each rotational energy states. The criteria is summarized in TABLE 9. Note that a complete symmetry of an electronic state is obtained by multiplying the above established symmetry with that of the core. Also, for singlet states ( $S = 0$ ), we can readily get exactly the same criteria by merely replacing  $J + S$  and  $K + \Omega$  in TABLE 9 by  $J$  and  $K + \Lambda$ , respectively. Similarly, the replacements (in TABLE 9) of  $J + S$  by  $J$  and  $K + \Omega$  by  $K$  gives the criteria for purely rotational states. The resulting conditions for the symmetry of rotational states are the same as those already given in TABLE 1 (Chapter 2).

TABLE 9 CRITERIA FOR ASSIGNING THE FULL MOLECULAR  
SPECIES TO THE ROTATION-ELECTRONIC STATES  
FOR THE MOLECULES OF SYMMETRY  $C_{2V}$

$J+S$	$K+\Omega$	$a_{K,\Lambda,\Sigma}^{\tau} = a_{-K,-\Lambda,-\Sigma}^{\tau}$	$a_{K,\Lambda,\Sigma}^{\tau} = -a_{-K,-\Lambda,-\Sigma}^{\tau}$
		Symmetry Species	Symmetry Species
EVEN	EVEN	$A_1$	$A_2$
EVEN	ODD	$B_2$	$B_1$
ODD	EVEN	$A_2$	$A_1$
ODD	ODD	$B_1$	$B_2$

#### 4.5 THE THEORY OF RELATIVE TRANSITION INTENSITIES

In this section, expressions for the line strengths and the corresponding relative intensities are obtained for rotation-electronic dipole transitions. Electric dipole transitions are governed by the matrix elements

$$\langle f | \mu_z | i \rangle \quad (100)$$

where  $|i\rangle$  and  $\langle f|$  are respectively the initial and final rovibronic states between which transitions take place.  $\mu_z$ , having symmetry species  $A_2$ , is the space-fixed Z-component of the dipole moment  $\vec{\mu}$ . In order to be non-zero, the integral (100) must be totally symmetric. Then,

$$\Gamma(f) \times \Gamma(i) = A_2 \quad (101)$$

where  $\Gamma(i)$  and  $\Gamma(f)$  are the irreducible representations of the initial and final states  $|i\rangle$  and  $\langle f|$  respectively.

Let us now write

$$|i\rangle = \psi_{evr}'' = \psi_{ev}'' \psi_r'' \quad (102a)$$

where  $\psi_{ev}''$  is the complete vibronic part and  $\psi_r''$  is the rotational part. The electronic portion of the final state must be separated into a core, which may be included with the vibrational part, and a single electron state which must be combined with the rotational part. That is,

$$|f\rangle \equiv \psi_{evr}' = \psi_{core, v}' \cdot \psi_{er}' \quad (102b)$$



Assuming  $\psi''_{ev}$  and  $\psi'_{ev}$  to be totally symmetric we thus see that (101) may be rewritten as

$$[\Gamma'_{core} \times \Gamma'_{er}] \times \Gamma''_r = A_2 \quad (103)$$

or

$$\Gamma'_{er} \times \Gamma''_r = A_2 \times \Gamma'_{core} \quad (104)$$

Note that  $\Gamma''_r$  and  $\Gamma'_{er}$  represent the initial and final states' "rotational" symmetries given by our previously discussed rules. The complete state symmetries are given by  $\Gamma''_r$  and  $\Gamma'_{core} \times \Gamma'_{er}$  for the initial and final states respectively.

Now with the choice of rotation-electronic wavefunctions given by (94), consistent with our assumption for vibrational states, let  $\psi^{\tau''}$  and  $\psi^{\tau'}$  be the wavefunctions of the initial and final states of energies  $E^{\tau''}$  and  $E^{\tau'}$  respectively, between which transitions are considered, then the dipole transition moments are given by

$$\langle \psi^{\tau'} | \mu_z | \psi^{\tau''} \rangle = \sum_{\substack{\kappa'', \Lambda'', \Sigma'' \\ \kappa', \Lambda', \Sigma'}} a_{\kappa'', \Lambda'', \Sigma''}^{\tau''} a_{\kappa', \Lambda', \Sigma'}^{\tau'} \langle J' \kappa'; \Lambda' \Sigma' | \sum_r f_r \mu_r | J'' \kappa''; \Lambda'' \Sigma'' \rangle \quad (105)$$

where  $\mu_Z$  is the space-fixed  $Z$ -component of dipole moment  $\vec{\mu}$ ;  $f_{-r}$  are appropriate functions of the direction cosines and  $\mu_r$  represents the components of a spherical tensor of rank unity (see (35) in Chapter 2). The expression given by the right hand side of (105) is general in the sense that it includes both the orbital and the electronic spin. Then the line strength  $[S]_{J'}^{J''}$  is given by the spatial average (see Lepard [13]):

$$[S]_{J'}^{J''} = \overline{|\langle \Psi^{\tau'}(J') | \mu_Z | \Psi^{\tau''}(J'') \rangle|^2} = \frac{1}{3} [G]_{J'}^{J''} \quad (106)$$

where

$$[G]_{J'}^{J''} = \left| \sum_{\substack{K'', \Lambda'', \Sigma'' \\ K', \Lambda', \Sigma'}} a_{K'', \Lambda'', \Sigma''}^{\tau''} a_{K', \Lambda', \Sigma'}^{\tau'} \langle J'K'; \Lambda' \Sigma' | \sum_r f_{-r} \mu_r | J''K''; \Lambda'' \Sigma'' \rangle \right|^2 \quad (107)$$

where  $|J''K''; \Lambda'' \Sigma''\rangle$  and  $|J'K'; \Lambda' \Sigma'\rangle$  are the rotation-electronic basis functions for the initial and final states of combination. Then in view of (91) we can write

$$[G]_{J'}^{J''} = \left| \sum_{\substack{K'', \Lambda'', \Sigma'' \\ K', \Lambda', \Sigma', \tau}} a_{K'', \Lambda'', \Sigma''}^{\tau''} a_{K', \Lambda', \Sigma'}^{\tau'} \langle \Lambda' \Sigma' | \mu_r | \Lambda'' \Sigma'' \rangle \langle J'K' | f_{-r} | J''K'' \rangle \right|^2 \quad (108)$$

where  $\Delta J = J' - J'' = 0, \pm 1$  and  $\gamma = \Delta K = K' - K'' = 0, \pm 1$ .

Since  $\vec{\mu}$  is an orbital function, the electronic integral has a value only when  $\Delta S = \Delta \Sigma = 0$ . Then from (108), we may rewrite (106) in the form

$$[S]_{J'}^{J''} = \frac{1}{3} \left| \sum_{\substack{K'', \Lambda'', \Sigma'' \\ K', \Lambda', \Delta K}} a_{K'', \Lambda'', \Sigma''}^{\tau''} a_{K', \Lambda', \Sigma''}^{\tau'} \langle \Lambda' \Sigma'' | \mu_{\Delta K} | \Lambda'' \Sigma'' \rangle \langle J' K' | f_{\Delta K} | J'' K'' \rangle \right|^2 \quad (109)$$

The corresponding expression for the relative intensities for the dipole transitions can be written as

$$[I]_{J'}^{J''} = \nu g_{J''} (2J''+1) e^{-E/T^*} [S]_{J'}^{J''} \quad (110)$$

where

$\nu$  = Frequency of absorption.

$g_{J''}$  = Nuclear statistical weight for the initial state.

$E$  = Energy of the lower state in  $\text{cm}^{-1}$ .

$T^* = T / \left( \frac{hc}{k} \right) = T / (\text{Second Radiation Constant})$

$T$  = Temperature in absolute units ( $^{\circ}\text{K}$ ).

For the transitions involving singlet states only, (109) and (110) reduce to

$$[S]_{J'}^{J''} = \frac{1}{3} \left| \sum_{\substack{K'', \Lambda'' \\ K', \Lambda', \Delta K}} a_{K'', \Lambda''}^{\tau''} a_{K', \Lambda'}^{\tau'} \langle \Lambda' | \mu_{\Delta K} | \Lambda'' \rangle \langle J' K' | f_{\Delta K} | J'' K'' \rangle \right|^2 \quad (111)$$

and

$$[I]_{J'}^{J''} = \nu g_{J''} (2J''+1) e^{-E/T^*} [S]_{J'}^{J''} \quad (112)$$

The non-vanishing rotational matrix elements are given in TABLE 2 (Chapter 2) while the non-vanishing electronic matrix elements are determined by requiring the elements

$$\langle \Lambda' | \mu_{\Delta K} | \Lambda'' \rangle \quad \text{to be totally symmetric.}$$

#### 4.6 RELATIVE INTENSITIES FOR THE SINGLET-SINGLET

##### TRANSITIONS TO $3p$ -COMPLEX

The transitions between the ground state and the excited electronic states corresponding to  $L = 1$  are governed by (111) and (112) where  $\Lambda = 0, \pm 1$ . Since the overall symmetry of the ground electronic state is taken as totally symmetric, then  $|\Lambda''\rangle \equiv |\Lambda_G\rangle = |A_1\rangle$  for the ground rovibronic state.  $|\Lambda_G\rangle$  indicates the ground electronic state. Then (111) reduces to

$$[S]_{J'}^{J''} = \frac{1}{3} \left| \sum_{K'', K', \Delta K} a_{K''}^{\tau''} \langle J'K' | f_{\Delta K} | J''K'' \rangle \left[ a_{K',-1}^{\tau'} \langle -1 | \mu_{\Delta K} | A_1 \rangle + a_{K',0}^{\tau'} \langle 0 | \mu_{\Delta K} | A_1 \rangle + a_{K',1}^{\tau'} \langle 1 | \mu_{\Delta K} | A_1 \rangle \right] \right|^2 \quad (113)$$

The symmetry conditions for non-zero integrals  $\langle \Lambda' | \mu_{\Delta K} | \Lambda \rangle$  are examined below. We must use the complete symmetry of the levels and thus the  $\Gamma'_{er}$  of the upper state must be multiplied by  $\Gamma'_{core}$ .

CASE (I):  $B_1$  MOLECULAR CORE

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We use the symmetry elements  $\hat{\sigma}_v(xz)$  and  $\hat{\sigma}_v(yz)$ . The components of dipole moment transform as follows:

$$\hat{\sigma}_v(xz)\mu_{\pm} = \mu_{\mp} \quad (114a)$$

$$\hat{\sigma}_v(yz)\mu_o = \mu_o \quad (114b)$$

$$\hat{\sigma}_v(xz)\mu_{\pm} = -\mu_{\mp} \quad (115a)$$

$$\hat{\sigma}_v(yz)\mu_o = \mu_o \quad (115b)$$

The upper state (i.e. the excited state) electronic functions, including the  $B_1$  molecular core, transform as

$$\hat{\sigma}_v(xz)|\Lambda\rangle = (-1)^{\Lambda}|- \Lambda\rangle \quad (116)$$

$$\hat{\sigma}_v(yz)|\Lambda\rangle = -|- \Lambda\rangle \quad (117)$$

where, for the sake of brevity, the electronic functions are defined by  $|\Lambda\rangle \equiv |L\Lambda\rangle$ . Then from (114), (115), (116) and (117) one finds that

$$\hat{\sigma}_v(xz)\langle -1|\mu_o|A_1\rangle = -\langle 1|\mu_o|A_1\rangle \quad (118a)$$

$$\hat{\sigma}_v(yz)\langle -1|\mu_o|A_1\rangle = -\langle 1|\mu_o|A_1\rangle \quad (118b)$$

$$\hat{\sigma}_v(xz)\langle 0|\mu_o|A_1\rangle = \langle 0|\mu_o|A_1\rangle \quad (119a)$$

$$\hat{\sigma}_v(yz)\langle 0|\mu_o|A_1\rangle = -\langle 0|\mu_o|A_1\rangle \quad (119b)$$

$$\hat{\sigma}_v(xz)\langle 1|\mu_o|A_1\rangle = -\langle -1|\mu_o|A_1\rangle \quad (120a)$$

$$\hat{\sigma}_v(yz)\langle 1|\mu_o|A_1\rangle = -\langle -1|\mu_o|A_1\rangle \quad (120b)$$

$$\hat{\sigma}_v(xz)\langle -1|\mu_{\pm}|A_1\rangle = -\langle 1|\mu_{\mp}|A_1\rangle \quad (121a)$$

$$\hat{\sigma}_v(yz)\langle -1|\mu_{\pm}|A_1\rangle = \langle 1|\mu_{\mp}|A_1\rangle \quad (121b)$$

$$\hat{\sigma}_v(xz) \langle 0 | \mu_{\pm} | A_1 \rangle = \langle 0 | \mu_{\mp} | A_1 \rangle \quad (122a)$$

$$\hat{\sigma}_v(yz) \langle 0 | \mu_{\pm} | A_1 \rangle = \langle 0 | \mu_{\mp} | A_1 \rangle \quad (122b)$$

$$\hat{\sigma}_v(xz) \langle 1 | \mu_{\pm} | A_1 \rangle = - \langle -1 | \mu_{\mp} | A_1 \rangle \quad (123a)$$

$$\hat{\sigma}_v(yz) \langle 1 | \mu_{\pm} | A_1 \rangle = \langle -1 | \mu_{\mp} | A_1 \rangle \quad (123b)$$

Since the effect of  $\hat{\sigma}_v(xz)$  and  $\hat{\sigma}_v(yz)$  on  $\langle -1 | \mu_0 | A_1 \rangle$  is the same in (118a) and (118b), each of (118a) and (118b) must be equal to the operand  $\langle -1 | \mu_0 | A_1 \rangle$  in order that this matrix element be non-zero. Note that the use of the  $\hat{C}_{2z}$  operator or the identity operator does not add any new information and, therefore, their use will be redundant. Only two of the four molecular point group elements are sufficient here.

We conclude, therefore, that

$$\langle -1 | \mu_0 | A_1 \rangle = - \langle 1 | \mu_0 | A_1 \rangle \neq 0 \quad (124a)$$

(120a) and (120b) together also lead to the same result (124a). Similarly, to be non-vanishing, (119a) and (119b) each must be equal to  $\langle 0 | \mu_0 | A_1 \rangle$ . But here the effect of  $\hat{\sigma}_v(xz)$  and  $\hat{\sigma}_v(yz)$  on  $\langle 0 | \mu_0 | A_1 \rangle$  give opposite signs to the same resulting quantity. This implies that

$$\langle 0 | \mu_0 | A_1 \rangle = 0 \quad (124b)$$

In a similar fashion, for the equations (121a), (121b), (122a), (122b) and (123a), (123b) we conclude

that

$$\langle -1 | \mu_{\pm} | A_1 \rangle = \langle 1 | \mu_{\mp} | A_1 \rangle = 0 \quad (124c)$$

$$\langle 0 | \mu_{+} | A_1 \rangle = \langle 0 | \mu_{-} | A_1 \rangle \neq 0 \quad (124d)$$

where (124c) is obtained independently by the pairs of equations (121a), (121b) and (123a), (123b). Thus we have established that on the basis of symmetry requirements some of the matrix elements do reduce to zero.

Now, our next step is to see if the non-zero matrix elements are real or imaginary. For this purpose a time reversal operator  $\hat{\theta}_t$  is introduced here which, by giving the complex conjugate of the operand, decides whether a quantity (i.e., an operand) is real or imaginary depending upon whether the quantity under consideration remains invariant or changes sign.

We assume a choice of phase so that the lower state and also the upper state core are each represented by real functions. then, from spherical harmonics we see that orbital functions obey

$$\hat{\theta}_t |\Lambda\rangle = (-1)^{\Lambda} |-\Lambda\rangle \quad (125)$$

Therefore, from (125) and (124a), one obtains

$$\hat{\theta}_t \langle -1 | \mu_o | A_1 \rangle = - \langle 1 | \mu_o | A_1 \rangle = \langle -1 | \mu_o | A_1 \rangle \quad (126)$$

which implies that  $\langle -1 | \mu_0 | A_1 \rangle$  is real. That is,

$$\langle -1 | \mu_0 | A_1 \rangle = -\langle 1 | \mu_0 | A_1 \rangle = \text{REAL}. \quad (127)$$

Again from (125) and (124d), one obtains

$$\hat{\theta}_t \langle 0 | \mu_+ | A_1 \rangle = \langle 0 | \mu_- | A_1 \rangle = \langle 0 | \mu_+ | A_1 \rangle \quad (128)$$

which implies that

$$\langle 0 | \mu_+ | A_1 \rangle = \langle 0 | \mu_- | A_1 \rangle = \text{REAL} \quad (129)$$

Thus we summarize our conclusions as follows

$$\left. \begin{aligned} \langle -1 | \mu_0 | A_1 \rangle &= -\langle 1 | \mu_0 | A_1 \rangle = \text{REAL} \neq 0 \\ \langle -1 | \mu_{\pm} | A_1 \rangle &= \langle 1 | \mu_{\mp} | A_1 \rangle = 0 \\ \langle 0 | \mu_0 | A_1 \rangle &= 0 \\ \langle 0 | \mu_+ | A_1 \rangle &= \langle 0 | \mu_- | A_1 \rangle = \text{REAL} \neq 0 \end{aligned} \right\} \quad (130)$$

In view of the results (130), the expression for the line strengths of spectral absorption lines, (113), becomes

$$[S]_{J'}^{J''} = \frac{1}{3} \left| \sum_{K''} a_{K''}^{\tau''} \left\{ a_{K'',-1}^{\tau'} \langle J'K'' | f_0 | J''K'' \rangle \langle -1 | \mu_0 | A_1 \rangle \right. \right. \\ + a_{K'',+1,0}^{\tau'} \langle J'K''+1 | f_{\pm} | J''K'' \rangle \langle 0 | \mu_+ | A_1 \rangle \\ + a_{K'',-1,0}^{\tau'} \langle J'K''-1 | f_{\mp} | J''K'' \rangle \langle 0 | \mu_- | A_1 \rangle \\ \left. \left. + a_{K'',1}^{\tau'} \langle J'K'' | f_0 | J''K'' \rangle \langle 1 | \mu_0 | A_1 \rangle \right\} \right|^2 \quad (131)$$



Now (131) can be reduced further so that one can determine the components of  $\vec{\mu}$ , in the molecule-fixed frame, which are active in each matrix element. Consequently, the selection rules for transitions can be set forth in terms of the symmetry species of electronic energy states.

It is useful to note that the electronic integrals in (131) may be expressed in terms of purely electronic states  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$  defined by (58). These relations may be combined with those given for  $\mu_{\pm}$  and  $\mu_0$  by (34) to yield

$$\langle 0 | \mu_0 | A_1 \rangle = \langle z | \mu_z | A_1 \rangle \quad (132a)$$

$$\langle 0 | \mu_{\pm} | A_1 \rangle = \frac{1}{\sqrt{2}} \langle z | \mu_x | A_1 \rangle \pm \frac{i}{\sqrt{2}} \langle z | \mu_y | A_1 \rangle \quad (132b)$$

$$\langle \pm 1 | \mu_0 | A_1 \rangle = \frac{1}{\sqrt{2}} \langle y | \mu_z | A_1 \rangle \pm \frac{1}{\sqrt{2}} \langle x | \mu_z | A_1 \rangle \quad (132c)$$

$$\begin{aligned} \langle 1 | \mu_{\pm} | A_1 \rangle &= \frac{1}{2} \langle y | \mu_x | A_1 \rangle + \frac{1}{2} \langle x | \mu_x | A_1 \rangle \\ &\quad \pm \frac{i}{2} \langle y | \mu_y | A_1 \rangle \pm \frac{i}{2} \langle x | \mu_y | A_1 \rangle \end{aligned} \quad (132d)$$

$$\begin{aligned} \langle -1 | \mu_{\pm} | A_1 \rangle &= \frac{1}{2} \langle y | \mu_x | A_1 \rangle - \frac{1}{2} \langle x | \mu_x | A_1 \rangle \\ &\quad \pm \frac{i}{2} \langle y | \mu_y | A_1 \rangle \mp \frac{i}{2} \langle x | \mu_y | A_1 \rangle \end{aligned} \quad (132e)$$

The states  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$  are of symmetry species  $A_1$ ,  $A_2$  and  $B_1$  respectively, for a core of symmetry

species  $B_1$ . Since  $\mu_x$ ,  $\mu_y$ ,  $\mu_z$  are of symmetry  $B_1$ ,  $B_2$ ,  $A_1$ , respectively, the right hand side of the above equations reduces to one non-zero totally symmetric term. These may be written, using (130), as follows:

$$\langle 0 | \mu_{\pm} | A_1 \rangle = \frac{1}{\sqrt{2}} \langle \mp | \mu_x | A_1 \rangle \equiv \frac{1}{\sqrt{2}} \langle \mu_x \rangle \quad (133a)$$

$$\pm \langle \pm 1 | \mu_0 | A_1 \rangle = \frac{1}{\sqrt{2}} \langle \mp | \mu_z | A_1 \rangle \equiv \frac{1}{\sqrt{2}} \langle \mu_z \rangle \quad (133b)$$

where  $\langle \mu_x \rangle$  and  $\langle \mu_z \rangle$  are real.

Then by making use of the results (133) in (131), we obtain

$$[S]_{J'}^{J''} = \frac{1}{6} \left| \sum_{K''} a_{K''}^{\tau''} \left[ \left( a_{K''-1,0}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle + a_{K''+1,0}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle \right) \langle \mu_x \rangle \right. \right. \\ \left. \left. + (a_{K'',1}^{\tau'} - a_{K'',-1}^{\tau'}) \langle J'K'' | f_0 | J''K'' \rangle \langle \mu_z \rangle \right] \right|^2 \quad (134)$$

Note that the existence of  $\langle \mu_x \rangle$  and  $\langle \mu_z \rangle$  implies, ignoring rotation, purely electronic transitions to states  $\tilde{D}^1A_1$  and  $\tilde{C}^1B_1$ . However, unlike the previous treatment (Chapter 2), both  $\langle \mu_x \rangle$  and  $\langle \mu_z \rangle$  participate in the transition to each state, as is evident from (134).

In order to investigate the effect of both moments participating in a given transition, we shall consider the following limiting cases:

<u>CASE</u>	<u><math>\langle \mu_z \rangle</math></u>	<u><math>\langle \mu_x \rangle</math></u>
(a)	1	0
(b)	0	1
(c)	1	1
(d)	1	-1

The actual case, to be determined by examination of the experimental spectra, should lie within the above cases. Then for the case (a), only  $\mu_z$  terms will be non-zero while for the case (b),  $\mu_x$  terms will be non-zero. In cases (c) and (d), both the terms will exist in (134) and, therefore, there will be a mixture of transitions involving  $\mu_x$  and  $\mu_z$  both. Thus for:

CASE I (a):

$$[S]_{J'}^{J''} = \frac{1}{6} \left| \sum_{K''} a_{K''}^{\tau''} (a_{K'',1}^{\tau'} - a_{K'',-1}^{\tau'}) \langle J'K'' | f_0 | J''K'' \rangle \right|^2 \quad (135a)$$

CASE I (b):

$$[S]_{J'}^{J''} = \frac{1}{6} \left| \sum_{K''} a_{K''}^{\tau''} (a_{K''-1,0}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle + a_{K''+1,0}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle) \right|^2 \quad (135b)$$

CASE I (c):

$$[S]_{J'}^{J''} = \frac{1}{6} \left| \sum_{K''} a_{K''}^{\tau''} \left[ (a_{K''-1,0}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle + a_{K''+1,0}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle) + (a_{K'',1}^{\tau'} - a_{K'',-1}^{\tau'}) \langle J'K'' | f_0 | J''K'' \rangle \right] \right|^2 \quad (135c)$$

CASE I (d):

$$[S]_{J'}^{J''} = \frac{1}{6} \left| \sum_{K''} a_{K''}^{\tau''} \left[ - (a_{K''-1,0}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle + a_{K''+1,0}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle) + (a_{K'',1}^{\tau'} - a_{K'',-1}^{\tau'}) \langle J'K'' | f_0 | J''K'' \rangle \right] \right|^2 \quad (135d)$$

# CASE (II): $B_2$ MOLECULAR CORE

In the case where a molecular core symmetry  $B_2$  is involved, we adopt exactly a similar procedure as for the molecular core  $B_1$  (CASE (1)). However, since the ground state is assumed to have the symmetry  $A_1$  as before, the transformations of  $|\Lambda\rangle$ , with the molecular core  $B_2$  included, will be

$$\hat{G}_v(xz)|\Lambda\rangle = -(-1)^\Lambda |-\Lambda\rangle \quad (136a)$$

$$\hat{G}_v(yz)|\Lambda\rangle = |-\Lambda\rangle \quad (136b)$$

which, together with the use of time reversal operator  $\hat{\theta}_t$ , give the results

$$\left. \begin{aligned} \langle -1 | \mu_0 | A_1 \rangle &= \langle 1 | \mu_0 | A_1 \rangle = \text{IMAGINARY} \neq 0 \\ \langle 0 | \mu_0 | A_1 \rangle &= 0 \\ \langle -1 | \mu_{\pm} | A_1 \rangle &= \langle 1 | \mu_{\mp} | A_1 \rangle = 0 \\ \langle 0 | \mu_{+} | A_1 \rangle &= -\langle 0 | \mu_{-} | A_1 \rangle = \text{IMAGINARY} \neq 0 \end{aligned} \right\} \quad (137)$$

The symmetry species of the electronic states  $|\chi\rangle$ ,  $|\psi\rangle$  and  $|\zeta\rangle$ , with the molecular core  $B_2$  included, become  $A_2$ ,  $A_1$  and  $B_2$ , respectively. The (137) may be written, when reducing (132) as before, as follows:

$$\pm \langle 0 | \mu_{\pm} | A_1 \rangle = \frac{i}{\sqrt{2}} \langle \zeta | \mu_{\psi} | A_1 \rangle \equiv \frac{1}{\sqrt{2}} \langle \mu_{\psi} \rangle \quad (138a)$$

$$\langle \pm 1 | \mu_0 | A_1 \rangle = \frac{1}{\sqrt{2}} \langle \psi | \mu_{\zeta} | A_1 \rangle \equiv \frac{1}{\sqrt{2}} \langle \mu_{\zeta} \rangle \quad (138b)$$

where  $\langle \mu_y \rangle$  and  $\langle \mu_z \rangle$  are purely imaginary. Then, the expression for the line strength, from (113), (137) and (138) becomes

$$[S]_{J'}^{J''} = \frac{1}{6} \left| \sum_{K''} a_{K''}^{\tau''} \left[ (a_{K''+1,0}^{\tau'} \langle J'K''+1 | f_- | J''K'' \rangle - a_{K''-1,0}^{\tau'} \langle J'K''-1 | f_+ | J''K'' \rangle) \langle \mu_y \rangle + (a_{K'',-1}^{\tau'} + a_{K'',1}^{\tau'}) \langle J'K'' | f_0 | J''K'' \rangle \langle \mu_z \rangle \right] \right|^2 \quad (139)$$

Since both  $\langle \mu_y \rangle$  and  $\langle \mu_z \rangle$  are imaginary, we may simply use, instead, real numbers in the formula (139).

#### CASE (III): $A_1$ MOLECULAR CORE

In this case, with the core  $A_1$  included, we have

$$\hat{G}_V(xz) | \Lambda \rangle = (-1)^\Lambda | -\Lambda \rangle \quad (140a)$$

$$\hat{G}_V(yz) | \Lambda \rangle = | -\Lambda \rangle \quad (140b)$$

which when used in combination with the time reversal operator  $\hat{\Theta}_t$  on the purely electronic matrix elements give the results

$$\left. \begin{aligned} \langle -1 | \mu_0 | A_1 \rangle &= \langle 1 | \mu_0 | A_1 \rangle = 0 \\ \langle 0 | \mu_0 | A_1 \rangle &= \text{REAL} \neq 0 \\ \langle -1 | \mu_{\pm} | A_1 \rangle &= -\langle 1 | \mu_{\mp} | A_1 \rangle = \text{REAL} \neq 0 \\ \langle 0 | \mu_{+} | A_1 \rangle &= \langle 0 | \mu_{-} | A_1 \rangle = 0 \end{aligned} \right\} \quad (141)$$

The symmetry species of the electronic states  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$ , with the molecular core symmetry  $A_1$  included, are  $B_1$ ,  $B_2$  and  $A_1$ , respectively. Then (141) may be written, when reducing (132) as before, as follows:

$$\langle 0 | \mu_0 | A_1 \rangle = \langle z | \mu_z | A_1 \rangle \equiv \langle \mu_z \rangle \quad (142a)$$

$$\begin{aligned} \langle 1 | \mu_{\pm} | A_1 \rangle &= - \langle -1 | \mu_{\mp} | A_1 \rangle \\ &= \frac{1}{2} \langle x | \mu_x | A_1 \rangle \pm \frac{i}{2} \langle y | \mu_y | A_1 \rangle \\ &= \frac{1}{2} \langle \mu_x \rangle \pm \frac{1}{2} \langle \mu_y \rangle \end{aligned} \quad (142b)$$

where  $\langle \mu_x \rangle = \langle x | \mu_x | A_1 \rangle$  and  $\langle \mu_y \rangle = i \langle y | \mu_y | A_1 \rangle$  are purely real. Then, the expression for the line strength, from (113), (141) and (142) becomes

$$\begin{aligned} [S]_{J'}^{J''} &= \frac{1}{3} \left| \sum_{K''} a_{K''}^{\tau''} \left[ \{ (a_{K''-1,1}^{\tau'} - a_{K''-1,-1}^{\tau'}) \langle J'K''-1 | f_+ | J''K'' \rangle \right. \right. \\ &\quad \left. \left. + (a_{K''+1,1}^{\tau'} - a_{K''+1,-1}^{\tau'}) \langle J'K''+1 | f_- | J''K'' \rangle \right\} \frac{\langle \mu_x \rangle}{2} \right. \\ &\quad \left. + \{ - (a_{K''-1,1}^{\tau'} + a_{K''-1,-1}^{\tau'}) \langle J'K''-1 | f_+ | J''K'' \rangle \right. \\ &\quad \left. + (a_{K''+1,1}^{\tau'} + a_{K''+1,-1}^{\tau'}) \langle J'K''+1 | f_- | J''K'' \rangle \right\} \frac{\langle \mu_y \rangle}{2} \\ &\quad \left. + \{ a_{K'',0}^{\tau'} \langle J'K'' | f_0 | J''K'' \rangle \} \langle \mu_z \rangle \right] \Big|^2 \quad (143) \end{aligned}$$

Here we note that  $\langle \mu_x \rangle$ ,  $\langle \mu_y \rangle$  and  $\langle \mu_z \rangle$  are all real quantities. Also we note that all the components of participate in the transition for a totally symmetric molecular core.

CASE (IV):  $A_2$  MOLECULAR CORE:

Here, with the core  $A_2$  included, we have

$$\hat{S}_v(xz)|\Lambda\rangle = -(-1)^\Lambda |-\Lambda\rangle \quad (144a)$$

$$\hat{S}_v(yz)|\Lambda\rangle = -|-\Lambda\rangle \quad (144b)$$

which, on using the time reversal operator  $\hat{\theta}_t$ , give the results

$$\left. \begin{aligned} \langle -1 | \mu_0 | A_1 \rangle &= \langle 1 | \mu_0 | A_1 \rangle = 0 \\ \langle 0 | \mu_0 | A_1 \rangle &= 0 \\ \langle -1 | \mu_{\pm} | A_1 \rangle &= \langle 1 | \mu_{\mp} | A_1 \rangle = \text{IMAGINARY} \neq 0 \\ \langle 0 | \mu_{+} | A_1 \rangle &= \langle 0 | \mu_{-} | A_1 \rangle = 0 \end{aligned} \right\} \quad (145)$$

We find that the symmetry species of the electronic states  $|x\rangle$ ,  $|y\rangle$  and  $|z\rangle$ , with the molecular core  $A_2$  included, are  $B_2$ ,  $B_1$  and  $A_2$ , respectively. Then (145) may be written, when reducing (132) as before, as follows:

$$\begin{aligned} \langle 1 | \mu_{\pm} | A_1 \rangle &= \langle -1 | \mu_{\mp} | A_1 \rangle \\ &= \frac{1}{2} \langle y | \mu_x | A_1 \rangle \pm \frac{i}{2} \langle x | \mu_y | A_1 \rangle \\ &= \frac{1}{2} \langle \mu_x \rangle \pm \frac{1}{2} \langle \mu_y \rangle \end{aligned} \quad (146)$$

where  $\langle \mu_x \rangle = \langle y | \mu_x | A_1 \rangle$  and  $\langle \mu_y \rangle = i \langle x | \mu_y | A_1 \rangle$  are purely imaginary. Then, from (113), (145) and (146), the expression for the line strength becomes

$$\begin{aligned}
[S]_{J'}^{J''} = \frac{1}{12} \left| \sum_{K''} a_{K''}^{\tau''} \left[ \{ (a_{K''-1,-1}^{\tau'} + a_{K''-1,1}^{\tau'}) \langle J'K''-1 | f_+ | J''K'' \rangle \right. \right. \\
+ (a_{K''+1,-1}^{\tau'} + a_{K''+1,1}^{\tau'}) \langle J'K''+1 | f_- | J''K'' \rangle \} \langle \mu_x \rangle \\
+ \{ (a_{K''-1,-1}^{\tau'} - a_{K''-1,1}^{\tau'}) \langle J'K''-1 | f_+ | J''K'' \rangle \\
\left. \left. - (a_{K''+1,-1}^{\tau'} - a_{K''+1,1}^{\tau'}) \langle J'K''+1 | f_- | J''K'' \rangle \} \langle \mu_y \rangle \right] \right|^2
\end{aligned}
\tag{147}$$

Thus, we see that both the moments  $\langle \mu_x \rangle$  and  $\langle \mu_y \rangle$  participate in the transition when the molecular core  $A_2$  is involved. Also both  $\langle \mu_x \rangle$  and  $\langle \mu_y \rangle$  involved in the transitions in (147) are imaginary. However, we may simply use, instead, real numbers in the formula because the absolute value of the entire sum is involved.

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## 5. "3p-COMPLEX" CALCULATIONS FOR THE $\tilde{C}^1B_1$ AND $\tilde{D}^1A_1$ BANDS OF WATER

### 5.1 THE ROTATIONAL CONSTANTS

The rotation -electronic interaction theory, presented in Chapter 4, includes the various interaction terms explicitly. This requires the use of numerical values for the "deperturbed ( $\ell$ -uncoupled) rotational constants" in the expressions for the energy matrix elements given in TABLES 7 and 8 for the general spin case and the singlet spin case respectively. For a p-complex,  $\ell=1$ , the electronic interaction constants  $\lambda_{LL}$  and  $\delta_{LL}$  must also be specified. We shall ignore the other interaction constants. Those interaction constants which involve spin are not in any case defined for the singlet case in which we are interested. Values for the orbit-rotation constants  $\lambda_{LR}$ ,  $\delta_{LR}$  and  $\gamma_{LR}$  are not available. Values could, of course, be obtained by a non-linear least squares fit to the frequencies of the transitions in the spectra.

### 5.2 CALCULATIONS OF INTERACTION CONSTANTS

From Eq (7) of Raynes [20] we write the orbit-orbit effects as

$$\begin{aligned} & \lambda_{LL} (3\hat{L}_z^2 - \hat{L}^2) + \delta_{LL} (\hat{L}_x^2 - \hat{L}_y^2) + \mathcal{E} \\ &= \mathcal{E} - (\lambda_{LL} - \delta_{LL})\hat{L}_x^2 - (\lambda_{LL} + \delta_{LL})\hat{L}_y^2 + 2\lambda_{LL}\hat{L}_z^2 \end{aligned} \quad (148)$$

where we have replaced  $\alpha$  and  $\beta$  by  $\lambda_{LL}$  and  $\delta_{LL}$  respectively and have also included a purely electronic energy  $\mathcal{E}$ .

Creutzberg and Hougen [5] have given an equivalent formulation for the triplet case. This, when written for our

case of  $L = 1$  rather than  $S = 1$ , is given by

$$\begin{aligned} & \mathcal{E}_x (1 - \hat{L}_x^2) + \mathcal{E}_y (1 - \hat{L}_y^2) + \mathcal{E}_z (1 - \hat{L}_z^2) \\ &= \mathcal{E}_x + \mathcal{E}_y + \mathcal{E}_z - \mathcal{E}_x \hat{L}_x^2 - \mathcal{E}_y \hat{L}_y^2 - \mathcal{E}_z \hat{L}_z^2 \end{aligned} \quad (149)$$

On comparing (148) and (149), we find that

$$\mathcal{E} = \mathcal{E}_x + \mathcal{E}_y + \mathcal{E}_z \quad (150a)$$

$$\mathcal{E}_x = \lambda_{LL} - \delta_{LL} \quad (150b)$$

$$\mathcal{E}_y = \lambda_{LL} + \delta_{LL} \quad (150c)$$

$$\mathcal{E}_z = -2\lambda_{LL} \quad (150d)$$

Then from (150), we find that

$$\mathcal{E} = \mathcal{E}_x + \mathcal{E}_y + \mathcal{E}_z = 0 \quad (151a)$$

$$\lambda_{LL} = \frac{1}{2}(\mathcal{E}_x + \mathcal{E}_y) = -\frac{1}{2}\mathcal{E}_z \quad (151b)$$

$$\delta_{LL} = -\frac{1}{2}(\mathcal{E}_x - \mathcal{E}_y) \quad (151c)$$

A redundancy condition such as that given above in (151a) is of course expected since only two parameters, such as  $\lambda_{LL}$  and  $\delta_{LL}$ , are required to describe the interaction. This redundancy condition permits us to rewrite (151b) and (151c) in terms of electronic energy differences that are experimentally known values. Hence we find that

$$\lambda_{LL} = \frac{\mathcal{E}_x + \mathcal{E}_y + \mathcal{E}_z - 3\mathcal{E}_z}{6} = \frac{\mathcal{E}_x + \mathcal{E}_y - 2\mathcal{E}_z}{6} \quad (152a)$$

$$\delta_{LL} = \frac{1}{2}(\mathcal{E}_y - \mathcal{E}_x) \quad (152b)$$

Bell [1] and Johns [11] have given the values of the effective electronic energy differences between the  $\tilde{D}^1A_1$ , and  $\tilde{C}^1B_1$  electronic states and between the  $\tilde{D}^1A_1$  and  $^1A_2$  electronic states for both  $H_2O$  and  $D_2O$  ( (85a) and (85b) in Chapter 3). Then from (73) one obtains the purely electronic energy differences as follows:

$$\mathcal{E}_x - \mathcal{E}_z = (\mathcal{E}_{\text{eff } x} - \mathcal{E}_{\text{eff } z}) + (B - C) \quad (153a)$$

$$\mathcal{E}_y - \mathcal{E}_z = (\mathcal{E}_{\text{eff } y} - \mathcal{E}_{\text{eff } z}) + (B - A) \quad (153b)$$

The expressions (153), on using (85a), (85b) and the numerical values of the deperturbed rotational constants A, B, C (which are represented by A', B', C' in TABLE 4), give the purely electronic energy differences for H<sub>2</sub>O and D<sub>2</sub>O as follows:

FOR H<sub>2</sub>O:

$$\left. \begin{aligned} \mathcal{E}_x - \mathcal{E}_z &= 1438.17 \quad \text{cm}^{-1} \\ \mathcal{E}_y - \mathcal{E}_z &= -3602.46 \quad \text{cm}^{-1} \\ \mathcal{E}_y - \mathcal{E}_x &= -5040.63 \quad \text{cm}^{-1} \end{aligned} \right\} \quad (154a)$$

FOR D<sub>2</sub>O

$$\left. \begin{aligned} \mathcal{E}_x - \mathcal{E}_z &= 1324.93 \quad \text{cm}^{-1} \\ \mathcal{E}_y - \mathcal{E}_z &= -2207.04 \quad \text{cm}^{-1} \\ \mathcal{E}_y - \mathcal{E}_x &= -3531.97 \quad \text{cm}^{-1} \end{aligned} \right\} \quad (154b)$$

Substitution of the results (154a) in (152) gives the orbit-orbit interaction constants  $\lambda_{\text{LL}}$  and  $\delta_{\text{LL}}$  for H<sub>2</sub>O. Similarly, the values of  $\lambda_{\text{LL}}$  and  $\delta_{\text{LL}}$  for D<sub>2</sub>O are obtained by using (154b) in (152). The results are summarized in TABLE 10.

### 5.3 COMPUTATIONAL DETAILS OF ENERGIES

It has been found convenient to centre the energy levels about the quantum numbers J=0, K=0 and  $\Lambda=0$ . If we add the three diagonal elements corresponding to  $\Lambda=0, \pm 1$  for J=0 and K=0 then, the average (i.e., one-third) of such a sum is

$$\left[ \frac{2}{3} (A + B + C) - 2 \gamma_{\text{LR}} \right] \quad (155)$$

This can be verified from the expression for the diagonal matrix elements given in TABLE 8. Thus, on adding  $-\left[\frac{2}{3}(A+B+C) - 2\gamma_{LR}\right]$  to the right hand side of the expression for the diagonal matrix elements in TABLE 8, we find that the result for  $L = 1$  is

$$\begin{aligned} & \langle JK; \Lambda \Sigma | \hat{H}_{eff} | JK; \Lambda \Sigma \rangle \\ &= \frac{1}{2} [A+C] [J(J+1)] - \left[ \frac{A+C}{2} - B \right] K^2 - \left[ \left( \frac{A+C}{2} - B \right) - 3\lambda_{LL} + 3\lambda_{LR} \right] \Lambda^2 \\ &+ [-2B + \gamma_{LR} + 2\lambda_{LR}] K\Lambda + \frac{2}{3} \left[ \frac{A+C}{2} - B \right] - 2\lambda_{LL} + 2\lambda_{LR} \quad (156) \end{aligned}$$

Thus (156), when used as the diagonal matrix elements, centres the energy levels about  $J = 0$  and  $K = 0$ .

In order to calculate the rotation-electronic energies for the three electronic states  $\tilde{C}^1B_1$ ,  $\tilde{D}^1A_1$  and  $^1A_2$  of the 3p-complex of Rydberg, the values of the interaction constants  $\lambda_{LR}$  &  $\gamma_{LR}$  are set to zero because they are not available as yet. A computer programme has been developed which by using the diagonal matrix elements (156) and the off-diagonal elements given in TABLE 8, diagonalizes the matrix to give eigenvalues and eigenvectors for the rotational bands in the three electronic states  $\tilde{C}^1B_1$ ,  $\tilde{D}^1A_1$  and  $^1A_2$ . It is to be noted that because of the presence of three bands, the matrix size for a total quantum number  $J$  will be  $3[(2J+1) \times (2J+1)]$ . The results are obtained for both  $H_2O$  and  $D_2O$ . True values of the rotational energies in the various electronic states are obtained by adding the appropriate band origins (TABLE 10). Since we have found that the transitions to  $^1A_2$  level are very weak compared to those of  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$ , the rotational energies for  $^1A_2$  electronic state are not listed. The energies of rotation-electronic

states for  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  bands for  $H_2O$  as well as  $D_2O$  are listed in Tables IV.1 and IV.2 in APPENDIX IV.

TABLE 10

BAND ORIGINS AND INTERACTION CONSTANTS FOR  $H_2O$  AND  $D_2O$

	$H_2O$	$D_2O$
Band Origin	79907.0 $cm^{-1}$	80460.2 $cm^{-1}$
$\lambda_{LL}$	-356.95167 $cm^{-1}$	-144.64833 $cm^{-1}$
$\delta_{LL}$	-2500.685 $cm^{-1}$	-1755.015 $cm^{-1}$

#### 5.4 COMPUTATIONAL DETAILS OF RELATIVE INTENSITIES OF ELECTRIC DIPOLE TRANSITIONS

Computer programmes for the Burroughs B6700 System have been developed to compute the relative intensities of electric dipole transitions from the ground rotation-electronic states  $\tilde{X}^1A_1$  to the p-complex Rydberg states in  $H_2O$  and  $D_2O$  molecules. That is, transitions from the  $\tilde{X}^1A_1$  band to all the three rotational bands in  $\tilde{C}^1B_1$ ,  $\tilde{D}^1A_1$  and  $^1A_2$  electronic states are considered. The molecular core of  $H_2O$  as well as that of  $D_2O$  is of symmetry  $B_1$  in both the ground and the excited states. Therefore, the expression (134) for the line strengths and hence the relations (135) for the various ratios of dipole components  $\langle \mu_x \rangle$  and  $\langle \mu_z \rangle$  are used to calculate the corresponding relative intensities. The numerical values of the eigenvalues and the corresponding eigenvectors used here have been calculated and stored in the initial stage of this programme for both the ground

state  $\tilde{X}^1A_1$  and the p-complex Rydberg states. The numerical values of  $\lambda_{LL}$  and  $\delta_{LL}$  for the final states of  $H_2O$  and  $D_2O$  used in these calculations are given in TABLE 10, while the values of both the deperturbed rotational constants and the rotational constants in the ground rotation-electronic states  $\tilde{X}^1A_1$  are given in TABLE 4 (Chapter 3).

The selection rules are brought into effect by first assigning and storing the symmetry species to the initial and final states, consistent with the criteria given in TABLE 1 (Chapter 2) and TABLE 9 (Chapter 4) respectively, in the form of symmetry codes, established by calling two separate subroutines. It is to be pointed out that the codes for the final states have been assigned such that the molecular species  $B_1$  are included. A third subroutine then changes the already stored symmetry codes of rotational states in the p-complex Rydberg states to those of the initial states for which transitions are allowed as determined by the selection rules (103). The nuclear statistical weights to the energy levels are attached as described in SECTION 3.4 (Chapter 3).

The results so obtained for line positions in  $H_2O$  and  $D_2O$  are listed in TABLES IV.1 and IV.2 respectively. Also, the corresponding relative intensities for  $\tilde{C}^1B_1$ ,  $\tilde{D}^1A_1$  bands for the various ratios of electronic dipole moment components are given in TABLES V.1, V.2 for  $H_2O$  and in TABLES V.3 and V.4 for  $D_2O$ . The relative intensities  $[I]_J^{J''} \times 10 < 0.5$  are not listed. The relative intensities of dipole transitions

to the  $^1A_2$  electronic state are extremely weak (from  $10^{-3}$  to  $10^{-8}$ ) and therefore not listed.

In order to give an overall picture of the rotational line positions and relative intensities in  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  bands of  $H_2O$ , graphical plots of the spectra are carried out in the form of theoretical stick spectra for all the three cases of dipole components' ratios for the  $\tilde{C}^1B_1$  band. However, for  $\tilde{D}^1A_1$  band, stick spectrum for only one case, viz.,  $\langle \mu_z \rangle : \langle \mu_x \rangle = 1 : 0$ , is plotted because the other cases do not differ appreciably in the values of their relative intensities. This is evident from TABLE V.2. Similarly, for  $D_2O$ , the relative intensities and line positions listed in TABLES V.3 and V.4 can be used to draw the theoretical stick spectra, not shown in this thesis.

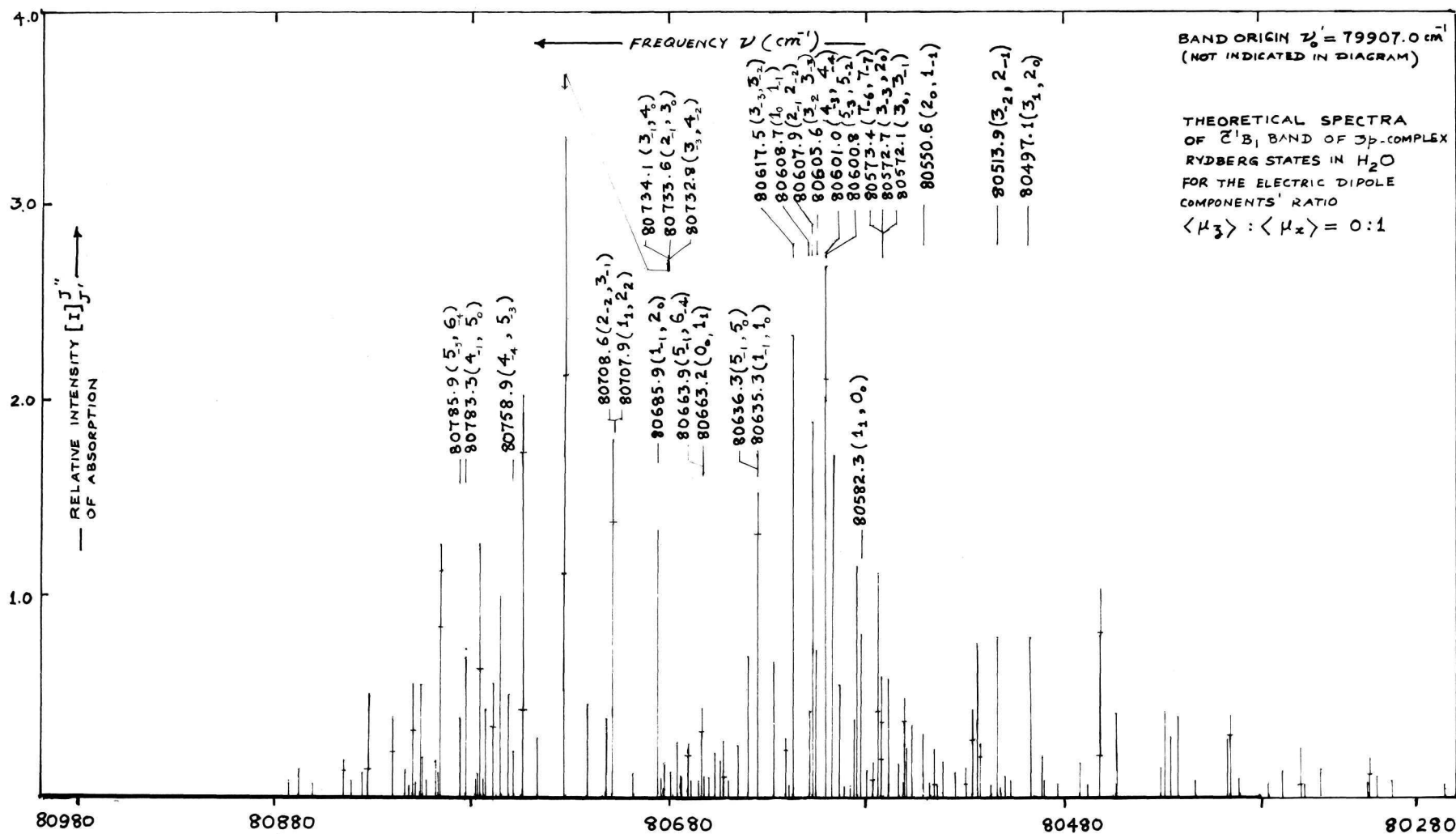
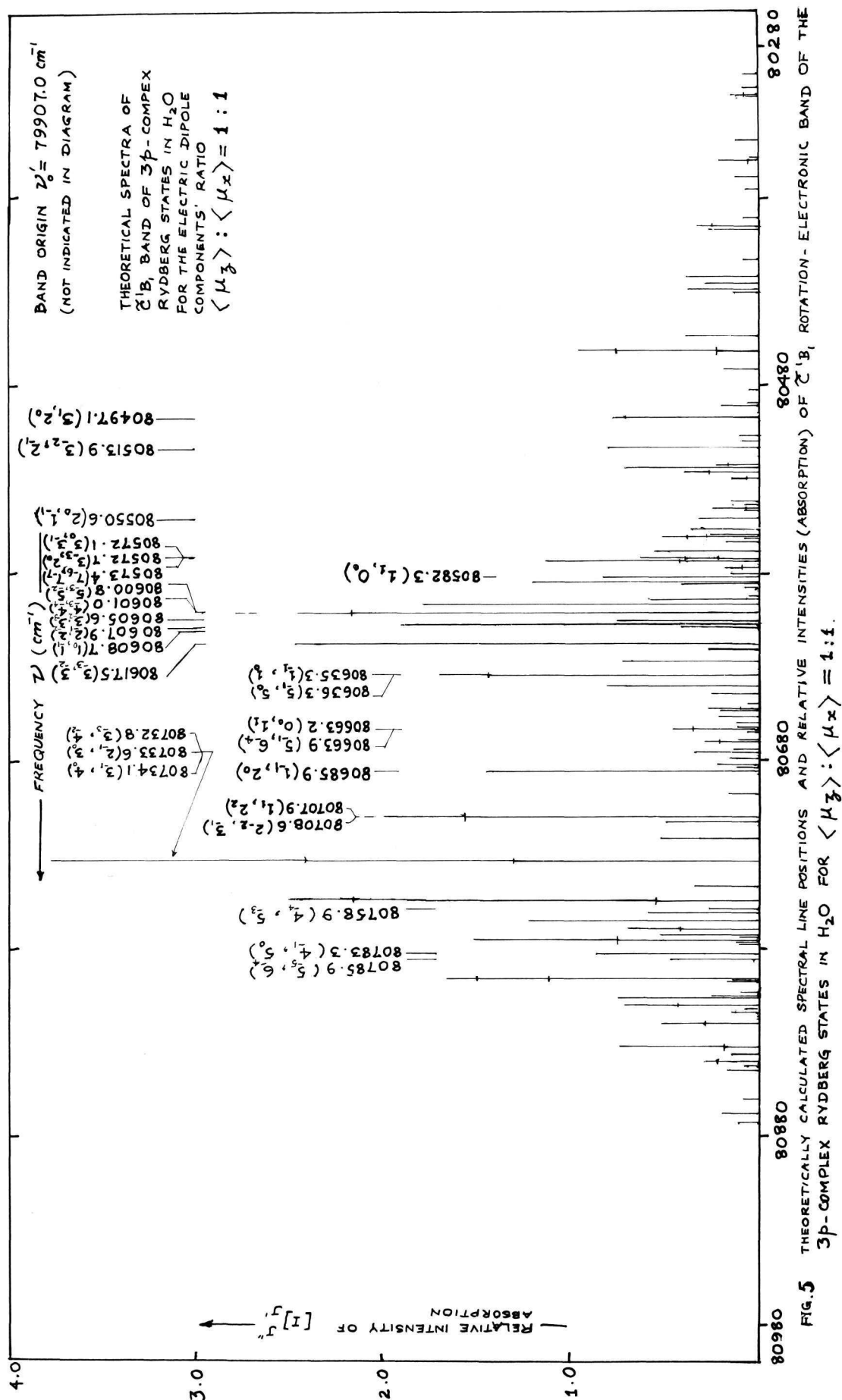


FIG. 4. THEORETICALLY CALCULATED SPECTRAL LINE POSITIONS AND RELATIVE INTENSITIES (ABSORPTION) OF  $\tilde{C}^1B_1$  ROTATION-ELECTRONIC BAND OF THE  $3p$ -COMPLEX RYDBERG STATES IN  $\text{H}_2\text{O}$  FOR  $\langle \mu_z \rangle : \langle \mu_x \rangle = 0:1$ . FOR THE PURPOSE OF COMPARISON WITH EXPERIMENTAL RESULTS, IMPORTANT LINE POSITIONS ARE IDENTIFIED EXPLICITLY. THE BRACKETS IDENTIFY THE STATES ( $J''$ ,  $J'$ ) INVOLVED IN A TRANSITION. WHENEVER LINE POSITIONS ARE VERY CLOSE, THEIR INTENSITIES APPEAR ALONG THE SAME VERTICAL LINE, THE LOWEST WAVE NUMBER'S INTENSITY APPEARING AT THE BOTTOM SECTION OF A LINE.





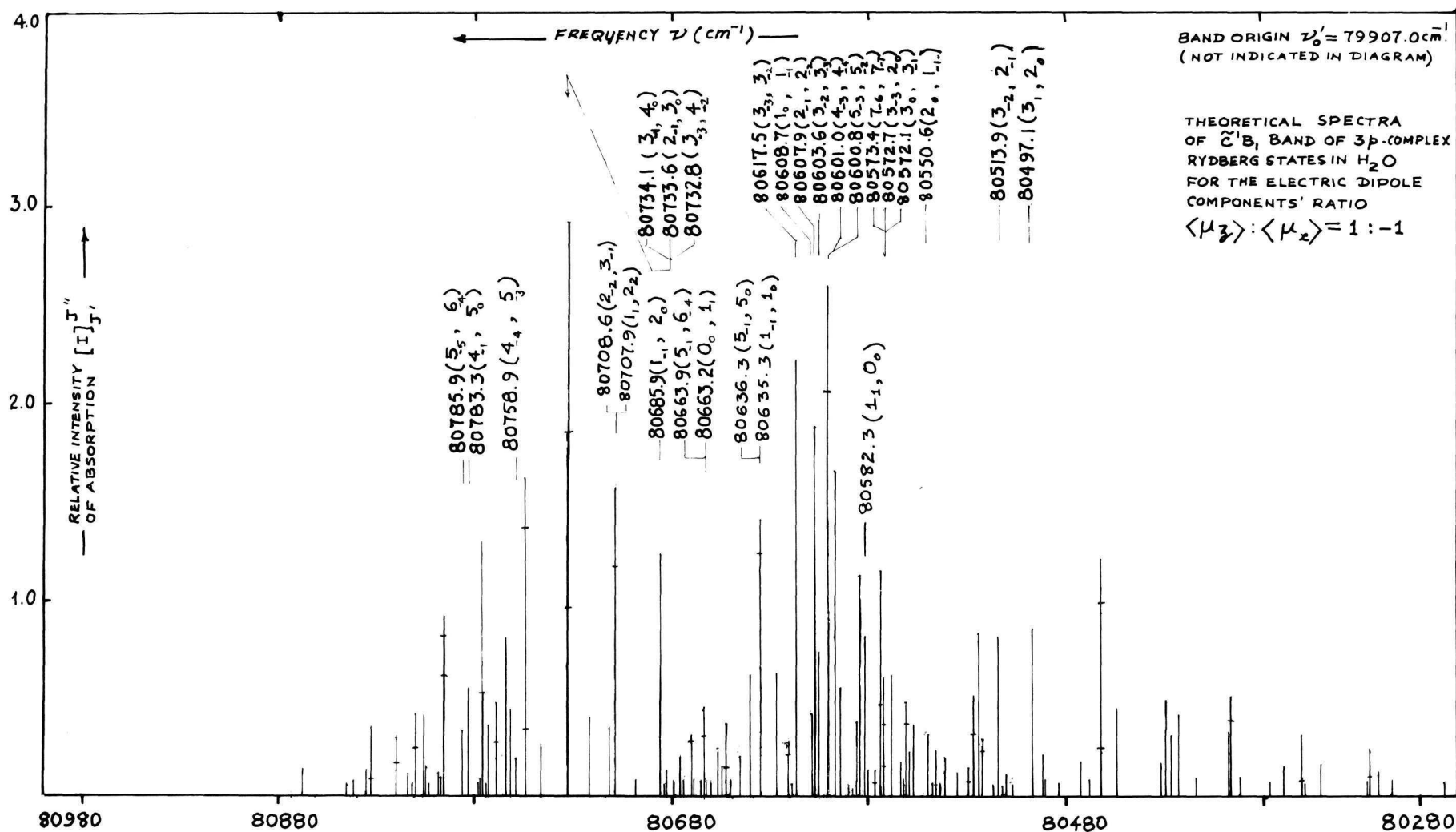


FIG. 6. THEORETICALLY CALCULATED SPECTRAL LINE POSITIONS AND RELATIVE INTENSITIES (ABSORPTION) OF  $\tilde{C}'B_1$  ROTATION-ELECTRONIC BAND OF THE 3p-COMPLEX RYDBERG STATE IN  $\text{H}_2\text{O}$  FOR  $\langle \mu_z \rangle : \langle \mu_x \rangle = 1 : -1$ .

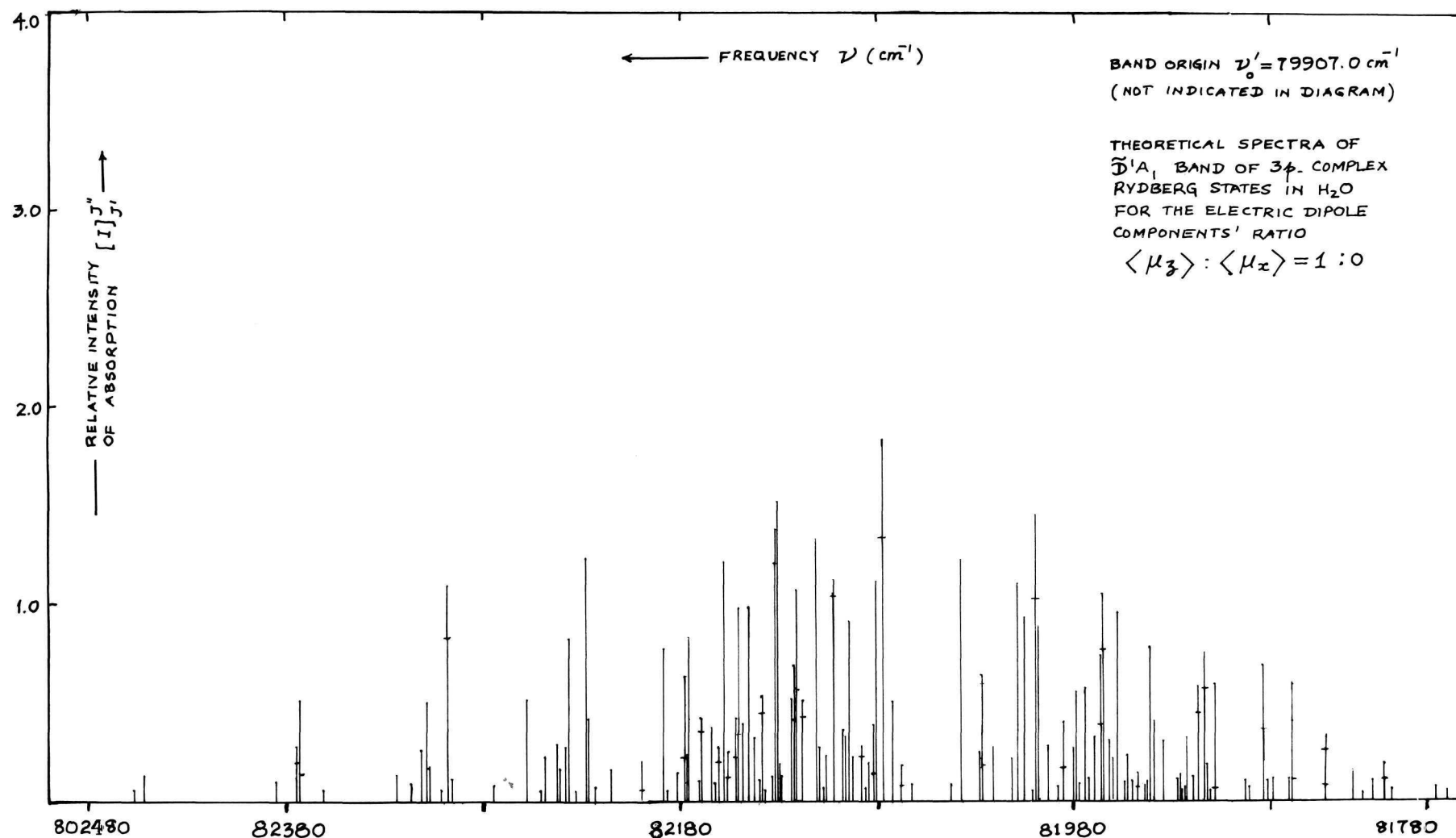


FIG. 7. THEORETICALLY CALCULATED SPECTRAL LINE POSITIONS AND RELATIVE INTENSITIES (ABSORPTION) OF  $\tilde{D}'A_1$  ROTATION-ELECTRONIC BAND OF THE 3p-COMPLEX RYDBERG STATE IN WATER FOR  $\langle \mu_z \rangle : \langle \mu_x \rangle = 1 : 0$

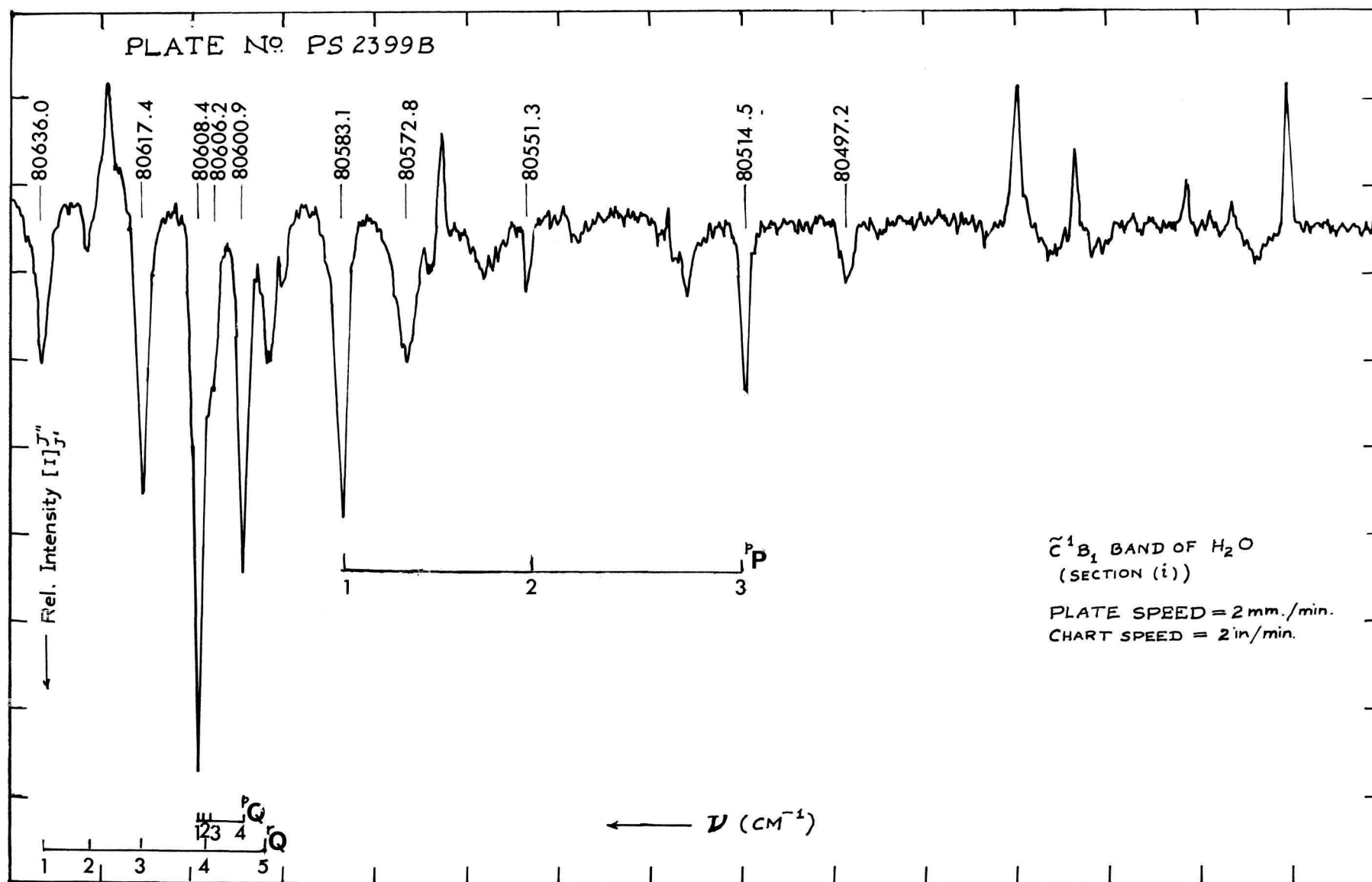


FIG. 8(2). EXPERIMENTAL SPECTRA OF THE  $\tilde{C}^1B_1$  BAND OF  $H_2O$ . THE SPECTRA WERE REPRODUCED ON A MICRODENSITOMETER FROM THE PHOTOGRAPHIC PLATE. (COURTESY OF DR. J.W.C. JOHNS OF HERZBERG INSTITUTE OF ASTROPHYSICS, NATIONAL RESEARCH COUNCIL, CANADA).

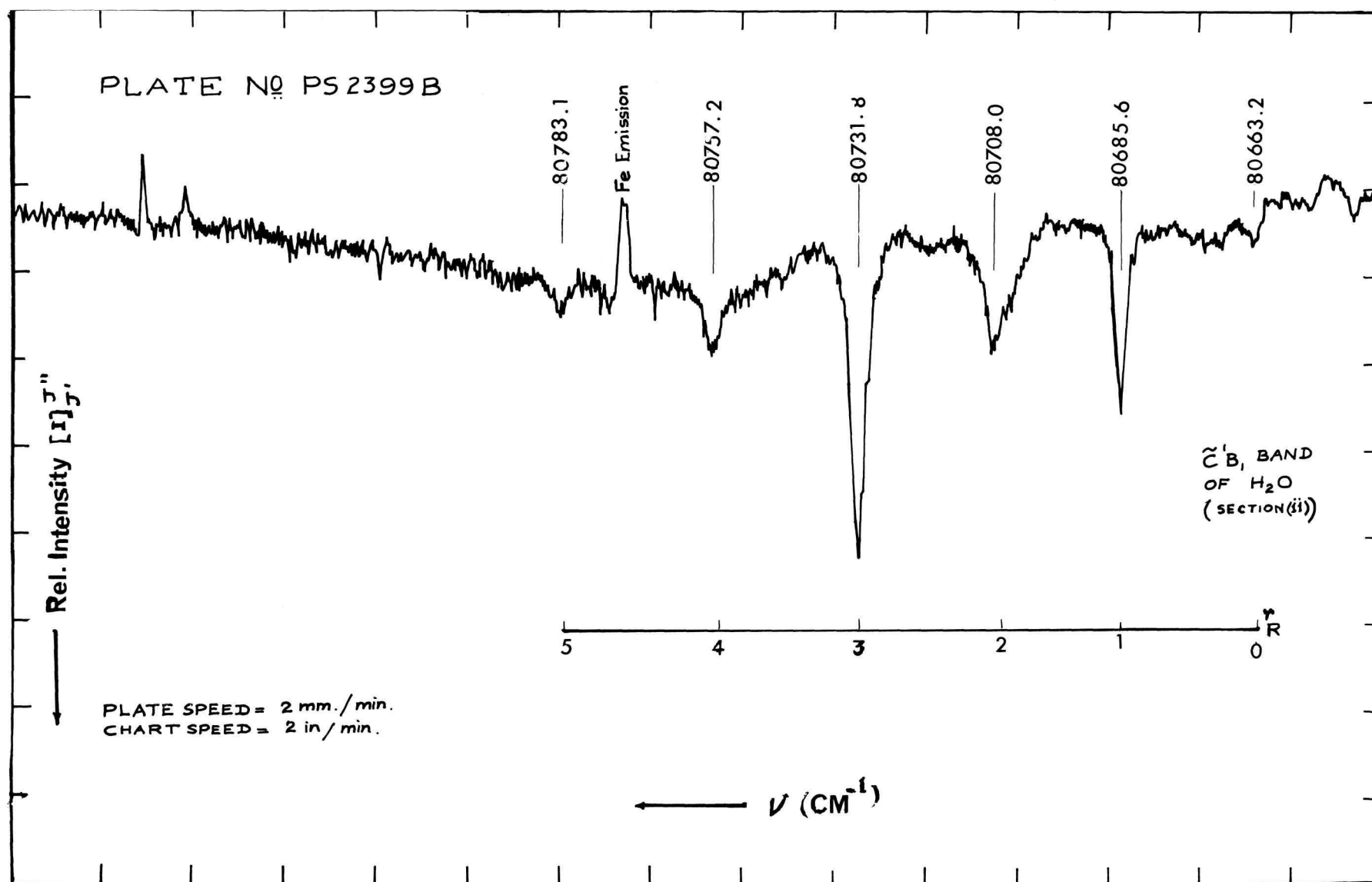


FIG 8(b). EXPERIMENTAL SPECTRA OF THE  $\tilde{C}^1B_1$  BAND OF  $H_2O$ . THE SPECTRA WERE REPRODUCED ON A MICRODENSITOMETER FROM THE PHOTOGRAPHIC PLATE (COURTESY OF DR. J.W.C. JOHNS OF HERZBERG INSTITUTE OF ASTROPHYSICS, NATIONAL RESEARCH COUNCIL, CANADA)

## 6. DISCUSSION OF THE RESULTS AND CONCLUSIONS

The results of the application of our theory to  $H_2O$  and  $D_2O$  are listed in TABLES IV.1, IV.2, V.1, V.2, V.3 and V.4. These results, on comparing with those given in TABLES II.1, II.2, III.1, III.2, III.3 and III.4, indicate that the line positions can be predicted to about the same accuracy by using the approximate method similar to that used by Creutzberg and Hougen[5]. This situation arises because the electronic levels in the p-complex are separated well enough so that the interactions among them is weak.

Approximate calculations of relative intensities assuming no interactions, are really not distinguishable from those of any of the three limiting cases of dipole components' ratios. There is, however, some evidence of interference effect. That is, some branches are slightly enhanced and some slightly weakened in their relative intensities when comparing one case to another. The effect can be expected to be enhanced when strong interactions are involved. However, for weak interactions, we see that the intensities show little departure from the usual rigid rotor case where no interactions are assumed.

Our results are also presented in the form of theoretical stick spectra, given by FIGS. 4, 5, 6 and 7, along with the experimental results supplied by

Dr. J.W.C. Johns (Private communication [24] ) for the  $\tilde{C}^1B_1$  band of  $H_2O$ , shown in FIG.8. Comparison of the theoretical and experimental spectra seems to show a qualitative agreement. Agreement is close, as should be, since the logarithmic response of the photographic plate, used to record the spectrum, tends to compensate for the exponential absorption law so that the intensities should be roughly proportional to the absorption coefficients or line strengths and is thus comparable to our calculated relative intensities.

It is, however, very clear that if calculations are carried out for higher Rydberg states (e.g.,  $\ell=1$ ,  $\ell=2$ ,  $\ell=3$ , etc.) the interactions are expected to become more and more significant with increasing  $\ell$  values, and the effect will appear in terms of changes in the intensity distribution. Therefore, in view of the present findings, it is suggested that calculations of energies and relative intensities be carried out in order to see the real effects of the interactions involved.

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## APPENDIX I

TABLE I.1

Character Table of the  $C_{2v}$  Point Group

$C_{2v}$	$\hat{E}$	$\hat{C}_{2z}$	$\hat{\sigma}_v(xz)$	$\hat{\sigma}_v(yz) \equiv \hat{\sigma}'_v$		
$A_1$	1	1	1	1		$\mu_z$
$A_2$	1	1	-1	-1	$R_z$	$\vec{\mu}(\text{SPACE FIXED})$
$B_1$	1	-1	1	-1	$R_y$	$\mu_x$
$B_2$	1	-1	-1	1	$R_x$	$\mu_y$

## APPENDIX II

TABLE II.1

Rotation-Electronic Energy Levels of the  $\tilde{X}^1A_1$ ,  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  States of  $H_2O$

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
Energy Level $J''_K''$	Energy $E''(cm^{-1})$	Energy Level $J'_K'$	Energy $E'(cm^{-1})$	Energy Level $J'_K'$	Energy $E'(cm^{-1})$
$0_0$	000.00	$0_0$	80624.70	$0_0$	82058.70
$1_{-1}$	023.80	$1_{-1}$	0645.89	$1_{-1}$	2079.94
$1_0$	037.16	$1_0$	0659.15	$1_0$	2097.47
$1_1$	042.39	$1_1$	0663.24	$1_1$	2101.77
$2_{-2}$	070.13	$2_{-2}$	0687.46	$2_{-2}$	2121.71
$2_{-1}$	079.53	$2_{-1}$	0697.44	$2_{-1}$	2135.65
$2_0$	095.21	$2_0$	0709.71	$2_0$	2148.54
$2_1$	135.31	$2_1$	0749.49	$2_1$	2201.15
$2_2$	136.56	$2_2$	0750.30	$2_2$	2201.85
$3_{-3}$	136.91	$3_{-3}$	0747.98	$3_{-3}$	2182.75
$3_{-2}$	142.37	$3_{-2}$	0754.41	$3_{-2}$	2192.51
$3_{-1}$	173.54	$3_{-1}$	0778.85	$3_{-1}$	2218.22
$3_0$	206.70	$3_0$	0813.06	$3_0$	2264.86
$3_1$	212.57	$3_1$	0816.92	$3_1$	2268.23
$3_2$	287.30	$3_2$	0890.05	$3_2$	2363.68
$3_3$	287.49	$3_3$	0890.15	$3_3$	2363.76
$4_{-4}$	222.37	$4_{-4}$	0826.05	$4_{-4}$	2261.61
$4_{-3}$	225.07	$4_{-3}$	0829.63	$4_{-3}$	2267.66

## APPX II

TABLE II.1 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
$J''_{\tau''}$	$E''(\text{cm}^{-1})$	$J'_{\tau'}$	$E'(\text{cm}^{-1})$	$J'_{\tau'}$	$E'(\text{cm}^{-1})$
4 <sub>-2</sub>	276.01	4 <sub>-2</sub>	80869.83	4 <sub>-2</sub>	82310.14
4 <sub>-1</sub>	300.89	4 <sub>-1</sub>	0897.19	4 <sub>-1</sub>	2349.26
4 <sub>0</sub>	316.47	4 <sub>0</sub>	0907.73	4 <sub>0</sub>	2358.72
4 <sub>1</sub>	384.52	4 <sub>1</sub>	0976.17	4 <sub>1</sub>	2449.84
4 <sub>2</sub>	385.85	4 <sub>2</sub>	0976.87	4 <sub>2</sub>	2450.33
4 <sub>3</sub>	494.62	4 <sub>3</sub>	1082.12	4 <sub>3</sub>	2586.56
4 <sub>4</sub>	494.64	4 <sub>4</sub>	1082.13	4 <sub>4</sub>	2586.57
5 <sub>-5</sub>	325.90	5 <sub>-5</sub>	0920.91	5 <sub>-5</sub>	2357.31
5 <sub>-4</sub>	327.10	5 <sub>-4</sub>	0922.71	5 <sub>-4</sub>	2360.70
5 <sub>-3</sub>	400.58	5 <sub>-3</sub>	0981.39	5 <sub>-3</sub>	2423.24
5 <sub>-2</sub>	417.10	5 <sub>-2</sub>	1001.34	5 <sub>-2</sub>	2453.90
5 <sub>-1</sub>	447.92	5 <sub>-1</sub>	1022.89	5 <sub>-1</sub>	2473.80
5 <sub>0</sub>	506.19	5 <sub>0</sub>	1084.00	5 <sub>0</sub>	2557.77
5 <sub>1</sub>	511.10	5 <sub>1</sub>	1086.67	5 <sub>1</sub>	2559.69
5 <sub>2</sub>	616.38	5 <sub>2</sub>	1189.86	5 <sub>2</sub>	2694.29
5 <sub>3</sub>	616.61	5 <sub>3</sub>	1189.95	5 <sub>3</sub>	2694.35
5 <sub>4</sub>	757.63	5 <sub>4</sub>	1325.95	5 <sub>4</sub>	2870.02
5 <sub>5</sub>	757.63	5 <sub>5</sub>	1325.95	5 <sub>5</sub>	2870.02
6 <sub>-6</sub>	447.60	6 <sub>-6</sub>	1032.48	6 <sub>-6</sub>	2469.53
6 <sub>-5</sub>	448.09	6 <sub>-5</sub>	1033.32	6 <sub>-5</sub>	2471.30

## APPX II

TABLE II.1 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
$J''_{\tau''}$	$E''(cm^{-1})$	$J'_{\tau'}$	$E'(cm^{-1})$	$J'_{\tau'}$	$E'(cm^{-1})$
6 <sub>-4</sub>	0544.85	6 <sub>-4</sub>	81111.85	6 <sub>-4</sub>	82556.09
6 <sub>-3</sub>	0554.43	6 <sub>-3</sub>	1124.94	6 <sub>-3</sub>	2578.24
6 <sub>-2</sub>	0605.51	6 <sub>-2</sub>	1161.68	6 <sub>-2</sub>	2613.13
6 <sub>-1</sub>	0651.86	6 <sub>-1</sub>	1213.34	6 <sub>-1</sub>	2687.36
6 <sub>0</sub>	0664.83	6 <sub>0</sub>	1220.69	6 <sub>0</sub>	2692.81
6 <sub>1</sub>	0763.19	6 <sub>1</sub>	1319.64	6 <sub>1</sub>	2824.02
6 <sub>2</sub>	0764.25	6 <sub>2</sub>	1320.10	6 <sub>2</sub>	2824.29
6 <sub>3</sub>	0903.63	6 <sub>3</sub>	1455.14	6 <sub>3</sub>	2999.21
6 <sub>4</sub>	0903.66	6 <sub>4</sub>	1455.15	6 <sub>4</sub>	2999.21
6 <sub>5</sub>	1076.38	6 <sub>5</sub>	1621.58	6 <sub>5</sub>	3214.08
6 <sub>6</sub>	1076.38	6 <sub>6</sub>	1621.58	6 <sub>6</sub>	3214.08
7 <sub>-7</sub>	0587.64	7 <sub>-7</sub>	1160.89	7 <sub>-7</sub>	2598.32
7 <sub>-6</sub>	0587.83	7 <sub>-6</sub>	1161.26	7 <sub>-6</sub>	2599.20
7 <sub>-5</sub>	0707.15	7 <sub>-5</sub>	1259.65	7 <sub>-5</sub>	2707.06
7 <sub>-4</sub>	0712.07	7 <sub>-4</sub>	1267.36	7 <sub>-4</sub>	2721.71
7 <sub>-3</sub>	0787.12	7 <sub>-3</sub>	1322.86	7 <sub>-3</sub>	2775.78
7 <sub>-2</sub>	0820.81	7 <sub>-2</sub>	1363.79	7 <sub>-2</sub>	2838.36
7 <sub>-1</sub>	0847.67	7 <sub>-1</sub>	1379.86	7 <sub>-1</sub>	2850.78
7 <sub>0</sub>	0935.09	7 <sub>0</sub>	1471.57	7 <sub>0</sub>	2975.90
7 <sub>1</sub>	0938.72	7 <sub>1</sub>	1473.19	7 <sub>1</sub>	2976.86
7 <sub>2</sub>	1074.74	7 <sub>2</sub>	1606.38	7 <sub>2</sub>	3150.36

## APPX II

TABLE II.1 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
$J''\tau''$	$E''(cm^{-1})$	$J'\tau'$	$E'(cm^{-1})$	$J'\tau'$	$E'(cm^{-1})$
$7_3$	1074.92	$7_3$	81606.44	$7_3$	83150.39
$7_4$	1246.58	$7_4$	1772.21	$7_4$	3364.72
$7_5$	1246.58	$7_5$	1772.21	$7_5$	3364.72
$7_6$	1450.89	$7_6$	1969.01	$7_6$	3618.75
$7_7$	1450.89	$7_7$	1969.01	$7_7$	3618.75
$8_{-8}$	0746.15	$8_{-8}$	1306.26	$8_{-8}$	2743.82
$8_{-7}$	0746.22	$8_{-7}$	1306.42	$8_{-7}$	2744.23
$8_{-6}$	0887.02	$8_{-6}$	1423.91	$8_{-6}$	2874.84
$8_{-5}$	0889.32	$8_{-5}$	1428.05	$8_{-5}$	2883.74
$8_{-4}$	0990.14	$8_{-4}$	1504.80	$8_{-4}$	2960.42
$8_{-3}$	1012.13	$8_{-3}$	1534.79	$8_{-3}$	3010.31
$8_{-2}$	1058.75	$8_{-2}$	1564.27	$8_{-2}$	3034.27
$8_{-1}$	1131.88	$8_{-1}$	1645.64	$8_{-1}$	3150.00
$8_0$	1141.57	$8_0$	1650.16	$8_0$	3152.74
$8_1$	1271.23	$8_1$	1779.86	$8_1$	3323.68
$8_2$	1271.99	$8_2$	1780.13	$8_2$	3323.81
$8_3$	1441.83	$8_3$	1944.84	$8_3$	3537.28
$8_4$	1441.86	$8_4$	1944.85	$8_4$	3537.28
$8_5$	1645.29	$8_5$	2141.09	$8_5$	3790.84
$8_6$	1645.29	$8_6$	2141.09	$8_6$	3790.84
$8_7$	1881.16	$8_7$	2368.24	$8_7$	4084.02

## APPX II

TABLE II.1 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
$J''_{\tau''}$	$E'' (cm^{-1})$	$J'_{\tau'}$	$E' (cm^{-1})$	$J'_{\tau'}$	$E' (cm^{-1})$
8 <sub>8</sub>	1881.16	8 <sub>8</sub>	82368.24	8 <sub>8</sub>	84084.02
9 <sub>-9</sub>	0923.18	9 <sub>-9</sub>	1468.66	9 <sub>-9</sub>	2906.12
9 <sub>-8</sub>	0923.21	9 <sub>-8</sub>	1468.73	9 <sub>-8</sub>	2906.31
9 <sub>-7</sub>	1084.69	9 <sub>-7</sub>	1604.49	9 <sub>-7</sub>	3058.79
9 <sub>-6</sub>	1085.70	9 <sub>-6</sub>	1606.56	9 <sub>-6</sub>	3063.82
9 <sub>-5</sub>	1212.03	9 <sub>-5</sub>	1705.59	9 <sub>-5</sub>	3165.42
9 <sub>-4</sub>	1224.83	9 <sub>-4</sub>	1725.68	9 <sub>-4</sub>	3202.66
9 <sub>-3</sub>	1296.07	9 <sub>-3</sub>	1773.05	9 <sub>-3</sub>	3243.12
9 <sub>-2</sub>	1353.00	9 <sub>-2</sub>	1841.62	9 <sub>-2</sub>	3346.26
9 <sub>-1</sub>	1374.21	9 <sub>-1</sub>	1852.15	9 <sub>-1</sub>	3352.90
9 <sub>0</sub>	1493.27	9 <sub>0</sub>	1975.76	9 <sub>0</sub>	3519.35
9 <sub>1</sub>	1495.76	9 <sub>1</sub>	1976.67	9 <sub>1</sub>	3519.80
9 <sub>2</sub>	1662.42	9 <sub>2</sub>	2139.65	9 <sub>2</sub>	3731.93
9 <sub>3</sub>	1662.55	9 <sub>3</sub>	2139.69	9 <sub>3</sub>	3731.94
9 <sub>4</sub>	1864.68	9 <sub>4</sub>	2335.12	9 <sub>4</sub>	3984.82
9 <sub>5</sub>	1864.68	9 <sub>5</sub>	2335.12	9 <sub>5</sub>	3984.82
9 <sub>6</sub>	2099.76	9 <sub>6</sub>	2561.77	9 <sub>6</sub>	4277.58
9 <sub>7</sub>	2099.76	9 <sub>7</sub>	2561.77	9 <sub>6</sub>	4277.58
9 <sub>8</sub>	2367.18	9 <sub>8</sub>	2819.27	9 <sub>8</sub>	4609.90
9 <sub>9</sub>	2367.18	9 <sub>9</sub>	2819.27	9 <sub>9</sub>	4609.90
10 <sub>-10</sub>	1118.77	10 <sub>-10</sub>	1648.12	10 <sub>-10</sub>	3085.29

## APPX II

TABLE II.1 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
$J''_{\tau''}$	$E''(\text{cm}^{-1})$	$J'_{\tau'}$	$E'(\text{cm}^{-1})$	$J'_{\tau'}$	$E'(\text{cm}^{-1})$
$10_{-9}$	1118.78	$10_{-9}$	81648.15	$10_{-9}$	83085.38
$10_{-8}$	1300.49	$10_{-8}$	1801.59	$10_{-8}$	3258.86
$10_{-7}$	1300.91	$10_{-7}$	1802.57	$10_{-7}$	3261.55
$10_{-6}$	1451.26	$10_{-6}$	1923.49	$10_{-6}$	3388.95
$10_{-5}$	1457.98	$10_{-5}$	1935.75	$10_{-5}$	3414.76
$10_{-4}$	1556.99	$10_{-4}$	2004.68	$10_{-4}$	3476.36
$10_{-3}$	1597.63	$10_{-3}$	2059.11	$10_{-3}$	3564.44
$10_{-2}$	1636.84	$10_{-2}$	2080.07	$10_{-2}$	3578.44
$10_{-1}$	1740.83	$10_{-1}$	2194.18	$10_{-1}$	3737.53
$10_0$	1747.57	$10_0$	2196.75	$10_0$	3738.81
$10_1$	1908.63	$10_1$	2356.84	$10_1$	3948.85
$10_2$	1909.15	$10_2$	2356.99	$10_2$	3948.91
$10_3$	2109.30	$10_3$	2551.27	$10_3$	4200.83
$10_4$	2109.33	$10_4$	2551.27	$10_4$	4200.83
$10_5$	2343.31	$10_5$	2777.22	$10_5$	4492.99
$10_6$	2343.31	$10_6$	2777.22	$10_6$	4492.99
$10_7$	2609.99	$10_7$	3034.26	$10_7$	4824.92
$10_8$	2609.99	$10_8$	3034.26	$10_8$	4824.92
$10_9$	2908.96	$10_9$	3322.10	$10_9$	5196.38
$10_{10}$	2908.96	$10_{10}$	3322.10	$10_{10}$	5196.38
$11_{-11}$	1332.91	$11_{-11}$	1844.67	$11_{-11}$	3281.37



## APPX II

TABLE II.1 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
$J''\tau''$	$E''(\text{cm}^{-1})$	$J'\tau'$	$E'(\text{cm}^{-1})$	$J'\tau'$	$E'(\text{cm}^{-1})$
11 <sub>-10</sub>	1332.92	11 <sub>-10</sub>	81844.68	11 <sub>-10</sub>	83281.41
11 <sub>-9</sub>	1534.63	11 <sub>-9</sub>	2015.44	11 <sub>-9</sub>	3475.26
11 <sub>-8</sub>	1534.81	11 <sub>-8</sub>	2015.89	11 <sub>-8</sub>	3476.65
11 <sub>-7</sub>	1707.58	11 <sub>-7</sub>	2157.49	11 <sub>-7</sub>	3629.39
11 <sub>-6</sub>	1710.83	11 <sub>-6</sub>	2164.37	11 <sub>-6</sub>	3645.97
11 <sub>-5</sub>	1838.51	11 <sub>-5</sub>	2257.26	11 <sub>-5</sub>	3732.52
11 <sub>-4</sub>	1864.77	11 <sub>-4</sub>	2297.51	11 <sub>-4</sub>	3804.13
11 <sub>-3</sub>	1928.04	11 <sub>-3</sub>	2333.99	11 <sub>-3</sub>	3830.19
11 <sub>-2</sub>	2013.57	11 <sub>-2</sub>	2435.08	11 <sub>-2</sub>	3978.31
11 <sub>-1</sub>	2029.06	11 <sub>-1</sub>	2441.35	11 <sub>-1</sub>	3981.52
11 <sub>0</sub>	2180.72	11 <sub>0</sub>	2596.62	11 <sub>0</sub>	4188.23
11 <sub>1</sub>	2182.35	11 <sub>1</sub>	2597.11	11 <sub>1</sub>	4188.42
11 <sub>2</sub>	2379.45	11 <sub>2</sub>	2789.70	11 <sub>2</sub>	4439.01
11 <sub>3</sub>	2379.54	11 <sub>3</sub>	2789.72	11 <sub>3</sub>	4439.02
11 <sub>4</sub>	2612.01	11 <sub>4</sub>	3014.73	11 <sub>4</sub>	4730.39
11 <sub>5</sub>	2612.01	11 <sub>5</sub>	3014.73	11 <sub>5</sub>	4730.39
11 <sub>6</sub>	2877.71	11 <sub>6</sub>	3271.14	11 <sub>6</sub>	5061.78
11 <sub>7</sub>	2877.71	11 <sub>7</sub>	3271.14	11 <sub>7</sub>	5061.78
11 <sub>8</sub>	3175.98	11 <sub>8</sub>	3558.54	11 <sub>8</sub>	5432.87
11 <sub>9</sub>	3175.98	11 <sub>9</sub>	3558.54	11 <sub>9</sub>	5432.87
11 <sub>10</sub>	3506.49	11 <sub>10</sub>	3876.73	11 <sub>10</sub>	5843.47
11 <sub>11</sub>	3506.49	11 <sub>11</sub>	3876.73	11 <sub>11</sub>	5843.47

## APPX II

TABLE II.2

Rotation-Electronic Energy Levels of the  $\tilde{X}^1A_1$ ,  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  States of  $D_2O$

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
Energy Level $J''_{\tau''}$	Energy $E''(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$
$0_0$	000.00	$0_0$	80751.90	$0_0$	82074.90
$1_{-1}$	012.12	$1_{-1}$	0762.63	$1_{-1}$	2085.64
$1_0$	020.23	$1_0$	0770.96	$1_0$	2095.34
$1_1$	022.65	$1_1$	0772.85	$1_1$	2097.32
$2_{-2}$	035.90	$2_{-2}$	0783.80	$2_{-2}$	2106.83
$2_{-1}$	042.05	$2_{-1}$	0790.53	$2_{-1}$	2114.84
$2_0$	049.31	$2_0$	0796.20	$2_0$	2120.76
$2_1$	073.64	$2_1$	0821.19	$2_1$	2149.88
$2_2$	074.11	$2_2$	0821.48	$2_2$	2150.16
$3_{-3}$	070.50	$3_{-3}$	0814.89	$3_{-3}$	2137.98
$3_{-2}$	074.51	$3_{-2}$	0819.72	$3_{-2}$	2143.92
$3_{-1}$	088.98	$3_{-1}$	0831.03	$3_{-1}$	2155.75
$3_0$	110.00	$3_0$	0853.38	$3_0$	2182.09
$3_1$	112.22	$3_1$	0854.77	$3_1$	2183.42
$3_2$	156.87	$3_2$	0899.92	$3_2$	2235.72
$3_3$	156.93	$3_3$	0899.95	$3_3$	2235.75
$4_{-4}$	115.09	$4_{-4}$	0855.27	$4_{-4}$	2178.47
$4_{-3}$	117.37	$4_{-3}$	0858.36	$4_{-3}$	2182.43

## APPX II

TABLE II.2 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
energy Level $J''_{\tau''}$	Energy $E'' (\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E' (\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E' (\text{cm}^{-1})$
4 <sub>-2</sub>	141.18	4 <sub>-2</sub>	80877.07	4 <sub>-2</sub>	82202.02
4 <sub>-1</sub>	158.12	4 <sub>-1</sub>	0896.08	4 <sub>-1</sub>	2224.82
4 <sub>0</sub>	164.22	4 <sub>0</sub>	0900.01	4 <sub>0</sub>	2228.60
4 <sub>1</sub>	206.13	4 <sub>1</sub>	0943.34	4 <sub>1</sub>	2279.15
4 <sub>2</sub>	206.52	4 <sub>2</sub>	0943.53	4 <sub>2</sub>	2279.31
4 <sub>3</sub>	270.69	4 <sub>3</sub>	1007.82	4 <sub>3</sub>	2353.58
4 <sub>4</sub>	270.69	4 <sub>4</sub>	1007.83	4 <sub>4</sub>	2353.58
5 <sub>-5</sub>	169.22	5 <sub>-5</sub>	0904.49	5 <sub>-5</sub>	2227.79
5 <sub>-4</sub>	170.38	5 <sub>-4</sub>	0906.28	5 <sub>-4</sub>	2230.2
5 <sub>-3</sub>	205.18	5 <sub>-3</sub>	0933.89	5 <sub>-3</sub>	2259.19
5 <sub>-2</sub>	217.68	5 <sub>-2</sub>	0949.09	5 <sub>-2</sub>	2277.89
5 <sub>-1</sub>	230.21	5 <sub>-1</sub>	0957.43	5 <sub>-1</sub>	2286.02
5 <sub>0</sub>	267.83	5 <sub>0</sub>	0997.72	5 <sub>0</sub>	2333.53
5 <sub>1</sub>	269.32	5 <sub>1</sub>	0998.46	5 <sub>1</sub>	2334.18
5 <sub>2</sub>	332.32	5 <sub>2</sub>	1062.11	5 <sub>2</sub>	2407.86
5 <sub>3</sub>	332.37	5 <sub>3</sub>	1062.13	5 <sub>3</sub>	2407.88
5 <sub>4</sub>	415.24	5 <sub>4</sub>	1145.00	5 <sub>4</sub>	2503.56
5 <sub>5</sub>	415.24	5 <sub>5</sub>	1145.00	5 <sub>5</sub>	2503.56
6 <sub>-6</sub>	232.82	6 <sub>-6</sub>	0962.37	6 <sub>-6</sub>	2285.71

## APPX II

TABLE II.2 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
Energy Level $J''_{\tau''}$	Energy $E''(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$
6 <sub>-5</sub>	233.37	6 <sub>-5</sub>	80963.34	6 <sub>-5</sub>	82287.07
6 <sub>-4</sub>	280.04	6 <sub>-4</sub>	1000.91	6 <sub>-4</sub>	2326.70
6 <sub>-3</sub>	288.36	6 <sub>-3</sub>	1012.20	6 <sub>-3</sub>	2341.10
6 <sub>-2</sub>	309.81	6 <sub>-2</sub>	1026.96	6 <sub>-2</sub>	2355.65
6 <sub>-1</sub>	341.84	6 <sub>-1</sub>	1063.03	6 <sub>-1</sub>	2398.87
6 <sub>0</sub>	345.98	6 <sub>0</sub>	1065.15	6 <sub>0</sub>	2400.72
6 <sub>1</sub>	406.56	6 <sub>1</sub>	1127.44	6 <sub>1</sub>	2473.18
6 <sub>2</sub>	406.81	6 <sub>2</sub>	1127.54	6 <sub>2</sub>	2473.25
6 <sub>3</sub>	489.15	6 <sub>3</sub>	1210.10	6 <sub>3</sub>	2568.65
6 <sub>4</sub>	489.15	6 <sub>4</sub>	1210.10	6 <sub>4</sub>	2568.65
6 <sub>5</sub>	590.56	6 <sub>5</sub>	1311.45	6 <sub>5</sub>	2685.65
6 <sub>6</sub>	590.56	6 <sub>6</sub>	1311.45	6 <sub>6</sub>	2685.65
7 <sub>-7</sub>	305.95	7 <sub>-7</sub>	1028.92	7 <sub>-7</sub>	2352.19
7 <sub>-6</sub>	306.20	7 <sub>-6</sub>	1029.42	7 <sub>-6</sub>	2352.92
7 <sub>-5</sub>	364.80	7 <sub>-5</sub>	1077.44	7 <sub>-5</sub>	2403.89
7 <sub>-4</sub>	369.79	7 <sub>-4</sub>	1085.17	7 <sub>-4</sub>	2414.19
7 <sub>-3</sub>	402.32	7 <sub>-3</sub>	1108.24	7 <sub>-3</sub>	2437.22
7 <sub>-2</sub>	427.95	7 <sub>-2</sub>	1139.17	7 <sub>-2</sub>	2475.08
7 <sub>-1</sub>	437.07	7 <sub>-1</sub>	1144.06	7 <sub>-1</sub>	2479.41

## APPX II

TABLE II.2 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
Energy Level $J''_{\tau''}$	Energy $E''(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$
7 <sub>0</sub>	493.48	7 <sub>0</sub>	81203.89	7 <sub>0</sub>	82549.61
7 <sub>1</sub>	494.37	7 <sub>1</sub>	1204.23	7 <sub>1</sub>	2549.88
7 <sub>2</sub>	575.66	7 <sub>2</sub>	1286.24	7 <sub>2</sub>	2644.77
7 <sub>3</sub>	575.69	7 <sub>3</sub>	1286.25	7 <sub>3</sub>	2644.78
7 <sub>4</sub>	676.73	7 <sub>4</sub>	1387.37	7 <sub>4</sub>	2761.57
7 <sub>5</sub>	676.73	7 <sub>5</sub>	1387.37	7 <sub>5</sub>	2761.57
7 <sub>6</sub>	796.64	7 <sub>6</sub>	1507.18	7 <sub>6</sub>	2899.88
7 <sub>7</sub>	796.64	7 <sub>7</sub>	1507.18	7 <sub>7</sub>	2899.88
8 <sub>-8</sub>	388.69	8 <sub>-8</sub>	1104.19	8 <sub>-8</sub>	2427.29
8 <sub>-7</sub>	388.80	8 <sub>-7</sub>	1104.34	8 <sub>-7</sub>	2427.67
8 <sub>-6</sub>	458.91	8 <sub>-6</sub>	1162.86	8 <sub>-6</sub>	2490.10
8 <sub>-5</sub>	461.64	8 <sub>-5</sub>	1167.74	8 <sub>-5</sub>	2496.94
8 <sub>-4</sub>	506.79	8 <sub>-4</sub>	1200.74	8 <sub>-4</sub>	2530.24
8 <sub>-3</sub>	525.84	8 <sub>-3</sub>	1225.96	8 <sub>-3</sub>	2562.01
8 <sub>-2</sub>	542.70	8 <sub>-2</sub>	1235.53	8 <sub>-2</sub>	2570.66
8 <sub>-1</sub>	593.09	8 <sub>-1</sub>	1291.49	8 <sub>-1</sub>	2637.19
8 <sub>0</sub>	595.57	8 <sub>0</sub>	1292.48	8 <sub>0</sub>	2637.98
8 <sub>1</sub>	674.90	8 <sub>1</sub>	1373.48	8 <sub>1</sub>	2731.99
8 <sub>2</sub>	675.04	8 <sub>2</sub>	1373.53	8 <sub>2</sub>	2732.02

## APPX II

TABLE II.2 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
Energy Level $J''_{\tau''}$	Energy $E'' (\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E' (\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E' (\text{cm}^{-1})$
8 <sub>3</sub>	0775.47	8 <sub>3</sub>	81474.30	8 <sub>3</sub>	82848.48
8 <sub>4</sub>	0775.48	8 <sub>4</sub>	1474.31	8 <sub>4</sub>	2848.49
8 <sub>5</sub>	0895.07	8 <sub>5</sub>	1593.92	8 <sub>5</sub>	2986.61
8 <sub>6</sub>	0895.07	8 <sub>6</sub>	1593.92	8 <sub>6</sub>	2986.61
8 <sub>7</sub>	1033.48	8 <sub>7</sub>	1732.19	8 <sub>7</sub>	3146.23
8 <sub>8</sub>	1033.48	8 <sub>8</sub>	1732.19	8 <sub>8</sub>	3146.23
9 <sub>-9</sub>	0481.09	9 <sub>-9</sub>	1188.23	9 <sub>-9</sub>	2511.05
9 <sub>-8</sub>	0481.13	9 <sub>-8</sub>	1188.35	9 <sub>-8</sub>	2511.25
9 <sub>-7</sub>	0562.26	9 <sub>-7</sub>	1256.84	9 <sub>-7</sub>	2584.87
9 <sub>-6</sub>	0563.65	9 <sub>-6</sub>	1259.70	9 <sub>-6</sub>	2589.11
9 <sub>-5</sub>	0622.13	9 <sub>-5</sub>	1303.78	9 <sub>-5</sub>	2634.09
9 <sub>-4</sub>	0635.11	9 <sub>-4</sub>	1323.18	9 <sub>-4</sub>	2659.46
9 <sub>-3</sub>	0662.40	9 <sub>-3</sub>	1339.60	9 <sub>-3</sub>	2674.62
9 <sub>-2</sub>	0705.26	9 <sub>-2</sub>	1390.23	9 <sub>-2</sub>	2735.95
9 <sub>-1</sub>	0711.07	9 <sub>-1</sub>	1392.66	9 <sub>-1</sub>	2737.90
9 <sub>0</sub>	0786.97	9 <sub>0</sub>	1471.92	9 <sub>0</sub>	2830.38
9 <sub>1</sub>	0787.45	9 <sub>1</sub>	1472.07	9 <sub>1</sub>	2830.49
9 <sub>2</sub>	0886.91	9 <sub>2</sub>	1572.32	9 <sub>2</sub>	2946.47
9 <sub>3</sub>	0886.93	9 <sub>3</sub>	1572.32	9 <sub>3</sub>	2946.47

## APPX II

TABLE II.2 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
Energy Level $J''_{\tau''}$	Energy $E''(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$
9 <sub>4</sub>	1006.06	9 <sub>4</sub>	1691.66	9 <sub>4</sub>	3084.34
9 <sub>5</sub>	1006.06	9 <sub>5</sub>	1691.66	9 <sub>5</sub>	3084.34
9 <sub>6</sub>	1144.18	9 <sub>6</sub>	1829.76	9 <sub>6</sub>	3243.78
9 <sub>7</sub>	1144.18	9 <sub>7</sub>	1829.76	9 <sub>7</sub>	3243.78
9 <sub>8</sub>	1301.07	9 <sub>8</sub>	1986.49	9 <sub>8</sub>	3424.70
9 <sub>9</sub>	1301.07	9 <sub>9</sub>	1986.49	9 <sub>9</sub>	3424.70
10 <sub>-10</sub>	0583.16	10 <sub>-10</sub>	1281.07	10 <sub>-10</sub>	2603.43
10 <sub>-9</sub>	0583.18	10 <sub>-9</sub>	1281.13	10 <sub>-9</sub>	2603.62
10 <sub>-8</sub>	0674.94	10 <sub>-8</sub>	1359.27	10 <sub>-8</sub>	2688.01
10 <sub>-7</sub>	0675.61	10 <sub>-7</sub>	1360.87	10 <sub>-7</sub>	2690.50
10 <sub>-6</sub>	0747.30	10 <sub>-6</sub>	1416.62	10 <sub>-6</sub>	2748.06
10 <sub>-5</sub>	0755.38	10 <sub>-5</sub>	1430.57	10 <sub>-5</sub>	2767.18
10 <sub>-4</sub>	0795.35	10 <sub>-4</sub>	1455.95	10 <sub>-4</sub>	2791.11
10 <sub>-3</sub>	0829.78	10 <sub>-3</sub>	1500.04	10 <sub>-3</sub>	2845.84
10 <sub>-2</sub>	0841.46	10 <sub>-2</sub>	1505.24	10 <sub>-2</sub>	2850.08
10 <sub>-1</sub>	0911.94	10 <sub>-1</sub>	1581.63	10 <sub>-1</sub>	2940.03
10 <sub>0</sub>	0913.31	10 <sub>0</sub>	1582.06	10 <sub>0</sub>	2940.34
10 <sub>1</sub>	1011.15	10 <sub>1</sub>	1681.48	10 <sub>1</sub>	3055.59
10 <sub>2</sub>	1011.23	10 <sub>2</sub>	1681.50	10 <sub>2</sub>	3055.60

## APPX II

TABLE II.2 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
Energy Level $J''_{\tau''}$	Energy $E''(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E'(\text{cm}^{-1})$
10 <sub>3</sub>	1129.70	10 <sub>3</sub>	81800.45	10 <sub>3</sub>	83193.10
10 <sub>4</sub>	1129.70	10 <sub>4</sub>	1800.45	10 <sub>4</sub>	3193.10
10 <sub>5</sub>	1267.42	10 <sub>5</sub>	1938.31	10 <sub>5</sub>	3352.32
10 <sub>6</sub>	1267.42	10 <sub>6</sub>	1938.31	10 <sub>6</sub>	3352.32
10 <sub>7</sub>	1424.05	10 <sub>7</sub>	2094.87	10 <sub>7</sub>	3533.08
10 <sub>8</sub>	1424.05	10 <sub>8</sub>	2094.87	10 <sub>8</sub>	3533.08
10 <sub>9</sub>	1599.43	10 <sub>9</sub>	2270.06	10 <sub>9</sub>	3735.30
10 <sub>10</sub>	1599.43	10 <sub>10</sub>	2270.06	10 <sub>10</sub>	3735.30
11 <sub>-11</sub>	0694.93	11 <sub>-11</sub>	1382.74	11 <sub>-11</sub>	2704.73
11 <sub>-10</sub>	0694.93	11 <sub>-10</sub>	1382.76	11 <sub>-10</sub>	2704.78
11 <sub>-9</sub>	0797.10	11 <sub>-9</sub>	1470.25	11 <sub>-9</sub>	2799.55
11 <sub>-8</sub>	0797.41	11 <sub>-8</sub>	1471.10	11 <sub>-8</sub>	2800.95
11 <sub>-7</sub>	0881.62	11 <sub>-7</sub>	1538.50	11 <sub>-7</sub>	2871.36
11 <sub>-6</sub>	0886.25	11 <sub>-6</sub>	1547.85	11 <sub>-6</sub>	2884.88
11 <sub>-5</sub>	0940.43	11 <sub>-5</sub>	1584.01	11 <sub>-5</sub>	2919.68
11 <sub>-4</sub>	0966.30	11 <sub>-4</sub>	1620.76	11 <sub>-4</sub>	2966.74
11 <sub>-3</sub>	0986.83	11 <sub>-3</sub>	1630.64	11 <sub>-3</sub>	2974.97
11 <sub>-2</sub>	1049.81	11 <sub>-2</sub>	1702.64	11 <sub>-2</sub>	3061.00
11 <sub>-1</sub>	1053.17	11 <sub>-1</sub>	1703.74	11 <sub>-1</sub>	3061.79



## APPX II

TABLE II.2 (Continued)

GROUND STATE $\tilde{X}^1A_1$		EXCITED STATE $\tilde{C}^1B_1$		EXCITED STATE $\tilde{D}^1A_1$	
Energy Level $J''_{\tau''}$	Energy $E'' (\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E' (\text{cm}^{-1})$	Energy Level $J'_{\tau'}$	Energy $E' (\text{cm}^{-1})$
$11_0$	1148.32	$11_0$	1801.88	$11_0$	3175.92
$11_1$	1148.58	$11_1$	1801.94	$11_1$	3175.96
$11_2$	1266.09	$11_2$	1920.36	$11_2$	3312.96
$11_3$	1266.10	$11_3$	1920.36	$11_3$	3312.96
$11_4$	1403.28	$11_4$	2057.89	$11_4$	3471.88
$11_5$	1403.28	$11_5$	2059.89	$11_5$	3471.88
$11_6$	1559.55	$11_6$	2214.24	$11_6$	3652.43
$11_7$	1559.55	$11_7$	2214.24	$11_7$	3652.43
$11_8$	1734.68	$11_8$	2389.27	$11_8$	3854.50
$11_9$	1734.68	$11_9$	2389.27	$11_9$	3854.50
$11_{10}$	1928.55	$11_{10}$	2582.91	$11_{10}$	4078.02
$11_{11}$	1928.55	$11_{11}$	2582.91	$11_{11}$	4078.02

## APPENDIX III

TABLE III.1

 $\tilde{C}^1B_1$  Transitions in  $H_2O$  Calculated for  $\langle \mu_x \rangle = 1$ 

(No electronic interactions)

IDENTIFICATION			FREQUENCY	*RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $cm^{-1}$ )	$[I]_{J'}^{J''} \times 10$
R	0 <sub>0</sub>	1 <sub>1</sub>	80663.2	3.3
P	1 <sub>1</sub>	0 <sub>0</sub>	582.3	8.1
Q	1 <sub>0</sub>	1 <sub>-1</sub>	608.7	4.2
	1 <sub>-1</sub>	1 <sub>0</sub>	635.4	13.3
R	1 <sub>1</sub>	2 <sub>-2</sub>	645.1	2.6
	1 <sub>-1</sub>	2 <sub>0</sub>	685.9	13.3
	1 <sub>1</sub>	2 <sub>2</sub>	707.9	13.7
	1 <sub>0</sub>	2 <sub>1</sub>	712.3	4.2
P	2 <sub>1</sub>	1 <sub>0</sub>	523.8	7.7
	2 <sub>2</sub>	1 <sub>1</sub>	526.7	2.9
	2 <sub>0</sub>	1 <sub>-1</sub>	550.7	3.1
	2 <sub>-2</sub>	1 <sub>1</sub>	593.1	0.7
Q	2 <sub>2</sub>	2 <sub>-2</sub>	560.9	0.8
	2 <sub>1</sub>	2 <sub>0</sub>	574.4	4.3
	2 <sub>-1</sub>	2 <sub>-2</sub>	607.9	19.0
	2 <sub>-2</sub>	2 <sub>-2</sub>	627.3	6.8
	2 <sub>0</sub>	2 <sub>1</sub>	654.3	1.7
	2 <sub>-1</sub>	2 <sub>2</sub>	670.8	3.6

\*Values of  $[I]_{J'}^{J''} \times 10$  less than 0.5 are not included in this table.

## APPX III

TABLE III.1 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ ( $\text{cm}^{-1}$ )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$
Branch	$J''_{\alpha''}$	$J'_{\alpha'}$		
R	$2_1$	$3_{-2}$	80619.1	0.5
	$2_0$	$3_{-3}$	652.8	0.9
	$2_{-2}$	$3_{-1}$	708.7	4.3
	$2_0$	$3_1$	721.7	4.6
	$2_{-1}$	$3_0$	733.5	11.3
	$2_2$	$3_3$	753.6	4.4
	$2_1$	$3_2$	754.7	13.2
P	$3_2$	$2_1$	462.2	2.1
	$3_3$	$2_2$	462.8	6.4
	$3_0$	$2_{-2}$	490.7	2.0
	$3_1$	$2_0$	497.1	8.1
	$3_{-1}$	$2_{-2}$	513.9	8.0
	$3_{-3}$	$2_0$	572.8	1.8
	$3_{-1}$	$2_2$	576.8	0.8
Q	$3_3$	$3_0$	525.6	1.7
	$3_2$	$3_1$	529.6	0.6
	$3_1$	$3_{-2}$	541.8	1.7
	$3_0$	$3_{-1}$	572.2	2.0
	$3_{-2}$	$3_{-3}$	605.6	7.4
	$3_{-3}$	$3_{-2}$	617.5	23.5
	$3_{-1}$	$3_0$	639.5	7.1
	$3_{-2}$	$3_1$	674.5	1.0
	$3_1$	$3_2$	677.5	2.6

## APPX III

TABLE III.1 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
R	$3_0$	$3_3$	80683.5	0.9
	$3_1$	$4_{-4}$	652.5	1.8
	$3_1$	$4_{-2}$	657.3	2.1
	$3_{-3}$	$4_{-2}$	732.9	10.0
	$3_{-1}$	$4_0$	734.2	12.2
	$3_{-2}$	$4_{-1}$	754.8	3.0
	$3_1$	$4_2$	764.3	10.1
	$3_0$	$4_1$	769.5	3.4
	$3_3$	$4_4$	794.6	8.7
P	$3_2$	$4_3$	794.8	2.9
	$4_3$	$3_2$	395.4	3.2
	$4_4$	$3_3$	395.5	1.1
	$4_1$	$3_0$	428.5	4.3
	$4_2$	$3_1$	431.1	1.5
	$4_{-1}$	$3_{-2}$	453.5	4.2
	$4_0$	$3_{-1}$	462.4	2.1
	$4_{-2}$	$3_{-3}$	472.0	1.8
	$4_{-3}$	$3_0$	588.0	0.5
Q	$4_3$	$4_2$	482.2	0.7
	$4_2$	$4_{-1}$	511.3	0.5
	$4_1$	$4_0$	523.2	2.0
	$4_{-1}$	$4_{-2}$	568.9	5.9

## APPX III

TABLE III.1 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
R	$4_{-3}$	$4_{-4}$	80601.0	21.2
	$4_{-4}$	$4_{-3}$	607.3	7.3
	$4_{-2}$	$4_{-1}$	621.2	2.3
	$4_0$	$4_1$	659.7	0.9
	$4_{-1}$	$4_2$	676.0	2.7
	$4_{-3}$	$4_0$	682.7	1.7
	$4_1$	$4_4$	697.6	1.2
	$4_{-1}$	$5_{-4}$	621.8	0.5
	$4_0$	$5_{-3}$	664.9	0.7
	$4_{-2}$	$5_{-1}$	746.9	2.9
	$4_{-4}$	$5_{-3}$	759.0	2.2
	$4_0$	$5_1$	770.2	2.3
	$4_{-3}$	$5_{-2}$	776.3	6.3
	$4_{-1}$	$5_0$	783.1	7.1
	$4_2$	$5_3$	804.1	1.9
	$4_1$	$5_2$	805.3	5.8
	$4_4$	$5_5$	831.3	1.3
	$4_3$	$5_4$	831.3	4.0
P	$5_5$	$4_4$	324.5	1.1
	$5_2$	$4_1$	359.8	0.6
	$5_3$	$4_2$	360.3	1.9
	$5_0$	$4_{-1}$	391.0	0.9
	$5_1$	$4_0$	396.6	2.9

## APPX III

TABLE III.1 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
Q	5 <sub>-2</sub>	4 <sub>-3</sub>	80412.5	0.8
	5 <sub>-1</sub>	4 <sub>-2</sub>	421.9	4.0
	5 <sub>-3</sub>	4 <sub>-4</sub>	425.5	3.0
	5 <sub>-3</sub>	4 <sub>0</sub>	507.1	0.8
	5 <sub>-5</sub>	4 <sub>-2</sub>	543.9	0.5
	5 <sub>3</sub>	5 <sub>0</sub>	467.4	0.6
	5 <sub>1</sub>	5 <sub>-2</sub>	490.2	0.8
	5 <sub>0</sub>	5 <sub>-1</sub>	516.7	0.5
	5 <sub>-2</sub>	5 <sub>-3</sub>	564.3	1.7
	5 <sub>-4</sub>	5 <sub>-5</sub>	593.8	5.6
	5 <sub>-5</sub>	5 <sub>-4</sub>	596.8	17.3
	5 <sub>-3</sub>	5 <sub>-2</sub>	600.8	5.8
	5 <sub>-1</sub>	5 <sub>0</sub>	636.1	2.2
	5 <sub>-2</sub>	5 <sub>1</sub>	669.6	0.6
R	5 <sub>1</sub>	5 <sub>2</sub>	678.8	1.1
	5 <sub>1</sub>	6 <sub>-2</sub>	650.6	0.7
	5 <sub>-1</sub>	6 <sub>-4</sub>	663.9	1.2
	5 <sub>-3</sub>	6 <sub>-2</sub>	761.1	5.1
	5 <sub>-1</sub>	6 <sub>0</sub>	772.8	4.4
	5 <sub>-5</sub>	6 <sub>-4</sub>	785.9	3.9
	5 <sub>-2</sub>	6 <sub>-1</sub>	796.2	1.4
	5 <sub>-4</sub>	6 <sub>-3</sub>	797.8	1.3
	5 <sub>1</sub>	6 <sub>2</sub>	809.0	3.3

## APPX III

TABLE III.1 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	5 <sub>0</sub>	6 <sub>1</sub>	80813.4	1.1
	5 <sub>3</sub>	6 <sub>4</sub>	838.5	2.3
	5 <sub>2</sub>	6 <sub>3</sub>	838.8	0.8
	5 <sub>5</sub>	6 <sub>6</sub>	863.9	1.3
P				
	6 <sub>3</sub>	5 <sub>2</sub>	286.2	0.6
	6 <sub>1</sub>	5 <sub>0</sub>	320.8	1.0
	6 <sub>-1</sub>	5 <sub>-2</sub>	349.5	1.4
	6 <sub>0</sub>	5 <sub>-1</sub>	358.1	0.6
	6 <sub>-3</sub>	5 <sub>-4</sub>	368.3	1.3
	6 <sub>-2</sub>	5 <sub>-3</sub>	375.9	0.7
Q				
	6 <sub>-1</sub>	6 <sub>-2</sub>	509.8	1.0
	6 <sub>-3</sub>	6 <sub>-4</sub>	557.4	3.6
	6 <sub>-4</sub>	6 <sub>-3</sub>	580.1	1.4
	6 <sub>-5</sub>	6 <sub>-6</sub>	584.4	11.6
	6 <sub>-6</sub>	6 <sub>-5</sub>	585.7	3.9
	6 <sub>-3</sub>	6 <sub>0</sub>	666.3	0.9
	6 <sub>-1</sub>	6 <sub>2</sub>	668.2	0.8
R				
	6 <sub>-2</sub>	7 <sub>-1</sub>	774.4	0.8
	6 <sub>-4</sub>	7 <sub>-3</sub>	778.0	0.9
	6 <sub>0</sub>	7 <sub>1</sub>	808.4	0.6
	6 <sub>-3</sub>	7 <sub>-2</sub>	809.4	2.3
	6 <sub>-6</sub>	7 <sub>-5</sub>	812.1	0.7

## APPX III

TABLE III.1 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	6 <sub>-5</sub>	7 <sub>-4</sub>	80819.3	2.2
	6 <sub>-1</sub>	7 <sub>0</sub>	819.7	1.8
	6 <sub>1</sub>	7 <sub>2</sub>	843.2	1.2
	6 <sub>3</sub>	7 <sub>4</sub>	868.6	0.7
P				
	7 <sub>-1</sub>	6 <sub>-2</sub>	314.0	0.8
	7 <sub>-3</sub>	6 <sub>-4</sub>	324.7	0.9
	7 <sub>-5</sub>	6 <sub>-6</sub>	325.3	0.7
Q				
	7 <sub>-4</sub>	7 <sub>-5</sub>	547.6	0.8
	7 <sub>-5</sub>	7 <sub>-4</sub>	560.2	2.4
	7 <sub>-6</sub>	7 <sub>-7</sub>	573.1	2.3
	7 <sub>-7</sub>	7 <sub>-6</sub>	573.6	7.0
	7 <sub>-3</sub>	7 <sub>-2</sub>	576.7	0.8
R				
	7 <sub>-3</sub>	8 <sub>-2</sub>	777.2	1.1
	7 <sub>-5</sub>	8 <sub>-4</sub>	797.6	1.1
	7 <sub>-1</sub>	8 <sub>0</sub>	802.5	0.8
	7 <sub>-7</sub>	8 <sub>-6</sub>	836.3	1.1
	7 <sub>1</sub>	8 <sub>2</sub>	841.4	0.5
Q				
	8 <sub>-5</sub>	8 <sub>-6</sub>	534.6	1.2
	8 <sub>-7</sub>	8 <sub>-8</sub>	560.0	3.7
	8 <sub>-8</sub>	8 <sub>-7</sub>	560.3	1.2
R				
	8 <sub>-7</sub>	9 <sub>-6</sub>	860.3	0.5



## APPX III

TABLE III.1 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
Q	9 <sub>-7</sub>	9 <sub>-6</sub>	80521.9	0.6
	9 <sub>-8</sub>	9 <sub>-9</sub>	545.4	0.6
	9 <sub>-9</sub>	9 <sub>-8</sub>	545.5	1.8
Q	10 <sub>-9</sub>	10 <sub>-10</sub>	529.3	0.8

## APPX III

TABLE III.2

 $\tilde{D}^1A_1$  Transitions in  $H_2O$  Calculated for  $\langle \mu_z \rangle = 1$ 

(NO Electronic Interaction)

IDENTIFICATION			FREQUENCY	*RELATIVE INTENSITY
Branch	$J''_{\alpha''}$	$J'_{\alpha'}$	$\nu$ ( $cm^{-1}$ )	$[I]_{J'}^{J''} \times 10$
R	0 <sub>0</sub>	1 <sub>0</sub>	82097.5	3.3
P	1 <sub>0</sub>	0 <sub>0</sub>	2021.5	2.8
Q	1 <sub>1</sub>	1 <sub>-1</sub>	2037.5	12.2
	1 <sub>-1</sub>	1 <sub>1</sub>	2078.0	13.3
R	1 <sub>0</sub>	2 <sub>-2</sub>	2084.6	1.9
	1 <sub>-1</sub>	2 <sub>-1</sub>	2111.8	13.3
	1 <sub>1</sub>	2 <sub>1</sub>	2158.8	12.2
	1 <sub>0</sub>	2 <sub>2</sub>	2164.7	3.7
P	2 <sub>2</sub>	1 <sub>0</sub>	1960.9	2.1
	2 <sub>1</sub>	1 <sub>1</sub>	1966.5	7.7
	2 <sub>-1</sub>	1 <sub>-1</sub>	2000.4	10.2
	2 <sub>-2</sub>	1 <sub>0</sub>	2027.3	1.8
Q	2 <sub>1</sub>	2 <sub>-1</sub>	2000.3	4.3
	2 <sub>2</sub>	2 <sub>0</sub>	2012.0	2.1
	2 <sub>0</sub>	2 <sub>-2</sub>	2026.5	4.6
	2 <sub>-2</sub>	2 <sub>0</sub>	2078.4	4.9
	2 <sub>0</sub>	2 <sub>2</sub>	2106.6	2.3
	2 <sub>-1</sub>	2 <sub>1</sub>	2121.6	5.6
R	2 <sub>1</sub>	3 <sub>-1</sub>	2082.9	1.3

\*Values of  $[I]_{J'}^{J''} \times 10$  less than 0.5 are not included in this table.

## APPX III

TABLE III.2 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	2 <sub>-1</sub>	3 <sub>-3</sub>	82103.2	10.3
	2 <sub>-2</sub>	3 <sub>-2</sub>	2122.4	5.1
	2 <sub>0</sub>	3 <sub>0</sub>	2169.6	3.5
	2 <sub>-1</sub>	3 <sub>1</sub>	2188.7	7.7
	2 <sub>2</sub>	3 <sub>2</sub>	2227.1	4.1
	2 <sub>1</sub>	3 <sub>3</sub>	2228.5	12.4
P				
	3 <sub>3</sub>	2 <sub>1</sub>	1913.7	5.8
	3 <sub>2</sub>	2 <sub>-1</sub>	1914.5	2.0
	3 <sub>1</sub>	2 <sub>-1</sub>	1923.1	3.3
	3 <sub>0</sub>	2 <sub>0</sub>	1941.8	2.0
	3 <sub>-2</sub>	2 <sub>-2</sub>	1979.3	3.5
	3 <sub>-3</sub>	2 <sub>-1</sub>	1998.7	8.9
	3 <sub>-1</sub>	2 <sub>1</sub>	2027.6	1.3
Q				
	3 <sub>2</sub>	3 <sub>0</sub>	1977.6	0.8
	3 <sub>3</sub>	3 <sub>1</sub>	1980.7	2.7
	3 <sub>0</sub>	3 <sub>-2</sub>	1985.8	1.6
	3 <sub>1</sub>	3 <sub>-1</sub>	2005.7	9.3
	3 <sub>-1</sub>	3 <sub>-3</sub>	2009.2	11.0
	3 <sub>-3</sub>	3 <sub>-1</sub>	2081.3	11.1
	3 <sub>-1</sub>	3 <sub>1</sub>	2094.7	9.2
	3 <sub>-2</sub>	3 <sub>0</sub>	2122.5	2.1
	3 <sub>1</sub>	3 <sub>3</sub>	2151.2	3.5
	3 <sub>0</sub>	3 <sub>2</sub>	2157.0	1.2

## APPX III

TABLE III.2 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
R	$3_0$	$4_{-2}$	82103.4	0.8
	$3_{-2}$	$4_{-4}$	2119.2	4.2
	$3_{-3}$	$4_{-3}$	2130.8	15.2
	$3_{-1}$	$4_{-1}$	2175.7	8.4
	$3_{-2}$	$4_0$	2216.4	1.5
	$3_1$	$4_1$	2237.3	8.3
	$3_0$	$4_2$	2243.6	2.8
	$3_3$	$4_3$	2299.1	8.3
	$3_2$	$4_4$	2299.3	2.8
P	$4_4$	$3_2$	1869.0	1.0
	$4_3$	$3_3$	1869.1	3.0
	$4_2$	$3_0$	1879.0	1.1
	$4_1$	$3_1$	1883.7	3.6
	$4_{-1}$	$3_{-1}$	1917.3	4.4
	$4_{-3}$	$3_{-3}$	1957.7	9.6
	$4_{-4}$	$3_{-2}$	1970.1	3.2
	$4_{-2}$	$3_0$	1988.8	0.7
	$4_{-3}$	$3_1$	2043.2	0.8
Q	$4_3$	$4_1$	1955.2	1.0
	$4_1$	$4_{-1}$	1964.7	2.9
	$4_{-1}$	$4_{-3}$	1966.8	3.9
	$4_2$	$4_0$	1972.9	1.1
	$4_{-2}$	$4_{-4}$	1985.6	2.2

## APPX III

TABLE III.2 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	$4_0$	$4_{-2}$	81993.7	2.8
	$4_{-2}$	$4_0$	2082.7	2.6
	$4_{-4}$	$4_{-2}$	2087.8	2.2
	$4_{-3}$	$4_{-1}$	2124.2	5.2
	$4_0$	$4_2$	2133.9	1.3
	$4_{-1}$	$4_1$	2148.9	3.9
	$4_2$	$4_4$	2200.7	0.5
	$4_1$	$4_3$	2202.0	1.5
R	$4_1$	$5_{-1}$	2089.3	0.5
	$4_{-1}$	$5_{-3}$	2122.3	2.8
	$4_{-3}$	$5_{-5}$	2132.2	12.0
	$4_{-4}$	$5_{-4}$	2138.3	4.4
	$4_{-2}$	$5_{-2}$	2177.9	2.1
	$4_0$	$5_0$	2241.3	1.7
	$4_{-3}$	$5_{-1}$	2248.7	2.2
	$4_{-1}$	$5_1$	2258.8	5.1
	$4_2$	$5_2$	2308.4	1.7
	$4_1$	$5_3$	2309.8	5.1
	$4_4$	$5_4$	2375.4	1.3
	$4_3$	$5_5$	2375.4	3.9
P	$5_5$	$4_3$	1828.9	1.1
	$5_3$	$4_1$	1833.2	1.6
	$5_2$	$4_2$	1834.0	0.5

## APPX III

TABLE III.2 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	5 <sub>1</sub>	4 <sub>-1</sub>	81838.2	1.5
	5 <sub>0</sub>	4 <sub>0</sub>	1852.5	0.7
	5 <sub>-2</sub>	4 <sub>-2</sub>	1893.0	1.0
	5 <sub>-4</sub>	4 <sub>-4</sub>	1934.5	2.6
	5 <sub>-5</sub>	4 <sub>-3</sub>	1941.8	7.9
	5 <sub>-3</sub>	4 <sub>-1</sub>	1948.7	2.3
	5 <sub>-1</sub>	4 <sub>1</sub>	2001.9	0.5
Q	5 <sub>3</sub>	5 <sub>1</sub>	1943.1	1.0
	5 <sub>-2</sub>	5 <sub>-4</sub>	1943.6	0.8
	5 <sub>0</sub>	5 <sub>-2</sub>	1947.7	0.7
	5 <sub>-3</sub>	5 <sub>-5</sub>	1956.7	3.5
	5 <sub>1</sub>	5 <sub>-1</sub>	1962.7	3.1
	5 <sub>-1</sub>	5 <sub>-3</sub>	1975.3	5.7
	5 <sub>-3</sub>	5 <sub>-1</sub>	2073.2	5.0
	5 <sub>-5</sub>	5 <sub>-3</sub>	2097.3	3.6
	5 <sub>-1</sub>	5 <sub>1</sub>	2111.8	2.8
	5 <sub>-4</sub>	5 <sub>-2</sub>	2126.8	1.1
	5 <sub>-2</sub>	5 <sub>0</sub>	2140.7	1.0
	5 <sub>1</sub>	5 <sub>3</sub>	2183.2	1.5
	5 <sub>0</sub>	5 <sub>2</sub>	2188.1	0.5
	5 <sub>3</sub>	5 <sub>5</sub>	2253.4	0.5
R	5 <sub>-2</sub>	6 <sub>-4</sub>	2139.0	0.9
	5 <sub>-4</sub>	6 <sub>-6</sub>	2142.4	3.2

## APPX III

TABLE III.2 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	5 <sub>-5</sub>	6 <sub>-5</sub>	82145.4	9.8
	5 <sub>-3</sub>	6 <sub>-3</sub>	2177.7	4.3
	5 <sub>-1</sub>	6 <sub>-1</sub>	2239.4	2.7
	5 <sub>-2</sub>	6 <sub>0</sub>	2275.7	0.9
	5 <sub>1</sub>	6 <sub>1</sub>	2312.9	2.7
	5 <sub>0</sub>	6 <sub>2</sub>	2318.1	0.9
	5 <sub>-5</sub>	6 <sub>-1</sub>	2361.5	0.5
	5 <sub>3</sub>	6 <sub>3</sub>	2382.6	2.1
	5 <sub>2</sub>	6 <sub>4</sub>	2382.8	0.7
	5 <sub>5</sub>	6 <sub>5</sub>	2456.4	1.3
P				
	6 <sub>3</sub>	5 <sub>3</sub>	1790.7	0.5
	6 <sub>1</sub>	5 <sub>1</sub>	1796.5	0.8
	6 <sub>-1</sub>	5 <sub>-1</sub>	1821.9	1.0
	6 <sub>-3</sub>	5 <sub>-3</sub>	1868.8	1.9
	6 <sub>-4</sub>	5 <sub>-2</sub>	1909.0	0.6
	6 <sub>-5</sub>	5 <sub>-5</sub>	1909.2	5.3
	6 <sub>-6</sub>	5 <sub>-4</sub>	1913.1	1.8
Q				
	6 <sub>-3</sub>	6 <sub>-5</sub>	1916.9	1.4
	6 <sub>1</sub>	6 <sub>-1</sub>	1924.2	0.7
	6 <sub>-4</sub>	6 <sub>-6</sub>	1924.7	0.5
	6 <sub>-1</sub>	6 <sub>-3</sub>	1926.4	1.4
	6 <sub>0</sub>	6 <sub>-2</sub>	1948.3	0.7
	6 <sub>-2</sub>	6 <sub>-4</sub>	1950.6	1.0

## APPX III

TABLE III.2 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	6 <sub>-4</sub>	6 <sub>-2</sub>	82068.3	0.8
	6 <sub>-2</sub>	6 <sub>0</sub>	2087.3	0.6
	6 <sub>-6</sub>	6 <sub>-4</sub>	2108.5	0.6
	6 <sub>-5</sub>	6 <sub>-3</sub>	2130.2	1.9
	6 <sub>-3</sub>	6 <sub>-1</sub>	2132.9	1.8
	6 <sub>-1</sub>	6 <sub>1</sub>	2172.2	1.0
R				
	6 <sub>-5</sub>	7 <sub>-7</sub>	2150.2	6.4
	6 <sub>-6</sub>	7 <sub>-6</sub>	2151.6	2.2
	6 <sub>-3</sub>	7 <sub>-5</sub>	2152.6	2.0
	6 <sub>-4</sub>	7 <sub>-4</sub>	2176.9	0.9
	6 <sub>-2</sub>	7 <sub>-2</sub>	2232.8	0.5
	6 <sub>-3</sub>	7 <sub>-1</sub>	2296.3	1.1
	6 <sub>-1</sub>	7 <sub>1</sub>	2325.0	1.3
	6 <sub>1</sub>	7 <sub>3</sub>	2387.2	1.0
	6 <sub>3</sub>	7 <sub>5</sub>	2461.1	0.6
P				
	7 <sub>-5</sub>	6 <sub>-3</sub>	1871.1	1.2
	7 <sub>-6</sub>	6 <sub>-6</sub>	1881.7	1.1
	7 <sub>-7</sub>	6 <sub>-5</sub>	1883.7	3.3
Q				
	7 <sub>-5</sub>	7 <sub>-7</sub>	1891.2	0.7
	7 <sub>1</sub>	7 <sub>-1</sub>	1912.1	0.5
	7 <sub>-3</sub>	7 <sub>-5</sub>	1919.9	1.2
	7 <sub>-1</sub>	7 <sub>-3</sub>	1928.1	1.1



## APPX III

TABLE III.2 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	7 <sub>-3</sub>	7 <sub>-1</sub>	82063.7	0.9
	7 <sub>-5</sub>	7 <sub>-3</sub>	2068.6	1.0
	7 <sub>-7</sub>	7 <sub>-5</sub>	2119.4	0.9
R	7 <sub>-6</sub>	8 <sub>-8</sub>	2156.0	1.3
	7 <sub>-7</sub>	8 <sub>-7</sub>	2156.6	3.8
	7 <sub>-5</sub>	8 <sub>-5</sub>	2176.6	1.5
	7 <sub>-3</sub>	8 <sub>-3</sub>	2223.2	0.7
	7 <sub>-1</sub>	8 <sub>-1</sub>	2302.3	0.5
P	8 <sub>-5</sub>	7 <sub>-5</sub>	1817.7	0.6
	8 <sub>-7</sub>	7 <sub>-7</sub>	1852.1	1.8
	8 <sub>-8</sub>	7 <sub>-6</sub>	1853.0	0.6
Q	8 <sub>-7</sub>	8 <sub>-5</sub>	2137.5	0.5
R	8 <sub>-7</sub>	9 <sub>-9</sub>	2159.9	2.0
	8 <sub>-8</sub>	9 <sub>-8</sub>	2160.2	0.7
	8 <sub>-5</sub>	9 <sub>-7</sub>	2169.5	0.7
P	9 <sub>-9</sub>	8 <sub>-7</sub>	1821.0	0.9
R	9 <sub>-9</sub>	10 <sub>-9</sub>	2162.2	0.9

## APPENDIX III

TABLE III.3

$\tilde{C}^1B_1$  Transitions in  $D_2O$  Calculated for  $\langle\mu_x\rangle = 1$ .  
(No electronic interaction)

IDENTIFICATION			FREQUENCY	*RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
R	0 <sub>0</sub>	1 <sub>1</sub>	80772.8	6.7
P	1 <sub>1</sub>	0 <sub>0</sub>	729.2	3.0
Q	1 <sub>0</sub>	1 <sub>-1</sub>	742.4	9.1
	1 <sub>-1</sub>	1 <sub>0</sub>	758.8	4.7
R	1 <sub>1</sub>	2 <sub>-2</sub>	761.2	1.1
	1 <sub>-1</sub>	2 <sub>0</sub>	784.1	4.7
	1 <sub>1</sub>	2 <sub>2</sub>	798.8	4.9
	1 <sub>0</sub>	2 <sub>1</sub>	801.0	9.1
P	2 <sub>1</sub>	1 <sub>0</sub>	697.3	3.5
	2 <sub>2</sub>	1 <sub>1</sub>	698.7	7.8
	2 <sub>0</sub>	1 <sub>-1</sub>	713.3	7.8
	2 <sub>-2</sub>	1 <sub>1</sub>	737.0	1.8
Q	2 <sub>2</sub>	2 <sub>-1</sub>	716.4	2.5
	2 <sub>1</sub>	2 <sub>0</sub>	722.6	1.9
	2 <sub>-1</sub>	2 <sub>-2</sub>	741.8	7.4
	2 <sub>-2</sub>	2 <sub>-1</sub>	754.6	15.6
	2 <sub>0</sub>	2 <sub>1</sub>	771.9	4.4
	2 <sub>-1</sub>	2 <sub>2</sub>	779.4	1.6

\*Values of  $[I]_{J'}^{J''} \times 10$  less than 0.5 are not included in this table.

## APPX III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
R	$2_2$	$3_{-1}$	80756.6	1.1
	$2_0$	$3_{-3}$	765.6	2.9
	$2_{-2}$	$3_{-1}$	795.1	10.5
	$2_0$	$3_1$	805.5	11.1
	$2_{-1}$	$3_0$	811.3	4.5
	$2_2$	$3_3$	825.8	11.8
	$2_1$	$3_2$	826.3	5.9
P	$3_2$	$2_1$	664.3	7.9
	$3_3$	$2_2$	664.6	4.0
	$3_0$	$2_{-1}$	680.5	6.5
	$3_1$	$2_0$	684.0	4.2
	$3_{-1}$	$2_{-2}$	694.8	4.1
	$3_{-3}$	$2_0$	725.7	1.1
	$3_{-2}$	$2_1$	746.7	0.5
Q	$3_3$	$3_0$	696.5	1.1
	$3_2$	$3_1$	697.9	2.3
	$3_1$	$3_{-2}$	707.5	1.2
	$3_0$	$3_{-1}$	721.0	6.1
	$3_{-2}$	$3_{-3}$	740.4	19.8
	$3_{-3}$	$3_{-2}$	749.2	10.5
	$3_{-1}$	$3_0$	764.4	3.5

## APPX III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J', J''}^{J''} \times 10$
Branch	$J''_{\tau''}$	$J'_{\tau'}$		
R	3 <sub>-2</sub>	3 <sub>1</sub>	80780.3	3.6
	3 <sub>1</sub>	3 <sub>2</sub>	787.7	1.5
	3 <sub>0</sub>	3 <sub>3</sub>	789.9	2.9
	3 <sub>0</sub>	4 <sub>-3</sub>	748.4	0.8
	3 <sub>1</sub>	4 <sub>-2</sub>	764.8	1.2
	3 <sub>-1</sub>	4 <sub>-4</sub>	766.3	1.3
	3 <sub>-3</sub>	4 <sub>-2</sub>	806.6	4.8
	3 <sub>-1</sub>	4 <sub>0</sub>	811.0	5.8
	3 <sub>-2</sub>	4 <sub>-1</sub>	821.6	8.4
	3 <sub>1</sub>	4 <sub>2</sub>	831.3	5.4
	3 <sub>0</sub>	4 <sub>1</sub>	833.3	10.8
	3 <sub>2</sub>	4 <sub>3</sub>	851.0	11.0
	3 <sub>3</sub>	4 <sub>4</sub>	850.9	5.5
P	4 <sub>3</sub>	3 <sub>2</sub>	629.2	3.2
	4 <sub>4</sub>	3 <sub>3</sub>	629.3	6.3
	4 <sub>1</sub>	3 <sub>0</sub>	647.2	3.4
	4 <sub>2</sub>	3 <sub>1</sub>	648.2	7.0
	4 <sub>-1</sub>	3 <sub>-2</sub>	661.6	2.8
	4 <sub>0</sub>	3 <sub>-1</sub>	666.8	8.6
	4 <sub>-2</sub>	3 <sub>-3</sub>	673.7	7.2
	4 <sub>-2</sub>	3 <sub>1</sub>	713.6	1.4
	4 <sub>-4</sub>	3 <sub>-1</sub>	715.9	1.7

## APPX III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
Q	$4_4$	$4_1$	80672.7	1.4
	$4_3$	$4_2$	672.8	0.7
	$4_2$	$4_1$	689.6	2.8
	$4_1$	$4_0$	693.9	1.6
	$4_0$	$4_{-3}$	694.1	1.4
	$4_{-1}$	$4_{-2}$	719.0	3.7
	$4_{-3}$	$4_{-4}$	737.9	11.5
	$4_{-4}$	$4_{-3}$	743.3	24.0
	$4_{-2}$	$4_{-1}$	754.9	8.5
	$4_0$	$4_1$	779.1	4.1
	$4_{-3}$	$4_0$	782.6	1.4
	$4_{-1}$	$4_2$	785.4	2.0
	$4_2$	$4_3$	801.3	1.9
	$4_1$	$4_4$	801.7	1.0
R	$4_{-1}$	$5_{-4}$	748.2	0.5
	$4_2$	$5_{-1}$	750.9	0.9
	$4_{-2}$	$5_{-5}$	763.3	1.8
	$4_0$	$5_{-3}$	769.7	3.0
	$4_{-2}$	$5_{-1}$	816.3	11.0
	$4_{-4}$	$5_{-3}$	818.8	7.8
	$4_{-3}$	$5_{-2}$	831.7	3.6
	$4_0$	$5_1$	834.2	9.4
	$4_{-1}$	$5_0$	839.6	4.7

## APPX III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	$4_2$	$5_3$	80855.6	9.1
	$4_1$	$5_2$	856.0	4.6
	$4_4$	$5_5$	874.3	8.0
	$4_3$	$5_4$	874.3	4.0
P	$5_4$	$4_3$	592.6	4.0
	$5_5$	$4_4$	592.6	2.0
	$5_2$	$4_1$	611.0	5.0
	$5_3$	$4_2$	611.2	2.5
	$5_0$	$4_{-1}$	628.3	5.6
	$5_1$	$4_0$	630.7	3.0
	$5_{-2}$	$4_{-3}$	640.7	4.5
	$5_{-1}$	$4_{-2}$	646.9	3.8
	$5_{-3}$	$4_{-4}$	650.1	2.7
	$5_{-3}$	$4_0$	694.8	0.8
	$5_{-5}$	$4_{-2}$	707.8	0.6
	$5_{-2}$	$4_1$	725.7	0.5
	$5_{-4}$	$4_{-1}$	725.7	0.7
Q	$5_4$	$5_3$	646.9	0.7
	$5_3$	$5_0$	665.4	0.9
	$5_2$	$5_1$	666.1	1.8
	$5_1$	$5_{-2}$	679.8	1.1
	$5_0$	$5_{-1}$	689.6	3.3
	$5_{-2}$	$5_{-3}$	716.2	8.0

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	$5_{-4}$	$5_{-5}$	80734.1	23.5
	$5_{-5}$	$5_{-4}$	737.1	12.1
	$5_{-3}$	$5_{-2}$	743.9	4.6
	$5_{-1}$	$5_0$	767.5	2.1
	$5_{-2}$	$5_1$	780.8	3.8
	$5_{-4}$	$5_{-1}$	787.1	1.7
	$5_1$	$5_2$	792.8	1.3
	$5_0$	$5_3$	794.3	2.6
	$5_3$	$5_4$	812.6	0.5
	$5_2$	$5_5$	812.7	1.1
R	$5_0$	$6_{-3}$	744.4	0.8
	$5_{-2}$	$6_{-5}$	745.7	0.8
	$5_{-3}$	$6_{-6}$	757.2	0.6
	$5_1$	$6_{-2}$	757.6	0.7
	$5_{-1}$	$6_{-4}$	770.7	1.4
	$5_{-3}$	$6_{-2}$	821.8	4.5
	$5_{-5}$	$6_{-4}$	831.7	2.9
	$5_{-1}$	$6_0$	834.9	3.9
	$5_{-4}$	$6_{-3}$	841.8	5.8
	$5_{-2}$	$6_{-1}$	845.3	7.6
	$5_1$	$6_2$	858.2	3.6
	$5_0$	$6_1$	859.6	7.2
	$5_3$	$6_4$	877.7	3.1

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION		FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$ $J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
P	5 <sub>2</sub> 6 <sub>3</sub>	80877.8	6.2
	5 <sub>5</sub> 6 <sub>6</sub>	896.2	2.4
	5 <sub>4</sub> 6 <sub>5</sub>	896.2	4.8
	6 <sub>5</sub> 5 <sub>4</sub>	554.4	1.0
	6 <sub>6</sub> 5 <sub>5</sub>	554.4	2.0
	6 <sub>3</sub> 5 <sub>2</sub>	573.0	1.4
	6 <sub>4</sub> 5 <sub>3</sub>	573.0	2.9
	6 <sub>1</sub> 5 <sub>0</sub>	591.2	1.9
	6 <sub>2</sub> 5 <sub>1</sub>	591.7	3.8
	6 <sub>-1</sub> 5 <sub>-2</sub>	607.3	2.1
	6 <sub>0</sub> 5 <sub>-1</sub>	611.5	5.0
	6 <sub>-3</sub> 5 <sub>-4</sub>	617.9	1.7
	6 <sub>-2</sub> 5 <sub>-3</sub>	624.1	5.9
	6 <sub>-4</sub> 5 <sub>-5</sub>	624.5	3.8
	6 <sub>-4</sub> 5 <sub>-1</sub>	677.4	1.3
	6 <sub>-2</sub> 5 <sub>1</sub>	688.7	0.6
	6 <sub>-6</sub> 5 <sub>-3</sub>	701.1	0.7
Q	6 <sub>4</sub> 6 <sub>1</sub>	638.3	0.9
	6 <sub>2</sub> 6 <sub>-1</sub>	656.2	1.6
	6 <sub>1</sub> 6 <sub>0</sub>	658.6	0.8
	6 <sub>0</sub> 6 <sub>-3</sub>	666.2	1.4
	6 <sub>-1</sub> 6 <sub>-2</sub>	685.1	1.5
	6 <sub>-3</sub> 6 <sub>-4</sub>	712.5	4.0
	6 <sub>-5</sub> 6 <sub>-6</sub>	729.0	10.8



## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	6 <sub>-6</sub>	6 <sub>-5</sub>	80730.5	21.9
	6 <sub>-4</sub>	6 <sub>-3</sub>	732.2	9.0
	6 <sub>-2</sub>	6 <sub>-1</sub>	753.2	3.8
	6 <sub>-3</sub>	6 <sub>0</sub>	776.8	1.4
	6 <sub>0</sub>	6 <sub>1</sub>	781.5	2.4
	6 <sub>-1</sub>	6 <sub>2</sub>	785.7	1.2
	6 <sub>-5</sub>	6 <sub>-2</sub>	793.6	0.5
	6 <sub>2</sub>	6 <sub>3</sub>	803.3	1.4
	6 <sub>1</sub>	6 <sub>4</sub>	803.5	0.7
	6 <sub>4</sub>	6 <sub>5</sub>	822.3	0.5
R	6 <sub>2</sub>	7 <sub>-1</sub>	737.2	0.5
	6 <sub>-4</sub>	7 <sub>-7</sub>	748.9	0.8
	6 <sub>0</sub>	7 <sub>-3</sub>	762.3	1.5
	6 <sub>-2</sub>	7 <sub>-5</sub>	767.6	2.1
	6 <sub>-4</sub>	7 <sub>-3</sub>	828.2	6.5
	6 <sub>-2</sub>	7 <sub>-1</sub>	834.2	6.2
	6 <sub>-6</sub>	7 <sub>-5</sub>	844.6	4.3
	6 <sub>-3</sub>	7 <sub>-2</sub>	850.8	2.8
	6 <sub>-5</sub>	7 <sub>-4</sub>	851.8	2.2
	6 <sub>0</sub>	7 <sub>1</sub>	858.2	5.2
	6 <sub>-1</sub>	7 <sub>0</sub>	862.0	2.7
	6 <sub>2</sub>	7 <sub>3</sub>	879.4	4.5
	6 <sub>1</sub>	7 <sub>2</sub>	879.7	2.3
	6 <sub>4</sub>	7 <sub>5</sub>	898.2	3.5

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	$6_3$	$7_4$	80898.2	1.7
	$6_6$	$7_7$	916.6	2.4
	$6_5$	$7_6$	916.6	1.2
P	$7_6$	$6_5$	514.8	0.9
	$7_4$	$6_3$	533.4	1.4
	$7_5$	$6_4$	533.4	0.7
	$7_2$	$6_1$	551.8	2.0
	$7_3$	$6_2$	551.8	1.0
	$7_0$	$6_{-1}$	569.5	2.7
	$7_1$	$6_0$	570.8	1.4
	$7_{-2}$	$6_{-3}$	584.3	3.0
	$7_{-1}$	$6_{-2}$	589.9	1.9
	$7_{-4}$	$6_{-5}$	593.5	2.3
	$7_{-5}$	$6_{-6}$	597.6	1.3
	$7_{-3}$	$6_{-4}$	598.6	2.0
Q	$7_2$	$7_1$	628.6	0.8
	$7_1$	$7_{-2}$	644.8	0.6
	$7_0$	$7_{-1}$	650.6	1.3
	$7_{-2}$	$7_{-3}$	680.3	2.6
	$7_{-4}$	$7_{-5}$	707.6	7.2
	$7_{-5}$	$7_{-4}$	720.4	4.0
	$7_{-6}$	$7_{-7}$	722.7	18.1
	$7_{-7}$	$7_{-6}$	723.5	9.1
	$7_{-3}$	$7_{-2}$	736.9	1.6

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	$7_{-1}$	$7_0$	766.8	1.0
	$7_{-4}$	$7_{-1}$	774.3	1.8
	$7_{-2}$	$7_1$	776.3	2.0
	$7_1$	$7_2$	791.9	0.6
	$7_0$	$7_3$	792.8	1.3
	$7_{-6}$	$7_{-3}$	802.0	0.5
	$7_2$	$7_5$	811.7	0.6
R	$7_{-2}$	$8_{-5}$	739.8	0.6
	$7_{-3}$	$8_{-6}$	760.5	0.6
	$7_{-1}$	$8_{-4}$	763.7	0.7
	$7_{-3}$	$8_{-2}$	833.2	2.2
	$7_{-5}$	$8_{-4}$	835.9	2.1
	$7_{-1}$	$8_0$	855.4	1.8
	$7_{-4}$	$8_{-3}$	856.2	4.0
	$7_{-7}$	$8_{-6}$	856.9	1.5
	$7_{-6}$	$8_{-5}$	861.5	3.1
	$7_{-2}$	$8_{-1}$	863.5	3.8
	$7_1$	$8_2$	879.2	1.5
	$7_0$	$8_1$	880.0	3.1
	$7_3$	$8_4$	898.6	1.2
	$7_2$	$8_3$	898.6	2.3
	$7_5$	$8_6$	917.2	0.8
	$7_4$	$8_5$	917.2	1.6
	$7_7$	$8_8$	935.6	0.5

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
P	7 <sub>6</sub>	8 <sub>7</sub>	80935.6	1.0
	8 <sub>6</sub>	7 <sub>5</sub>	492.3	0.6
	8 <sub>4</sub>	7 <sub>3</sub>	510.8	0.9
	8 <sub>1</sub>	7 <sub>0</sub>	529.0	0.7
	8 <sub>2</sub>	7 <sub>1</sub>	529.2	1.3
	8 <sub>-1</sub>	7 <sub>-2</sub>	546.1	0.9
	8 <sub>0</sub>	7 <sub>-1</sub>	548.5	1.9
	8 <sub>-3</sub>	7 <sub>-4</sub>	559.3	1.0
	8 <sub>-2</sub>	7 <sub>-3</sub>	565.5	2.6
	8 <sub>-5</sub>	7 <sub>-6</sub>	567.8	0.8
	8 <sub>-6</sub>	7 <sub>-7</sub>	570.0	1.6
	8 <sub>-4</sub>	7 <sub>-5</sub>	570.6	2.5
	8 <sub>-4</sub>	7 <sub>-1</sub>	637.3	0.5
	8 <sub>-6</sub>	7 <sub>-3</sub>	649.3	0.5
Q	8 <sub>2</sub>	8 <sub>-1</sub>	616.4	0.5
	8 <sub>0</sub>	8 <sub>-3</sub>	630.4	0.7
	8 <sub>-1</sub>	8 <sub>-2</sub>	642.4	0.5
	8 <sub>-3</sub>	8 <sub>-4</sub>	674.9	1.0
	8 <sub>-5</sub>	8 <sub>-6</sub>	701.2	3.0
	8 <sub>-6</sub>	8 <sub>-5</sub>	708.8	6.4
	8 <sub>-7</sub>	8 <sub>-8</sub>	715.4	7.0
	8 <sub>-8</sub>	8 <sub>-7</sub>	715.7	14.2

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	8 <sub>-4</sub>	8 <sub>-3</sub>	719.2	2.6
	8 <sub>-2</sub>	8 <sub>-1</sub>	748.8	1.4
	8 <sub>-3</sub>	8 <sub>0</sub>	766.6	0.7
	8 <sub>-5</sub>	8 <sub>-2</sub>	773.9	0.5
	8 <sub>0</sub>	8 <sub>1</sub>	777.9	0.9
	8 <sub>-1</sub>	8 <sub>2</sub>	780.4	0.5
	8 <sub>2</sub>	8 <sub>3</sub>	799.3	0.5
R	8 <sub>0</sub>	9 <sub>-3</sub>	744.0	0.5
	8 <sub>-4</sub>	9 <sub>-7</sub>	750.0	0.7
	8 <sub>-2</sub>	9 <sub>-5</sub>	761.1	1.1
	8 <sub>-4</sub>	9 <sub>-3</sub>	832.8	2.9
	8 <sub>-6</sub>	9 <sub>-5</sub>	844.9	2.6
	8 <sub>-2</sub>	9 <sub>-1</sub>	850.0	2.3
	8 <sub>-5</sub>	9 <sub>-4</sub>	861.5	1.3
	8 <sub>-3</sub>	9 <sub>-2</sub>	864.4	1.2
	8 <sub>-8</sub>	9 <sub>-7</sub>	868.1	2.1
	8 <sub>-7</sub>	9 <sub>-6</sub>	870.9	1.0
	8 <sub>0</sub>	9 <sub>1</sub>	876.5	1.9
	8 <sub>-1</sub>	9 <sub>0</sub>	878.8	1.0
	8 <sub>2</sub>	9 <sub>3</sub>	897.3	1.5
	8 <sub>1</sub>	9 <sub>2</sub>	897.4	0.7
	8 <sub>4</sub>	9 <sub>5</sub>	916.2	1.0
	8 <sub>3</sub>	9 <sub>4</sub>	916.2	0.5

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
P	8 <sub>6</sub>	9 <sub>7</sub>	80934.7	0.6
	9 <sub>2</sub>	8 <sub>1</sub>	486.6	0.5
	9 <sub>0</sub>	8 <sub>-1</sub>	504.5	0.8
	9 <sub>-2</sub>	8 <sub>-3</sub>	520.7	1.1
	9 <sub>-1</sub>	8 <sub>-2</sub>	524.5	0.6
	9 <sub>-4</sub>	8 <sub>-5</sub>	532.6	1.2
	9 <sub>-3</sub>	8 <sub>-4</sub>	538.3	0.8
	9 <sub>-5</sub>	8 <sub>-6</sub>	540.7	0.7
	9 <sub>-6</sub>	8 <sub>-7</sub>	540.8	0.9
	9 <sub>-7</sub>	8 <sub>-8</sub>	541.9	0.5
Q	9 <sub>-2</sub>	9 <sub>-3</sub>	634.3	0.6
	9 <sub>-4</sub>	9 <sub>-5</sub>	668.7	1.6
	9 <sub>-6</sub>	9 <sub>-7</sub>	693.2	4.5
	9 <sub>-7</sub>	9 <sub>-6</sub>	697.4	2.3
	9 <sub>-5</sub>	9 <sub>-4</sub>	701.1	1.0
	9 <sub>-8</sub>	9 <sub>-9</sub>	701.1	10.2
	9 <sub>-9</sub>	9 <sub>-8</sub>	707.3	5.1
	9 <sub>-3</sub>	9 <sub>-2</sub>	727.8	0.5
	9 <sub>-4</sub>	9 <sub>-1</sub>	757.5	0.8
	9 <sub>-2</sub>	9 <sub>1</sub>	766.8	0.7
	9 <sub>-6</sub>	9 <sub>-3</sub>	775.9	0.5
R	9 <sub>-5</sub>	10 <sub>-4</sub>	833.8	0.9

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	9 <sub>-3</sub>	10 <sub>-2</sub>	80842.8	0.7
	9 <sub>-7</sub>	10 <sub>-6</sub>	854.4	0.8
	9 <sub>-4</sub>	10 <sub>-3</sub>	864.9	1.5
	9 <sub>-6</sub>	10 <sub>-5</sub>	866.9	1.6
	9 <sub>-1</sub>	10 <sub>0</sub>	871.0	0.6
	9 <sub>-2</sub>	10 <sub>-1</sub>	876.4	1.2
	9 <sub>-9</sub>	10 <sub>-8</sub>	878.2	0.7
	9 <sub>-8</sub>	10 <sub>-7</sub>	879.7	1.3
	9 <sub>0</sub>	10 <sub>1</sub>	894.5	0.9
	9 <sub>2</sub>	10 <sub>3</sub>	913.5	0.6
P	10 <sub>0</sub>	9 <sub>-1</sub>	479.3	0.5
	10 <sub>-2</sub>	9 <sub>-3</sub>	498.1	0.8
	10 <sub>-4</sub>	9 <sub>-5</sub>	508.4	0.9
	10 <sub>-6</sub>	9 <sub>-7</sub>	509.5	0.8
	10 <sub>-8</sub>	9 <sub>-9</sub>	513.3	0.6
Q	10 <sub>-5</sub>	10 <sub>-6</sub>	661.2	0.6
	10 <sub>-6</sub>	10 <sub>-5</sub>	683.3	1.4
	10 <sub>-7</sub>	10 <sub>-8</sub>	683.7	1.5
	10 <sub>-8</sub>	10 <sub>-7</sub>	685.9	3.2
	10 <sub>-9</sub>	10 <sub>-10</sub>	697.9	3.5
	10 <sub>-10</sub>	10 <sub>-9</sub>	698.0	7.0
	10 <sub>-4</sub>	10 <sub>-3</sub>	704.7	0.6

## APPX. III

TABLE III.3 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
R	$10_{-4}$	$11_{-3}$	80835.3	0.8
	$10_{-6}$	$11_{-5}$	836.7	0.9
	$10_{-2}$	$11_{-1}$	862.3	0.6
	$10_{-8}$	$11_{-7}$	863.6	0.9
	$10_{-7}$	$11_{-6}$	972.2	0.5
	$10_{-10}$	$11_{-9}$	887.1	0.8
	$10_0$	$11_1$	888.6	0.5



## APPX. III

## TABLE III.4

 $\tilde{D}^1A_1$  Transitions in  $D_2O$  Calculated for  $\langle \mu_z \rangle = 1$ 

(No Electronic Interaction)

IDENTIFICATION			FREQUENCY	*RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
R	0 <sub>0</sub>	1 <sub>0</sub>	82095.3	6.7
P	1 <sub>0</sub>	0 <sub>0</sub>	2054.7	6.0
Q	1 <sub>1</sub>	1 <sub>-1</sub>	2063.0	4.5
	1 <sub>-1</sub>	1 <sub>1</sub>	2085.2	4.7
R	1 <sub>0</sub>	2 <sub>-2</sub>	2086.6	3.9
	1 <sub>-1</sub>	2 <sub>-1</sub>	2102.7	4.7
	1 <sub>1</sub>	2 <sub>1</sub>	2127.2	4.5
	1 <sub>0</sub>	2 <sub>2</sub>	2129.9	8.2
P	2 <sub>2</sub>	1 <sub>0</sub>	2021.2	6.0
	2 <sub>1</sub>	1 <sub>1</sub>	2023.7	3.5
	2 <sub>-1</sub>	1 <sub>-1</sub>	2043.6	4.1
	2 <sub>-2</sub>	1 <sub>0</sub>	2059.4	3.9
Q	2 <sub>1</sub>	2 <sub>-1</sub>	2041.2	1.9
	2 <sub>2</sub>	2 <sub>0</sub>	2046.7	5.4
	2 <sub>0</sub>	2 <sub>-2</sub>	2057.5	11.8
	2 <sub>-2</sub>	2 <sub>0</sub>	2084.9	12.1
	2 <sub>0</sub>	2 <sub>2</sub>	2100.8	5.6
	2 <sub>-1</sub>	2 <sub>1</sub>	2107.8	2.3

\*Values of  $[I]_{J'}^{J''} \times 10$  less than 0.5 are not included in this table.

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
R				
	$2_2$	$3_{-2}$	82069.8	0.5
	$2_1$	$3_{-1}$	2082.1	0.5
	$2_{-1}$	$3_{-3}$	2095.9	3.9
	$2_{-2}$	$3_{-2}$	2108.0	11.9
	$2_0$	$3_0$	2132.8	8.7
	$2_{-1}$	$3_1$	2141.4	3.3
	$2_2$	$3_2$	2161.6	11.3
	$2_1$	$3_3$	2162.1	5.6
P				
	$3_3$	$2_1$	1993.0	3.7
	$3_2$	$2_2$	1993.3	7.5
	$3_1$	$2_{-1}$	2002.6	2.0
	$3_0$	$2_0$	2010.8	6.5
	$3_{-2}$	$2_{-2}$	2032.3	9.7
	$3_{-3}$	$2_{-1}$	2044.3	3.8
	$3_{-1}$	$2_1$	2060.9	0.6
	$3_{-2}$	$2_2$	2075.6	0.7
Q				
	$3_2$	$3_0$	2025.2	3.1
	$3_3$	$3_1$	2026.5	1.6
	$3_0$	$3_{-2}$	2033.9	5.3
	$3_1$	$3_{-1}$	2043.5	4.7
	$3_{-1}$	$3_{-3}$	2049.0	5.8
	$3_{-3}$	$3_{-1}$	2085.3	5.7

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION		FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$ $J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
R	$3_{-1}$ $3_1$	82094.4	4.5
	$3_{-2}$ $3_0$	2107.6	6.1
	$3_1$ $3_3$	2123.5	1.9
	$3_0$ $3_2$	2125.7	3.8
	$3_0$ $4_{-2}$	2092.0	2.3
	$3_{-2}$ $4_{-4}$	2104.0	11.2
	$3_{-3}$ $4_{-3}$	2111.9	6.9
	$3_{-1}$ $4_{-1}$	2135.8	4.2
	$3_{-2}$ $4_0$	2154.1	4.6
	$3_1$ $4_1$	2166.9	4.6
P	$3_0$ $4_2$	2169.3	9.3
	$3_3$ $4_3$	2196.7	5.3
	$3_2$ $4_4$	2196.7	10.6
	$4_4$ $3_2$	1965.0	6.0
	$4_3$ $3_3$	1965.1	3.0
	$4_2$ $3_0$	1975.6	5.5
	$4_1$ $3_1$	1977.3	2.9
	$4_0$ $3_{-2}$	1979.7	2.2
	$4_{-1}$ $3_{-1}$	1997.6	2.0
	$4_{-3}$ $3_{-3}$	2020.6	5.3
	$4_{-4}$ $3_{-2}$	2028.8	10.1
	$4_{-2}$ $3_0$	2040.9	2.4

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
Q	$4_{-3}$	$3_1$	82066.0	0.5
	$4_0$	$3_2$	2071.5	0.5
	$4_3$	$4_1$	2008.5	0.9
	$4_4$	$4_2$	2008.6	1.9
	$4_1$	$4_{-1}$	2018.7	2.3
	$4_2$	$4_0$	2022.1	5.0
	$4_{-1}$	$4_{-3}$	2024.3	2.7
	$4_{-2}$	$4_{-4}$	2037.3	9.4
	$4_0$	$4_{-2}$	2037.8	11.3
	$4_{-4}$	$4_{-2}$	2086.9	8.8
	$4_{-2}$	$4_0$	2087.4	10.3
	$4_{-3}$	$4_{-1}$	2107.5	3.1
	$4_0$	$4_2$	2115.1	5.2
	$4_{-1}$	$4_1$	2121.0	2.6
	$4_2$	$4_4$	2147.1	2.4
	$4_1$	$4_3$	2147.4	1.2
R	$4_2$	$5_{-2}$	2071.4	0.5
	$4_{-1}$	$5_{-3}$	2101.1	1.7
	$4_{-3}$	$5_{-5}$	2110.4	6.5
	$4_{-4}$	$5_{-4}$	2115.1	14.5
	$4_{-2}$	$5_{-2}$	2136.7	7.8

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	4 <sub>-3</sub>	5 <sub>-1</sub>	82168.6	1.4
	4 <sub>0</sub>	5 <sub>0</sub>	2169.3	7.2
	4 <sub>-1</sub>	5 <sub>1</sub>	2176.1	3.6
	4 <sub>2</sub>	5 <sub>2</sub>	2201.3	8.2
	4 <sub>1</sub>	5 <sub>3</sub>	2201.7	4.1
	4 <sub>-4</sub>	5 <sub>0</sub>	2218.4	0.5
	4 <sub>4</sub>	5 <sub>4</sub>	2232.9	7.8
	4 <sub>3</sub>	5 <sub>5</sub>	2232.9	3.9
P	5 <sub>5</sub>	4 <sub>3</sub>	1938.3	1.9
	5 <sub>4</sub>	4 <sub>4</sub>	1938.3	3.8
	5 <sub>3</sub>	4 <sub>1</sub>	1946.8	2.2
	5 <sub>2</sub>	4 <sub>2</sub>	1947.0	4.4
	5 <sub>-1</sub>	4 <sub>-3</sub>	1952.2	0.5
	5 <sub>1</sub>	4 <sub>-1</sub>	1955.5	1.8
	5 <sub>0</sub>	4 <sub>0</sub>	1960.8	4.3
	5 <sub>-2</sub>	4 <sub>-2</sub>	1984.3	5.2
	5 <sub>-4</sub>	4 <sub>-4</sub>	2008.1	10.7
	5 <sub>-5</sub>	4 <sub>-3</sub>	2013.2	5.4
	5 <sub>-3</sub>	4 <sub>-1</sub>	2019.6	1.7
	5 <sub>-4</sub>	4 <sub>0</sub>	2058.2	0.8
	5 <sub>-2</sub>	4 <sub>2</sub>	2061.6	0.8
Q	5 <sub>4</sub>	5 <sub>2</sub>	1992.6	0.9

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu(\text{cm}^{-1})$	$[I]_{J'}^{J''} \times 10$
	$5_5$	$5_3$	81992.6	0.5
	$5_2$	$5_0$	2001.2	2.6
	$5_3$	$5_1$	2001.8	1.3
	$5_0$	$5_{-2}$	2010.1	4.7
	$5_{-2}$	$5_{-4}$	2012.5	4.6
	$5_1$	$5_{-1}$	2016.7	3.0
	$5_{-3}$	$5_{-5}$	2022.6	3.4
	$5_{-1}$	$5_{-3}$	2029.0	5.4
	$5_{-3}$	$5_{-1}$	2080.8	4.7
	$5_{-5}$	$5_{-3}$	2090.0	3.1
	$5_{-1}$	$5_1$	2104.0	2.7
	$5_{-4}$	$5_{-2}$	2107.5	5.3
	$5_{-2}$	$5_0$	2115.9	5.3
	$5_1$	$5_3$	2138.3	1.6
	$5_0$	$5_2$	2140.0	3.2
	$5_3$	$5_5$	2171.2	0.7
	$5_2$	$5_4$	2171.2	1.3
R	$5_0$	$6_{-2}$	2087.8	1.0
	$5_{-2}$	$6_{-4}$	2109.0	4.1
	$5_{-4}$	$6_{-6}$	2115.3	13.2
	$5_{-5}$	$6_{-5}$	2117.9	6.9

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	5 <sub>-3</sub>	6 <sub>-3</sub>	82135.9	3.5
	5 <sub>-1</sub>	6 <sub>-1</sub>	2168.7	2.7
	5 <sub>-4</sub>	6 <sub>-2</sub>	2185.3	1.7
	5 <sub>-2</sub>	6 <sub>0</sub>	2183.0	5.1
	5 <sub>1</sub>	6 <sub>1</sub>	2203.9	3.0
	5 <sub>0</sub>	6 <sub>2</sub>	2205.4	6.1
	5 <sub>3</sub>	6 <sub>3</sub>	2236.3	2.9
	5 <sub>2</sub>	6 <sub>4</sub>	2236.3	5.7
	5 <sub>5</sub>	6 <sub>5</sub>	2270.4	2.4
	5 <sub>4</sub>	6 <sub>6</sub>	2270.4	4.7
P	6 <sub>4</sub>	5 <sub>2</sub>	1918.7	2.6
	6 <sub>3</sub>	5 <sub>3</sub>	1918.7	1.3
	6 <sub>6</sub>	5 <sub>4</sub>	1913.0	2.0
	6 <sub>5</sub>	5 <sub>5</sub>	1913.0	1.0
	6 <sub>2</sub>	5 <sub>0</sub>	1926.7	2.9
	6 <sub>1</sub>	5 <sub>1</sub>	1927.6	1.5
	6 <sub>0</sub>	5 <sub>-2</sub>	1931.9	2.1
	6 <sub>-1</sub>	5 <sub>-1</sub>	1944.2	1.6
	6 <sub>-3</sub>	5 <sub>-3</sub>	1970.8	2.2
	6 <sub>-5</sub>	5 <sub>-5</sub>	1994.4	5.0
	6 <sub>-6</sub>	5 <sub>-4</sub>	1997.4	10.2
	6 <sub>-4</sub>	5 <sub>-2</sub>	1997.9	3.8

## APPEX III

TABLE III.4 (Continued)

IDENTIFICATION		FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$ $J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
Q	$6_{-2}$ $5_0$	82023.7	1.1
	$6_{-3}$ $5_1$	2045.8	0.5
	$6_3$ $6_1$	1984.0	0.6
	$6_4$ $6_2$	1984.1	1.2
	$6_1$ $6_{-1}$	1992.3	1.3
	$6_2$ $6_0$	1993.9	2.8
	$6_{-3}$ $6_{-5}$	1998.7	1.8
	$6_{-1}$ $6_{-3}$	1999.3	2.1
	$6_{-4}$ $6_{-6}$	2005.7	4.4
	$6_0$ $6_{-2}$	2009.7	6.0
	$6_{-2}$ $6_{-4}$	2016.9	8.5
	$6_{-4}$ $6_{-2}$	2075.6	7.0
	$6_{-2}$ $6_0$	2090.9	4.9
	$6_{-6}$ $6_{-4}$	2093.9	4.2
	$6_{-5}$ $6_{-3}$	2107.7	2.0
	$6_{-3}$ $6_{-1}$	2110.5	2.2
	$6_0$ $6_2$	2127.3	3.0
	$6_{-1}$ $6_1$	2131.3	1.6
	$6_2$ $6_4$	2161.8	1.7
	$6_1$ $6_3$	2162.1	0.8
R	$6_4$ $6_6$	2196.5	0.6
	$6_{-1}$ $7_{-3}$	2095.4	0.6



## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION		FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$ $J'_{\tau'}$	$\nu$ ( $\text{cm}^{-1}$ )	$[I]_{J'}^{J''} \times 10$
	$6_{-3}$ $7_{-5}$	82115.5	2.2
	$6_{-5}$ $7_{-7}$	2118.8	6.0
	$6_{-6}$ $7_{-6}$	2120.1	12.2
	$6_{-4}$ $7_{-4}$	2134.2	6.1
	$6_{-2}$ $7_{-2}$	2165.3	3.9
	$6_{-3}$ $7_{-1}$	2191.1	1.6
	$6_0$ $7_0$	2203.6	4.1
	$6_{-5}$ $7_{-3}$	2203.9	0.5
	$6_{-1}$ $7_1$	2208.0	2.1
	$6_{-6}$ $7_{-2}$	2242.3	0.5
	$6_2$ $7_2$	2238.0	4.0
	$6_1$ $7_3$	2238.2	2.0
	$6_4$ $7_4$	2272.4	3.3
	$6_3$ $7_5$	2272.4	1.6
	$6_5$ $7_7$	2309.3	1.2
	$6_6$ $7_6$	2309.3	2.4
P	$7_6$ $6_6$	1889.0	0.9
	$7_5$ $6_3$	1891.9	0.6
	$7_4$ $6_4$	1891.9	1.3
	$7_3$ $6_1$	1897.5	0.8
	$7_2$ $6_2$	1897.6	1.7
	$7_{-1}$ $6_{-3}$	1904.0	0.5

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu(\text{cm}^{-1})$	$[I]_{J'}^{J''} \times 10$
	$7_1$	$6_1$	81904.5	0.9
	$7_0$	$6_0$	1907.2	1.9
	$7_{-2}$	$6_{-2}$	1927.7	2.1
	$7_{-4}$	$6_{-4}$	1956.9	3.7
	$7_{-5}$	$6_{-3}$	1976.3	1.8
	$7_{-6}$	$6_{-6}$	1979.5	8.5
	$7_{-7}$	$6_{-5}$	1981.1	4.3
	$7_{-3}$	$6_{-1}$	1996.6	0.6
	$7_{-4}$	$6_0$	2030.9	0.8
	$7_{-2}$	$6_2$	2045.3	0.5
Q	$7_4$	$7_2$	1968.0	0.5
	$7_2$	$7_{-6}$	1973.9	1.2
	$7_3$	$7_1$	1974.2	0.6
	$7_0$	$7_{-2}$	1981.6	2.3
	$7_{-4}$	$7_{-6}$	1983.1	2.5
	$7_1$	$7_{-1}$	1985.0	1.3
	$7_{-2}$	$7_2$	1986.2	3.2
	$7_{-5}$	$7_{-7}$	1987.4	1.4
	$7_{-1}$	$7_{-3}$	2000.1	2.6
	$7_{-3}$	$7_{-5}$	2001.6	2.9
	$7_{-5}$	$7_{-3}$	2072.4	2.2
	$7_{-3}$	$7_{-1}$	2077.1	1.9

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	7 <sub>-7</sub>	7 <sub>-5</sub>	82097.9	1.4
	7 <sub>-4</sub>	7 <sub>-2</sub>	2105.3	3.4
	7 <sub>-6</sub>	7 <sub>-4</sub>	2108.0	2.9
	7 <sub>-1</sub>	7 <sub>1</sub>	2112.8	1.2
	7 <sub>-2</sub>	7 <sub>-6</sub>	2121.7	2.5
	7 <sub>1</sub>	7 <sub>3</sub>	2150.4	0.8
	7 <sub>0</sub>	7 <sub>2</sub>	2151.3	1.5
	7 <sub>2</sub>	7 <sub>6</sub>	2185.9	0.7
R	7 <sub>-2</sub>	8 <sub>-4</sub>	2102.3	1.1
	7 <sub>-4</sub>	8 <sub>-6</sub>	2120.3	4.0
	7 <sub>-6</sub>	8 <sub>-8</sub>	2121.1	9.9
	7 <sub>-7</sub>	8 <sub>-7</sub>	2121.7	5.0
	7 <sub>-5</sub>	8 <sub>-5</sub>	2132.1	2.5
	7 <sub>-3</sub>	8 <sub>-3</sub>	2159.7	1.4
	7 <sub>-1</sub>	8 <sub>-1</sub>	2200.1	1.3
	7 <sub>-4</sub>	8 <sub>-2</sub>	2200.9	1.8
	7 <sub>-2</sub>	8 <sub>0</sub>	2210.0	2.7
	7 <sub>-6</sub>	8 <sub>-4</sub>	2224.0	0.5
	7 <sub>1</sub>	8 <sub>1</sub>	2237.6	1.3
	7 <sub>0</sub>	8 <sub>2</sub>	2238.5	2.6
	7 <sub>3</sub>	8 <sub>3</sub>	2272.8	1.1
	7 <sub>2</sub>	8 <sub>4</sub>	2272.8	2.1

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION			FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$	$J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
P	7 <sub>5</sub>	8 <sub>5</sub>	82309.9	0.8
	7 <sub>4</sub>	8 <sub>6</sub>	2309.9	1.5
	7 <sub>7</sub>	8 <sub>7</sub>	2349.6	0.5
	7 <sub>6</sub>	8 <sub>8</sub>	2349.6	1.0
	8 <sub>6</sub>	7 <sub>4</sub>	1866.5	0.5
	8 <sub>4</sub>	7 <sub>2</sub>	1869.3	0.8
	8 <sub>2</sub>	7 <sub>0</sub>	1874.6	1.0
	8 <sub>1</sub>	7 <sub>1</sub>	1875.0	0.5
	8 <sub>0</sub>	7 <sub>-2</sub>	1879.5	1.0
	8 <sub>-1</sub>	7 <sub>-1</sub>	1886.3	0.6
	8 <sub>-3</sub>	7 <sub>-3</sub>	1911.4	0.7
	8 <sub>-5</sub>	7 <sub>-5</sub>	1942.3	1.5
	8 <sub>-6</sub>	7 <sub>-4</sub>	1955.3	3.1
	8 <sub>-7</sub>	7 <sub>-7</sub>	1963.4	3.3
	8 <sub>-8</sub>	7 <sub>-6</sub>	1964.2	6.7
	8 <sub>-4</sub>	7 <sub>-2</sub>	1968.3	1.1
Q	8 <sub>4</sub>	8 <sub>2</sub>	1956.5	0.5
	8 <sub>1</sub>	8 <sub>-1</sub>	1962.3	0.5
	8 <sub>2</sub>	8 <sub>0</sub>	1962.9	1.0
	8 <sub>-5</sub>	8 <sub>-7</sub>	1966.0	0.8
	8 <sub>-6</sub>	8 <sub>-8</sub>	1968.4	1.7
	8 <sub>-1</sub>	8 <sub>-3</sub>	1968.9	0.9

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION		FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$ $J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_{J'}^{J''} \times 10$
	8 <sub>-3</sub> 8 <sub>-5</sub>	81971.1	1.1
	8 <sub>0</sub> 8 <sub>-2</sub>	1975.1	2.1
	8 <sub>-4</sub> 8 <sub>-6</sub>	1983.3	3.4
	8 <sub>-2</sub> 8 <sub>-4</sub>	1987.5	3.8
	8 <sub>-4</sub> 8 <sub>-2</sub>	2063.9	2.7
	8 <sub>-6</sub> 8 <sub>-4</sub>	2071.3	2.6
	8 <sub>-2</sub> 8 <sub>0</sub>	2095.3	1.7
	8 <sub>-5</sub> 8 <sub>-3</sub>	2100.4	1.2
	8 <sub>-8</sub> 8 <sub>-6</sub>	2101.4	1.9
	8 <sub>-7</sub> 8 <sub>-5</sub>	2108.1	1.0
	8 <sub>-3</sub> 8 <sub>-1</sub>	2111.4	0.9
	8 <sub>0</sub> 8 <sub>2</sub>	2136.5	1.1
	8 <sub>-1</sub> 8 <sub>1</sub>	2138.9	0.6
	8 <sub>2</sub> 8 <sub>4</sub>	2173.4	0.6
R	8 <sub>-3</sub> 9 <sub>-5</sub>	2108.3	0.5
	8 <sub>-7</sub> 9 <sub>-9</sub>	2122.3	3.8
	8 <sub>-8</sub> 9 <sub>-8</sub>	2122.6	7.7
	8 <sub>-5</sub> 9 <sub>-7</sub>	2123.2	1.7
	8 <sub>-6</sub> 9 <sub>-6</sub> <sup>q</sup>	2130.2	3.8
	8 <sub>-4</sub> 9 <sub>-4</sub>	2152.7	2.0
	8 <sub>-2</sub> 9 <sub>-2</sub>	2193.3	1.5
	8 <sub>-3</sub> 9 <sub>-1</sub>	2212.1	0.8
	8 <sub>-5</sub> 9 <sub>-3</sub>	2213.0	0.5

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION		FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''}$ $J'_{\tau'}$	$\nu$ (cm <sup>-1</sup> )	$[I]_J^{J''} \times 10$
P	$8_0$ $9_0$	82234.8	1.6
	$8_{-1}$ $9_1$	2237.4	0.8
	$8_2$ $9_2$	2271.4	1.3
	$8_1$ $9_3$	2271.6	0.7
	$8_4$ $9_4$	2308.9	0.9
	$8_3$ $9_5$	2308.9	0.5
	$8_6$ $9_6$	2348.7	0.6
	$9_0$ $8_0$	1851.0	0.6
	$9_{-2}$ $8_{-2}$	1865.4	0.7
	$9_{-4}$ $8_{-4}$	1895.1	1.0
	$9_{-6}$ $8_{-6}$	1926.5	2.2
	$9_{-7}$ $8_{-5}$	1934.7	1.2
	$9_{-8}$ $8_{-8}$	1946.2	4.9
Q	$9_{-9}$ $8_{-7}$	1946.6	2.5
	$9_{-6}$ $9_{-8}$	1947.6	1.0
	$9_{-7}$ $9_{-9}$	1948.8	0.5
	$9_0$ $9_{-2}$	1949.0	0.7
	$9_{-4}$ $9_{-6}$	1954.0	1.4
	$9_{-2}$ $9_{-4}$	1954.2	1.2
	$9_{-5}$ $9_{-7}$	1962.7	0.9
	$9_{-1}$ $9_{-3}$	1963.5	0.8
	$9_{-3}$ $9_{-5}$	1971.7	1.2
	$9_{-5}$ $9_{-3}$	2052.5	0.8

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION		FREQUENCY	*RELATIVE INTENSITY
Branch	$J''_{\tau''}$ $J'_{\tau'}$	$\nu(\text{cm}^{-1})$	$[I]_{J'}^{J''} \times 10$
R	$9_{-7}$ $9_{-5}$	82071.8	0.7
	$9_{-3}$ $9_{-1}$	2075.5	0.5
	$9_{-6}$ $9_{-4}$	2095.8	1.5
	$9_{-4}$ $9_{-2}$	2100.8	1.2
	$9_{-9}$ $9_{-7}$	2103.8	0.6
	$9_{-8}$ $9_{-6}$	2108.0	1.3
	$9_{-2}$ $9_0$	2125.1	0.8
	$9_0$ $9_2$	2159.5	0.5
	$9_{-4}$ $10_{-6}$	2112.9	0.8
	$9_{-8}$ $10_{-10}$	2122.4	5.5
	$9_{-9}$ $10_{-9}$	2122.5	2.7
	$9_{-6}$ $10_{-8}$	2124.4	2.5
	$9_{-7}$ $10_{-7}$	2128.2	1.3
	$9_{-5}$ $10_{-5}$	2145.0	0.7
	$9_{-4}$ $10_{-2}$	2215.0	0.9
	$9_{-6}$ $10_{-4}$	2227.5	0.5
	$9_{-2}$ $10_0$	2235.1	0.9
	$9_0$ $10_2$	2268.6	0.8
	$9_2$ $10_4$	2306.2	0.5
P	$10_{-7}$ $9_{-7}$	1909.3	0.8
	$10_{-6}$ $9_{-4}$	1912.2	0.7
	$10_{-8}$ $9_{-6}$	1914.2	1.6
	$10_{-9}$ $9_{-9}$	1927.9	1.7

## APPX. III

TABLE III.4 (Continued)

IDENTIFICATION		FREQUENCY	RELATIVE INTENSITY
Branch	$J''_{\tau''} \quad J'_{\tau'}$	$\nu(\text{cm}^{-1})$	$[I]_{J'}^{J''} \times 10$
Q	$10_{-10} \quad 9_{-8}$	81928.1	3.4
	$10_{-8} \quad 10_{-10}$	1928.6	0.6
	$10_0 \quad 10_{-2}$	1936.8	0.5
	$10_{-6} \quad 10_{-8}$	1940.7	1.0
	$10_{-2} \quad 10_{-4}$	1949.7	1.0
	$10_{-4} \quad 10_{-6}$	1952.7	1.4
	$10_{-6} \quad 10_{-4}$	2043.8	0.9
	$10_{-4} \quad 10_{-2}$	2054.7	0.6
	$10_{-8} \quad 10_{-6}$	2073.1	0.8
	$10_{-10} \quad 10_{-8}$	2104.9	0.7
R	$10_{-9} \quad 11_{-11}$	2121.6	1.9
	$10_{-10} \quad 11_{-10}$	2121.6	3.7
	$10_{-7} \quad 11_{-9}$	2123.9	0.9
	$10_{-8} \quad 11_{-8}$	2126.0	1.8
	$10_{-6} \quad 11_{-6}$	2137.6	0.9
	$10_{-4} \quad 11_{-4}$	2171.4	0.5



## APPENDIX IV

TABLE IV.1

Rotation-Electronic Energy Levels of the  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  States of  $H_2O$ .

(Electronic Interaction Included)

ENERGY LEVEL	EXCITED STATE $\tilde{C}^1B_1$	EXCITED STATE $\tilde{D}^1A_1$
$J'_{\tau'}$	$E' \text{ (cm}^{-1}\text{)}$	$E' \text{ (cm}^{-1}\text{)}$
$0_0$	80624.67	82058.67
$1_{-1}$	0645.86	2079.90
$1_0$	0659.13	2097.44
$1_1$	0663.20	2101.72
$2_{-2}$	0687.44	2121.69
$2_{-1}$	0697.45	2135.64
$2_0$	0709.65	2148.47
$2_1$	0749.52	2201.05
$2_2$	0750.32	2201.74
$3_{-3}$	0747.99	2182.75
$3_{-2}$	0754.45	2192.54
$3_{-1}$	0778.76	2218.13
$3_0$	0813.09	2264.76
$3_1$	0816.91	2268.10
$3_2$	0890.29	2363.35
$3_3$	0890.39	2363.42
$4_{-4}$	0826.11	2261.66
$4_{-3}$	0829.74	2267.74
$4_{-2}$	0869.73	2310.02
$4_{-1}$	0897.22	2349.17

APPX. IV

TABLE IV.1 (Continued)

ENERGY LEVEL $J'_{\tau'}$	EXCITED STATE $\tilde{C}^1B_1$ $E' \text{ (cm}^{-1}\text{)}$	EXCITED STATE $\tilde{D}^1A_1$ $E' \text{ (cm}^{-1}\text{)}$
$4_0$	80907.67	82358.55
$4_1$	0976.40	2449.49
$4_2$	0977.09	2449.98
$4_3$	1082.93	2586.64
$4_4$	1082.94	2586.64
$5_{-5}$	0921.07	2357.44
$5_{-4}$	0922.89	2360.86
$5_{-3}$	0981.28	2423.12
$5_{-2}$	1001.39	2453.83
$5_{-1}$	1022.76	2473.57
$5_0$	1084.21	2557.41
$5_1$	1086.84	2559.31
$5_2$	1190.66	2693.36
$5_3$	1190.75	2693.41
$5_4$	1327.91	2867.92
$5_5$	1327.91	2867.92
$6_{-6}$	1032.75	2469.77
$6_{-5}$	1033.60	2471.55
$6_{-4}$	1111.78	2555.98
$6_{-3}$	1125.02	2578.21
$6_{-2}$	1161.49	2612.84

APPX. IV

TABLE IV.1 (Continued)

ENERGY LEVEL	EXCITED STATE $\tilde{C}^1B_1$	EXCITED STATE $\tilde{D}^1A_1$
$J'_\tau$	$E' \text{ (cm}^{-1}\text{)}$	$E' \text{ (cm}^{-1}\text{)}$
$6_{-1}$	81213.54	82687.00
$6_0$	1220.78	2692.38
$6_1$	1320.41	2823.07
$6_2$	1320.86	2823.33
$6_3$	1457.09	2997.09
$6_4$	1457.10	2997.10
$6_5$	1625.55	3209.95
$6_6$	1625.55	3209.95
$7_{-7}$	1161.28	2598.69
$7_{-6}$	1161.66	2599.57
$7_{-5}$	1259.66	2707.01
$7_{-4}$	1267.48	2721.73
$7_{-3}$	1322.63	2775.43
$7_{-2}$	1363.98	2837.99
$7_{-1}$	1379.83	2850.28
$7_0$	1472.31	2974.92
$7_1$	1473.89	2975.87
$7_2$	1608.30	3148.23
$7_3$	1608.36	3148.26
$7_4$	1776.17	3360.57
$7_5$	1776.17	3360.57
$7_6$	1976.12	3611.45
$7_7$	1976.12	3611.45

APPX. IV

TABLE IV.1 (Continued)

ENERGY LEVEL	EXCITED STATE $\tilde{C}^1B_1$	EXCITED STATE $\tilde{D}^1A_1$
$J'_\tau$	$E' \text{ (cm}^{-1}\text{)}$	$E' \text{ (cm}^{-1}\text{)}$
$8_{-8}$	81306.79	82744.34
$8_{-7}$	1306.95	2744.76
$8_{-6}$	1424.01	2874.89
$8_{-5}$	1428.23	2883.85
$8_{-4}$	1504.56	2960.04
$8_{-3}$	1534.98	3009.95
$8_{-2}$	1564.11	3033.67
$8_{-1}$	1646.33	3149.00
$8_0$	1650.75	3151.70
$8_1$	1781.74	3321.52
$8_2$	1782.00	3321.65
$8_3$	1948.77	3533.10
$8_4$	1948.78	3533.10
$8_5$	2148.20	3783.51
$8_6$	2148.20	3783.51
$8_7$	2379.94	4072.10
$8_8$	2379.94	4072.10
$9_{-9}$	1469.34	2906.82
$9_{-8}$	1469.40	2907.02
$9_{-7}$	1604.70	3058.97
$9_{-6}$	1606.82	3064.05
$9_{-5}$	1705.40	3165.03
$9_{-4}$	1725.88	3202.33

APPX. IV

TABLE IV.1 (Continued)

ENERGY LEVEL	EXCITED STATE $\tilde{C}^1B_1$	EXCITED STATE $\tilde{D}^1A_1$
$J'_\tau$	$E' \text{ (cm}^{-1}\text{)}$	$E' \text{ (cm}^{-1}\text{)}$
$9_{-3}$	1772.78	3242.41
$9_{-2}$	1842.27	3345.23
$9_{-1}$	1852.57	3351.79
$9_0$	1977.58	3517.16
$9_1$	1978.47	3517.59
$9_2$	2143.54	3727.72
$9_3$	2143.58	3727.74
$9_4$	2342.21	3977.46
$9_5$	2342.21	3977.46
$9_6$	2573.47	4265.62
$9_7$	2573.47	4265.62
$9_8$	2837.28	4591.64
$9_9$	2837.28	4591.64
$10_{-10}$	1648.97	3086.21
$10_{-9}$	1648.99	3086.30
$10_{-8}$	1801.90	3261.94
$10_{-7}$	1802.92	3348.41
$10_{-6}$	1923.41	3348.41
$10_{-5}$	1935.98	3388.61
$10_{-4}$	2004.34	3475.54
$10_{-3}$	2059.72	3563.39
$10_{-2}$	2080.28	3577.22
$10_{-1}$	2195.93	3735.30

APPX. IV

TABLE IV.1 (Continued)

ENERGY LEVEL	EXCITED STATE $\tilde{C}^1B_1$	EXCITED STATE $\tilde{D}^1A_1$
$J'_{\tau'}$	$E' \text{ (cm}^{-1}\text{)}$	$E' \text{ (cm}^{-1}\text{)}$
$10_0$	82198.42	83736.56
$10_1$	2360.67	3944.60
$10_2$	2360.82	3944.66
$10_3$	2558.31	4193.43
$10_4$	2558.32	4193.43
$10_5$	2788.90	4480.99
$10_6$	2788.90	4480.99
$10_7$	3052.27	4806.61
$10_8$	3052.27	4806.61
$10_9$	3259.22	5169.77
$10_{10}$	3414.49	5169.77
$11_{-11}$	1845.69	3282.52
$11_{-10}$	1845.70	3282.56
$11_{-9}$	2015.86	3475.83
$11_{-8}$	2016.32	3477.24
$11_{-7}$	2157.55	3629.14
$11_{-6}$	2164.64	3645.80
$11_{-5}$	2256.91	3731.62
$11_{-4}$	2298.10	3803.09
$11_{-3}$	2333.97	3828.85
$11_{-2}$	2436.75	3976.02
$11_{-1}$	2442.81	3979.21
$11_0$	2600.37	4183.95

APPX. IV

TABLE IV.1 (Continued)

ENERGY LEVEL	EXCITED STATE $\tilde{C}^1B_1$	EXCITED STATE $\tilde{D}^1A_1$
$J'_{\tau'}$	$E' \text{ (cm}^{-1}\text{)}$	$E' \text{ (cm}^{-1}\text{)}$
$11_1$	82600.83	84184.14
$11_2$	2796.68	4431.57
$11_3$	2796.70	4431.58
$11_4$	3026.38	4718.34
$11_5$	3026.38	4718.34
$11_6$	3289.14	5043.42
$11_7$	3289.14	5043.42
$11_8$	3584.87	5406.20
$11_9$	3584.87	5406.20
$11_{10}$	3913.60	5806.26
$11_{11}$	3913.60	5806.26

APPX.IV

TABLE IV.2

Rotation-Electronic Energy Levels of the  $\tilde{C}^1B_1$  and  $\tilde{D}^1A_1$  States of  $D_2O$ .  
(Electronic Interaction Included)

ENERGY LEVEL $J'_\tau$	EXCITED STATE $\tilde{C}^1B_1$ $E'$ ( $\text{cm}^{-1}$ )	EXCITED STATE $\tilde{D}^1A_1$ $E'$ ( $\text{cm}^{-1}$ )
$0_0$	80751.9	82074.9
$1_{-1}$	0762.6	2085.6
$1_0$	0770.9	2095.3
$1_1$	0772.8	2097.3
$2_{-2}$	0783.8	2106.8
$2_{-1}$	0790.5	2114.8
$2_0$	0796.2	2120.7
$2_1$	0821.2	2149.8
$2_2$	0821.4	2150.1
$3_{-3}$	0814.8	2138.0
$3_{-2}$	0819.7	2143.9
$3_{-1}$	0831.0	2155.7
$3_0$	0853.3	2182.0
$3_1$	0854.7	2183.4
$3_2$	0899.9	2235.7
$3_3$	0899.9	2235.7
$4_{-4}$	0855.2	2178.5
$4_{-3}$	0858.3	2182.4
$4_{-2}$	0877.0	2202.0
$4_{-1}$	0896.0	2224.8
$4_0$	0899.9	2228.5
$4_1$	0943.3	2279.1



APPX. IV

TABLE IV.2(Continued)

ENERGY LEVEL

EXCITED STATE  $\tilde{C}^1B_1$   
 $E' \text{ (cm}^{-1}\text{)}$ EXCITED STATE  $\tilde{D}^1A_1$   
 $E' \text{ (cm}^{-1}\text{)}$ 

$J'_\tau$		
$4_2$	80943.5	82279.2
$4_3$	1007.9	2353.4
$4_4$	1007.9	2353.4
$5_{-5}$	0904.4	2227.8
$5_{-4}$	0906.2	2230.2
$5_{-3}$	0933.8	2259.1
$5_{-2}$	0949.0	2277.9
$5_{-1}$	0957.3	2286.0
$5_0$	0997.7	2333.5
$5_1$	0998.4	2334.1
$5_2$	1062.1	2407.7
$5_3$	1062.1	2407.7
$5_4$	1145.2	2503.3
$5_5$	1145.2	2503.3
$6_{-6}$	0962.2	2285.7
$6_{-5}$	0963.2	2287.1
$6_{-4}$	1000.8	2326.7
$6_{-3}$	1012.1	2341.1
$6_{-2}$	1026.8	2355.6
$6_{-1}$	1062.9	2398.9
$6_0$	1065.1	2400.6
$6_1$	1127.4	2473.0
$6_2$	1127.5	2473.1

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TABLE IV.2 (Continue)

ENERGY LEVEL $J'_\tau$	EXCITED STATE $\tilde{C}^1B_1$ $E' \text{ (cm}^{-1}\text{)}$	EXCITED STATE $\tilde{D}^1A_1$ $E' \text{ (cm}^{-1}\text{)}$
$6_3$	1210.2	2568.4
$6_4$	1210.2	2568.4
$6_5$	1311.8	2685.1
$6_6$	1311.8	2685.1
$7_{-7}$	1028.7	2352.2
$7_{-6}$	1029.2	2353.0
$7_{-5}$	1077.3	2403.9
$7_{-4}$	1085.0	2414.2
$7_{-3}$	1108.1	2437.1
$7_{-2}$	1139.0	2475.0
$7_{-1}$	1143.9	2479.3
$7_0$	1203.8	2549.5
$7_1$	1204.2	2549.7
$7_2$	1286.3	2644.5
$7_3$	1286.3	2644.5
$7_4$	1387.7	2761.0
$7_5$	1387.7	2761.0
$7_6$	1507.9	2898.9
$7_7$	1507.9	2898.9
$8_{-8}$	1104.0	2427.4
$8_{-7}$	1104.2	2427.7
$8_{-6}$	1162.6	2490.1
$8_{-5}$	1167.5	2496.9

## APPX. IV

TABLE IV.2 (Continued)

ENERGY LEVEL

EXCITED STATE  $\tilde{C}^1B_1$   
 $E' \text{ (cm}^{-1}\text{)}$ EXCITED STATE  $\tilde{D}^1A_1$   
 $E' \text{ (cm}^{-1}\text{)}$ 

$J'_\tau$		
$8_{-4}$	81200.5	82530.1
$8_{-3}$	1225.8	2561.9
$8_{-2}$	1235.4	2570.5
$8_{-1}$	1291.4	2637.0
$8_0$	1292.4	2637.8
$8_1$	1373.5	2731.7
$8_2$	1373.6	2731.7
$8_3$	1474.6	2847.9
$8_4$	1474.6	2847.9
$8_5$	1594.6	2985.7
$8_6$	1594.6	2985.7
$8_7$	1733.5	3144.7
$8_8$	1733.5	3144.7
$9_{-9}$	1187.9	2511.2
$9_{-8}$	1188.1	2511.3
$9_{-7}$	1256.6	2584.9
$9_{-6}$	1259.4	2589.1
$9_{-5}$	1303.5	2634.0
$9_{-4}$	1323.0	2659.4
$9_{-3}$	1339.4	2674.5
$9_{-2}$	1390.1	2735.8
$9_{-1}$	1392.5	2737.7

APPX.IV

TABLE IV.2 (Continued)

ENERGY LEVEL $J'_{\tau}$	EXCITED STATE $\tilde{C}^1B_1$ $E' \text{ (cm}^{-1}\text{)}$	EXCITED STATE $\tilde{D}^1A_1$ $E' \text{ (cm}^{-1}\text{)}$
$9_0$	81471.9	82830.1
$9_1$	1472.1	2830.2
$9_2$	1572.6	2945.9
$9_3$	1572.6	2945.9
$9_4$	1692.3	3083.4
$9_5$	1692.3	3083.8
$9_6$	1831.0	3242.2
$9_7$	1831.0	3242.2
$9_8$	1988.6	3422.3
$9_9$	1988.6	3422.3
$10_{-10}$	1280.7	2603.7
$10_{-9}$	1280.8	2603.8
$10_{-8}$	1358.9	2688.0
$10_{-7}$	1360.5	2690.5
$10_{-6}$	1460.3	2748.1
$10_{-5}$	1430.3	2767.1
$10_{-4}$	1455.7	2791.0
$10_{-3}$	1499.8	2845.7
$10_{-2}$	1505.1	2849.9
$10_{-1}$	1581.6	2939.7
$10_0$	1582.0	2940.0
$10_1$	1681.7	3055.0
$10_2$	1681.7	3055.0

APPX.IV

TABLE IV.2 (Continued)

ENERGY LEVEL $J'_{\tau}$	EXCITED STATE $\tilde{C}^1B_1$ $E' \text{ (cm}^{-1}\text{)}$	EXCITED STATE $\tilde{D}^1A_1$ $E' \text{ (cm}^{-1}\text{)}$
$10_3$	81801.1	83192.1
$10_4$	1801.1	3192.1
$10_5$	1939.6	3350.7
$10_6$	1939.6	3350.7
$10_7$	2097.0	3530.7
$10_8$	2097.0	3530.7
$10_9$	2273.3	3731.7
$10_{10}$	2273.3	3731.7
$11_{-11}$	1382.3	2704.9
$11_{-10}$	1382.3	2705.0
$11_{-9}$	1469.8	2799.6
$11_{-8}$	1470.7	2801.0
$11_{-7}$	1538.2	2871.3
$11_{-6}$	1547.5	2884.8
$11_{-5}$	1583.7	2919.5
$11_{-4}$	1620.5	2966.6
$11_{-3}$	1630.4	2974.8
$11_{-2}$	1702.5	3060.7
$11_{-1}$	1703.6	3061.5
$11_0$	1802.0	3175.4
$11_1$	1802.1	3175.4
$11_2$	1920.9	3312.0
$11_3$	1920.9	3312.0

APPX.IV

TABLE IV.2 (Continued)

ENERGY LEVEL $J'_\tau$	EXCITED STATE $\tilde{C}^1B_1$ $E'$ (cm $^{-1}$ )	EXCITED STATE $\tilde{D}^1A_1$ $E'$ (cm $^{-1}$ )
$11_4$	82059.1	83470.3
$11_5$	2059.1	3470.3
$11_6$	2216.3	3650.0
$11_7$	2216.3	3650.0
$11_8$	2392.5	3850.9
$11_9$	2392.5	3850.9
$11_{10}$	2587.7	4072.9
$11_{11}$	2587.7	4072.9

## APPENDIX V

TABLE V.1

$\tilde{C}^1B_1$  Transitions in  $H_2O$  Calculated for Various Ratios  $\langle \mu_z \rangle : \langle \mu_x \rangle$ .  
(Electronic Interactions)

IDENTIFICATION			FREQUENCY $\nu$ ( $cm^{-1}$ )	*RELATIVE INTENSITY $[I]_{J''}^{J'}$ x 10 FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{v''}$	$J'_{v'}$		1:0	0:1	1:1	1:-1
R	$0_0$	$1_1$	80663.2	-	3.3	3.5	3.1
P	$1_1$	$0_0$	582.3	-	8.1	8.1	8.1
Q	$1_0$	$1_{-1}$	608.7	-	4.2	4.2	4.2
	$1_{-1}$	$1_0$	635.3	-	13.3	14.4	12.3
R	$1_1$	$2_{-2}$	645.0	-	2.6	2.5	2.7
	$1_{-1}$	$2_0$	685.9	-	13.3	14.4	12.3
	$1_1$	$2_2$	707.9	-	13.6	15.6	11.7
	$1_0$	$2_1$	712.4	-	4.1	4.8	3.5
P	$2_1$	$1_0$	523.8	-	7.7	7.1	8.3
	$2_2$	$1_1$	526.6	-	2.9	2.7	3.1
	$2_0$	$1_{-1}$	550.6	-	3.1	3.1	3.1
	$2_{-2}$	$1_1$	593.1	-	0.7	0.8	0.6
Q	$2_2$	$2_{-2}$	560.9	-	0.8	0.7	0.9
	$2_1$	$2_0$	574.3	-	4.3	3.9	4.6
	$2_{-1}$	$2_{-2}$	607.9	-	19.0	19.1	18.8
	$2_{-2}$	$2_{-2}$	627.3	-	6.7	7.2	6.3
	$2_0$	$2_1$	654.3	-	1.7	2.0	1.5
	$2_{-1}$	$2_2$	670.8	-	3.6	4.3	2.9
R	$2_1$	$3_{-2}$	619.1	-	0.5	-	0.6

\*Values of  $[I]_{J''}^{J'}$  x 10 less than 0.5 are not included for  
 $\langle \mu_z \rangle : \langle \mu_x \rangle = 0:1$  and the corresponding cases of 1:0, 1:1 and 1:-1  
in this table.

## APPX V

TABLE V.1 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
P	2 <sub>0</sub>	3 <sub>-3</sub>	80652.8	-	0.9	0.9	1.0
	2 <sub>-2</sub>	3 <sub>-1</sub>	708.6	-	4.3	4.7	4.0
	2 <sub>0</sub>	3 <sub>1</sub>	721.7	-	4.6	5.2	4.0
	2 <sub>-1</sub>	3 <sub>0</sub>	733.6	-	11.2	13.0	9.5
	2 <sub>2</sub>	3 <sub>3</sub>	753.8	-	4.3	5.4	3.4
	2 <sub>1</sub>	3 <sub>2</sub>	755.0	-	13.0	16.2	10.2
	3 <sub>2</sub>	2 <sub>1</sub>	462.2	-	2.1	1.8	2.4
	3 <sub>3</sub>	2 <sub>2</sub>	462.8	-	6.3	5.4	7.3
	3 <sub>0</sub>	2 <sub>-2</sub>	490.7	-	2.0	1.9	2.2
	3 <sub>1</sub>	2 <sub>0</sub>	497.1	-	8.1	7.7	8.5
Q	3 <sub>-1</sub>	2 <sub>-2</sub>	513.9	-	8.0	7.9	8.1
	3 <sub>-3</sub>	2 <sub>0</sub>	572.7	-	1.8	2.2	1.5
	3 <sub>-1</sub>	2 <sub>2</sub>	576.8	-	0.8	0.9	0.6
	3 <sub>3</sub>	3 <sub>0</sub>	525.6	-	1.6	1.3	2.0
	3 <sub>2</sub>	3 <sub>1</sub>	529.6	-	0.6	0.5	0.7
	3 <sub>1</sub>	3 <sub>-2</sub>	541.9	-	1.7	1.4	2.0
	3 <sub>0</sub>	3 <sub>-1</sub>	572.1	-	1.9	1.8	2.1
	3 <sub>-2</sub>	3 <sub>-3</sub>	605.6	-	7.4	7.5	7.3
	3 <sub>-3</sub>	3 <sub>-2</sub>	617.5	-	23.4	24.7	22.2
	3 <sub>-1</sub>	3 <sub>0</sub>	639.6	-	7.0	8.0	6.1
	3 <sub>-2</sub>	3 <sub>1</sub>	674.5	-	1.0	1.3	0.8



## APPX V

TABLE V.1 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J', J''}^J \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	3 <sub>1</sub>	3 <sub>2</sub>	80677.7	-	2.6	3.2	2.0
	3 <sub>0</sub>	3 <sub>3</sub>	683.7	-	0.9	1.1	0.6
	3 <sub>1</sub>	4 <sub>-4</sub>	652.6	-	1.9	1.7	2.1
	3 <sub>1</sub>	4 <sub>-2</sub>	657.2	-	2.1	2.0	2.3
	3 <sub>-3</sub>	4 <sub>-2</sub>	732.8	-	10.0	11.1	8.9
	3 <sub>-1</sub>	4 <sub>0</sub>	734.1	-	12.1	13.6	10.7
	3 <sub>-2</sub>	4 <sub>-1</sub>	754.9	-	3.0	3.5	2.5
	3 <sub>1</sub>	4 <sub>2</sub>	764.5	-	10.0	12.2	8.0
	3 <sub>0</sub>	4 <sub>1</sub>	769.7	-	3.4	4.1	2.7
	3 <sub>3</sub>	4 <sub>4</sub>	795.4	-	8.5	11.2	6.1
P	3 <sub>2</sub>	4 <sub>3</sub>	795.6	-	2.8	3.8	2.0
	4 <sub>3</sub>	3 <sub>2</sub>	395.7	-	3.1	2.5	3.9
	4 <sub>4</sub>	3 <sub>3</sub>	396.8	-	1.0	0.8	1.3
	4 <sub>1</sub>	3 <sub>0</sub>	428.6	-	4.3	3.7	4.9
	4 <sub>2</sub>	3 <sub>1</sub>	431.1	-	1.5	1.3	1.7
	4 <sub>-1</sub>	3 <sub>-2</sub>	453.6	-	4.2	3.8	4.5
	4 <sub>0</sub>	3 <sub>-1</sub>	462.3	-	2.1	2.0	2.2
	4 <sub>-2</sub>	4 <sub>-3</sub>	472.0	-	1.8	1.7	1.8
Q	4 <sub>-3</sub>	3 <sub>0</sub>	588.0	-	0.5	0.7	0.4
	4 <sub>3</sub>	4 <sub>2</sub>	482.5	-	0.6	0.5	0.8
	4 <sub>2</sub>	4 <sub>-1</sub>	511.4	-	0.5	-	0.6
	4 <sub>1</sub>	4 <sub>0</sub>	523.1	-	2.0	1.6	2.3

## APPX V

TABLE V.1 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ ( $\text{cm}^{-1}$ )	RELATIVE INTENSITY $[I]_{J', J''}^J \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
	$4_{-1}$	$4_{-2}$	80568.8	-	5.9	5.6	6.1
	$4_{-3}$	$4_{-4}$	601.0	-	21.1	21.7	20.6
	$4_{-4}$	$4_{-3}$	607.4	-	7.3	7.6	7.0
	$4_{-2}$	$4_{-1}$	621.2	-	2.3	2.6	2.1
	$4_0$	$4_1$	659.9	-	0.9	1.1	0.7
	$4_{-1}$	$4_2$	676.2	-	2.7	3.4	2.0
	$4_{-3}$	$4_0$	682.6	-	1.7	2.2	1.3
	$4_1$	$4_4$	698.4	-	1.1	1.5	0.8
R	$4_{-1}$	$5_{-4}$	622.0	-	0.5	-	0.7
	$4_0$	$5_{-3}$	664.8	-	0.7	0.6	0.7
	$4_{-2}$	$5_{-1}$	746.7	-	2.9	3.3	2.5
	$4_{-4}$	$5_{-3}$	758.9	-	2.2	2.5	1.9
	$4_0$	$5_1$	770.4	-	2.3	2.8	1.9
	$4_{-3}$	$5_{-2}$	776.3	-	6.3	7.5	5.2
	$4_{-1}$	$5_0$	783.3	-	7.0	8.6	5.5
	$4_2$	$5_3$	804.9	-	1.9	2.4	1.4
	$4_1$	$5_2$	806.1	-	5.6	7.4	4.1
	$4_4$	$5_5$	833.3	-	1.3	1.8	0.9
	$4_3$	$5_4$	833.3	-	3.9	5.5	2.6
P	$5_5$	$4_4$	325.3	-	1.1	0.8	1.4
	$5_2$	$4_1$	360.0	-	0.6	0.5	0.8
	$5_3$	$4_2$	360.5	-	1.9	1.5	2.3

## APPX V

TABLE V.1 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_y \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
Q	5 <sub>0</sub>	4 <sub>-1</sub>	80391.0	-	0.9	0.8	1.0
	5 <sub>1</sub>	4 <sub>0</sub>	396.6	-	2.9	2.6	3.2
	5 <sub>-2</sub>	4 <sub>-3</sub>	412.6	-	0.8	0.8	0.9
	5 <sub>-1</sub>	4 <sub>-2</sub>	421.8	-	4.0	3.8	4.1
	5 <sub>-3</sub>	4 <sub>-4</sub>	425.5	-	3.0	2.8	3.1
	5 <sub>-3</sub>	4 <sub>0</sub>	507.1	-	0.8	1.0	0.6
	5 <sub>-5</sub>	4 <sub>-2</sub>	543.8	-	0.5	0.7	-
	5 <sub>3</sub>	5 <sub>0</sub>	467.6	-	0.6	-	0.8
	5 <sub>1</sub>	5 <sub>-2</sub>	490.3	-	0.8	0.6	1.1
	5 <sub>0</sub>	5 <sub>-1</sub>	516.6	-	0.5	-	0.6
	5 <sub>-2</sub>	5 <sub>-3</sub>	564.2	-	1.6	1.6	1.7
	5 <sub>-4</sub>	5 <sub>-5</sub>	594.0	-	5.6	5.8	5.5
	5 <sub>-5</sub>	5 <sub>-4</sub>	597.0	-	17.2	17.9	16.5
	5 <sub>-3</sub>	5 <sub>-2</sub>	600.8	-	5.7	6.2	5.3
	5 <sub>-1</sub>	5 <sub>0</sub>	636.3	-	2.1	2.6	1.7
	5 <sub>-2</sub>	5 <sub>1</sub>	669.7	-	0.6	0.8	0.4
	5 <sub>1</sub>	5 <sub>2</sub>	679.6	-	1.1	1.5	0.8
R	5 <sub>1</sub>	6 <sub>-2</sub>	650.4	-	0.7	0.6	0.8
	5 <sub>-1</sub>	6 <sub>-4</sub>	663.9	-	1.2	1.1	1.4
	5 <sub>-3</sub>	6 <sub>-2</sub>	760.9	-	5.1	5.8	4.4
	5 <sub>-1</sub>	6 <sub>0</sub>	772.9	-	4.3	5.1	3.6
	5 <sub>-5</sub>	6 <sub>-4</sub>	785.9	-	3.9	4.6	3.3

## APPX V

TABLE V.1 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ ( $\text{cm}^{-1}$ )	RELATIVE INTENSITY $[I]_{J_i}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
P	5 <sub>-2</sub>	6 <sub>-1</sub>	80796.4	-	1.4	1.7	1.1
	5 <sub>-4</sub>	6 <sub>-3</sub>	797.9	-	1.3	1.6	1.1
	5 <sub>1</sub>	6 <sub>2</sub>	809.8	-	3.2	4.2	2.4
	5 <sub>0</sub>	6 <sub>1</sub>	814.2	-	1.1	1.5	0.9
	5 <sub>3</sub>	6 <sub>4</sub>	840.5	-	2.2	3.1	1.5
	5 <sub>2</sub>	6 <sub>3</sub>	840.7	-	0.7	1.0	0.5
	5 <sub>5</sub>	6 <sub>6</sub>	867.9	-	1.3	1.9	0.8
	6 <sub>3</sub>	5 <sub>2</sub>	287.0	-	0.6	-	0.7
	6 <sub>1</sub>	5 <sub>0</sub>	321.0	-	1.0	0.8	1.2
	6 <sub>-1</sub>	5 <sub>-2</sub>	349.5	-	1.4	1.2	1.6
Q	6 <sub>0</sub>	5 <sub>-1</sub>	357.9	-	0.6	0.5	0.6
	6 <sub>-3</sub>	5 <sub>-4</sub>	368.5	-	1.3	1.2	1.5
	6 <sub>-2</sub>	5 <sub>-3</sub>	375.8	-	0.7	0.7	0.7
	6 <sub>-1</sub>	6 <sub>-2</sub>	509.6	-	1.0	0.9	1.2
	6 <sub>-3</sub>	6 <sub>-4</sub>	557.3	-	3.6	3.5	3.6
	6 <sub>-4</sub>	6 <sub>-3</sub>	580.2	-	1.3	1.4	1.3
	6 <sub>-5</sub>	6 <sub>-6</sub>	584.7	-	11.6	11.9	11.2
	6 <sub>-6</sub>	6 <sub>-5</sub>	586.0	-	3.9	4.0	3.8
R	6 <sub>-3</sub>	6 <sub>0</sub>	666.3	-	0.9	1.1	0.6
	6 <sub>-1</sub>	6 <sub>2</sub>	669.0	-	0.7	1.0	0.5
	6 <sub>-2</sub>	7 <sub>-1</sub>	774.3	-	0.8	0.9	0.6
	6 <sub>-4</sub>	7 <sub>-3</sub>	777.8	-	0.8	1.0	0.7

## APPX V

TABLE V.1 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J''}^{J'} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
P	6 <sub>0</sub>	7 <sub>1</sub>	80809.1	-	0.6	0.7	-
	6 <sub>-3</sub>	7 <sub>-2</sub>	809.5	-	2.3	2.9	1.8
	6 <sub>-6</sub>	7 <sub>-5</sub>	812.1	-	0.7	0.9	0.6
	6 <sub>-5</sub>	7 <sub>-4</sub>	819.4	-	2.2	2.8	1.7
	6 <sub>-1</sub>	7 <sub>0</sub>	820.4	-	1.8	2.3	1.3
	6 <sub>1</sub>	7 <sub>2</sub>	845.1	-	1.2	1.6	0.8
	6 <sub>3</sub>	7 <sub>4</sub>	872.5	-	0.7	1.0	-
	7 <sub>-1</sub>	6 <sub>-2</sub>	313.8	-	0.8	0.7	0.9
	7 <sub>-3</sub>	6 <sub>-4</sub>	324.7	-	0.9	0.8	0.9
	7 <sub>-5</sub>	6 <sub>-6</sub>	325.6	-	0.7	0.6	0.7
Q	7 <sub>-4</sub>	7 <sub>-5</sub>	547.6	-	0.7	0.7	0.7
	7 <sub>-5</sub>	7 <sub>-4</sub>	560.3	-	2.4	2.5	2.3
	7 <sub>-6</sub>	7 <sub>-7</sub>	573.4	-	2.3	2.4	2.2
	7 <sub>-7</sub>	7 <sub>-6</sub>	574.0	-	7.0	7.2	6.7
	7 <sub>-3</sub>	7 <sub>-2</sub>	576.9	-	0.8	0.9	0.7
R	7 <sub>-3</sub>	8 <sub>-2</sub>	777.0	-	1.1	1.2	0.9
	7 <sub>-5</sub>	8 <sub>-4</sub>	797.4	-	1.1	1.3	0.9
	7 <sub>-1</sub>	8 <sub>0</sub>	803.1	-	0.7	0.9	0.6
	7 <sub>-7</sub>	8 <sub>-6</sub>	836.4	-	1.1	1.4	0.9
	7 <sub>1</sub>	8 <sub>2</sub>	843.3	-	0.5	0.7	-
Q	8 <sub>-5</sub>	8 <sub>-6</sub>	534.7	-	1.2	1.2	1.2

APPX V

TABLE V.1 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J',J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
	8 <sub>-7</sub>	8 <sub>-8</sub>	80560.6	-	3.7	3.8	3.6
	8 <sub>-8</sub>	8 <sub>-7</sub>	560.8	-	1.2	1.3	1.2
R	8 <sub>-7</sub>	9 <sub>-6</sub>	860.6	-	0.5	0.7	-
Q	9 <sub>-7</sub>	9 <sub>-6</sub>	522.1	-	0.6	0.6	0.6
	9 <sub>-8</sub>	9 <sub>-9</sub>	546.1	-	0.6	0.6	0.6
	9 <sub>-9</sub>	9 <sub>-8</sub>	546.2	-	1.8	1.8	1.7
Q	10 <sub>-9</sub>	10 <sub>-10</sub>	530.2	-	0.8	0.8	0.7

## APPX V

TABLE V.2

$\tilde{D}^1A_1$  Transitions in  $H_2O$  Calculated for Various Ratios  $\langle \mu_z \rangle : \langle \mu_x \rangle$ .  
(Electronic Interaction)

Branch	IDENTIFICATION		FREQUENCY $\nu$ ( $cm^{-1}$ )	*RELATIVE INTENSITY $[I]_{J', J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
	$J''_{\alpha''}$	$J'_{\alpha'}$		1:0	0:1	1:1	1:-1
R	0 <sub>0</sub>	1 <sub>0</sub>	82097.4	3.3	-	3.1	3.6
P	1 <sub>0</sub>	0 <sub>0</sub>	2021.5	2.8	-	2.8	2.8
Q	1 <sub>1</sub>	1 <sub>-1</sub>	2037.5	12.2	-	12.2	12.2
	1 <sub>-1</sub>	1 <sub>1</sub>	2077.9	13.3	-	12.3	14.4
R	1 <sub>0</sub>	2 <sub>-2</sub>	2084.5	1.9	-	1.8	1.9
	1 <sub>-1</sub>	2 <sub>-1</sub>	2111.8	13.3	-	12.3	14.4
	1 <sub>1</sub>	2 <sub>1</sub>	2158.7	12.1	-	10.3	14.1
	1 <sub>0</sub>	2 <sub>2</sub>	2164.6	3.7	-	3.1	4.3
P	2 <sub>2</sub>	1 <sub>0</sub>	1960.9	2.1	-	2.3	1.9
	2 <sub>1</sub>	1 <sub>1</sub>	1966.4	7.7	-	8.3	7.1
	2 <sub>-1</sub>	1 <sub>-1</sub>	2000.4	10.2	-	10.2	10.2
	2 <sub>-2</sub>	1 <sub>0</sub>	2027.3	1.8	-	1.7	1.9
Q	2 <sub>1</sub>	2 <sub>-1</sub>	2000.3	4.3	-	4.6	3.9
	2 <sub>2</sub>	2 <sub>0</sub>	2011.9	2.1	-	2.2	2.0
	2 <sub>0</sub>	2 <sub>-2</sub>	2026.5	4.6	-	4.7	4.6
	2 <sub>-2</sub>	2 <sub>0</sub>	2078.3	4.9	-	4.5	5.3
	2 <sub>0</sub>	2 <sub>2</sub>	2106.5	2.3	-	2.0	2.6
	2 <sub>-1</sub>	2 <sub>1</sub>	2121.5	5.6	-	4.8	6.5

\*Values of  $[I]_{J', J''}^{J''} \times 10$  less than 0.5 are not included for  
 $\langle \mu_z \rangle : \langle \mu_x \rangle = 1:0$  and the corresponding cases of 0:1, 1:1 and  
1:-1 in this table.

## APPX V

TABLE V.2 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J_1}^{J_2} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J_2''$	$J_1'$		1:0	0:1	1:1	1:-1
R	2 <sub>1</sub>	3 <sub>-1</sub>	82082.8	1.3	-	1.3	1.2
	2 <sub>-1</sub>	3 <sub>-3</sub>	2103.2	10.3	-	10.0	10.7
	2 <sub>-2</sub>	3 <sub>-2</sub>	2122.4	5.1	-	4.7	5.5
	2 <sub>0</sub>	3 <sub>0</sub>	2169.5	3.5	-	2.9	4.0
	2 <sub>-1</sub>	3 <sub>1</sub>	2188.6	7.7	-	6.3	9.1
	2 <sub>2</sub>	3 <sub>2</sub>	2226.8	4.1	-	3.2	5.1
	2 <sub>1</sub>	3 <sub>3</sub>	2228.1	12.3	-	9.5	15.4
P	3 <sub>3</sub>	2 <sub>1</sub>	1913.6	5.7	-	6.7	4.8
	3 <sub>2</sub>	2 <sub>2</sub>	1914.4	1.9	-	2.3	1.6
	3 <sub>1</sub>	2 <sub>-1</sub>	1923.1	3.2	-	3.7	2.9
	3 <sub>0</sub>	2 <sub>0</sub>	1941.8	2.0	-	2.2	1.9
	3 <sub>-2</sub>	2 <sub>-2</sub>	1979.3	3.5	-	3.5	3.5
	3 <sub>-3</sub>	2 <sub>-1</sub>	1998.7	8.9	-	8.6	9.2
	3 <sub>-1</sub>	2 <sub>1</sub>	2027.5	1.3	-	1.2	1.4
Q	3 <sub>2</sub>	3 <sub>0</sub>	1977.5	0.8	-	0.9	0.7
	3 <sub>3</sub>	3 <sub>1</sub>	1980.6	2.7	-	3.0	2.4
	3 <sub>0</sub>	3 <sub>-2</sub>	1985.8	1.6	-	1.8	1.5
	3 <sub>1</sub>	3 <sub>-1</sub>	2005.6	9.3	-	9.7	9.0
	3 <sub>-1</sub>	3 <sub>-3</sub>	2009.2	11.0	-	11.3	10.7
	3 <sub>-3</sub>	3 <sub>-1</sub>	2081.2	11.1	-	9.8	12.3
	3 <sub>-1</sub>	3 <sub>1</sub>	2094.6	9.1	-	7.9	10.4
	3 <sub>-2</sub>	3 <sub>0</sub>	2122.4	2.1	-	1.8	2.5
	3 <sub>1</sub>	3 <sub>3</sub>	2150.8	3.4	-	2.8	4.2



## APPX V

TABLE V.2 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ ( $\text{cm}^{-1}$ )	RELATIVE INTENSITY $[I]_{J', J''}^J \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	$3_0$	$3_2$	82156.7	1.2	-	0.9	1.4
	$3_0$	$4_{-2}$	2103.3	0.8	-	0.8	0.8
	$3_{-2}$	$4_{-4}$	2119.3	4.2	-	4.0	4.4
	$3_{-3}$	$4_{-3}$	2130.8	15.1	-	14.1	16.2
	$3_{-1}$	$4_{-1}$	2175.6	8.3	-	7.1	9.6
	$3_{-2}$	$4_0$	2216.2	1.5	-	1.2	1.8
	$3_1$	$4_1$	2236.9	8.2	-	6.3	10.3
	$3_0$	$4_2$	2243.3	2.8	-	2.2	3.5
	$3_3$	$4_3$	2298.1	8.2	-	5.8	10.9
	$3_2$	$4_4$	2298.3	2.7	-	1.9	3.6
P	$4_4$	$3_2$	1868.7	1.0	-	1.2	0.8
	$4_3$	$3_3$	1868.8	3.0	-	3.7	2.3
	$4_2$	$3_0$	1878.9	1.1	-	1.3	0.9
	$4_1$	$3_1$	1883.6	3.6	-	4.2	0.3
	$4_{-1}$	$3_{-1}$	1917.2	4.4	-	4.7	4.1
	$4_{-3}$	$3_{-3}$	1957.7	9.5	-	9.5	9.6
	$4_{-4}$	$3_{-2}$	1970.2	3.2	-	3.1	3.2
	$4_{-2}$	$3_0$	1988.7	0.7	-	0.7	0.7
	$4_{-3}$	$3_1$	2043.0	0.8	-	0.7	0.9
Q	$4_3$	$4_1$	1954.9	0.9	-	1.1	0.8
	$4_1$	$4_{-1}$	1964.6	2.9	-	3.3	2.5
	$4_{-1}$	$4_{-3}$	1966.8	3.9	-	4.3	3.4

## APPX V

TABLE V.2 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
	4 <sub>2</sub>	4 <sub>0</sub>	81972.7	1.1	-	1.3	1.0
	4 <sub>-2</sub>	4 <sub>-4</sub>	1985.6	2.3	-	2.4	2.1
	4 <sub>0</sub>	4 <sub>-2</sub>	1993.6	2.8	-	2.9	2.8
	4 <sub>-2</sub>	4 <sub>0</sub>	2082.5	2.6	-	2.3	3.0
	4 <sub>-4</sub>	4 <sub>-2</sub>	2087.7	2.2	-	1.9	2.5
	4 <sub>-3</sub>	4 <sub>-1</sub>	2124.1	5.1	-	4.2	6.2
	4 <sub>0</sub>	4 <sub>2</sub>	2133.5	1.2	-	1.0	1.5
	4 <sub>-1</sub>	4 <sub>1</sub>	2148.6	3.9	-	3.1	4.8
	4 <sub>2</sub>	4 <sub>4</sub>	2199.8	0.5	-	0.4	0.6
	4 <sub>1</sub>	4 <sub>3</sub>	2201.1	1.5	-	1.1	1.9
R	4 <sub>1</sub>	5 <sub>-1</sub>	2089.0	0.5	-	0.5	0.5
	4 <sub>-1</sub>	5 <sub>-3</sub>	2122.2	2.8	-	2.7	2.9
	4 <sub>-3</sub>	5 <sub>-5</sub>	2132.4	12.0	-	11.4	12.6
	4 <sub>-4</sub>	5 <sub>-4</sub>	2138.5	4.4	-	4.1	4.6
	4 <sub>-2</sub>	5 <sub>-2</sub>	2177.8	2.1	-	1.8	2.4
	4 <sub>0</sub>	5 <sub>0</sub>	2240.9	1.6	-	1.3	2.1
	4 <sub>-3</sub>	5 <sub>-1</sub>	2248.5	2.2	-	1.7	2.7
	4 <sub>-1</sub>	5 <sub>1</sub>	2258.4	5.1	-	3.8	6.5
	4 <sub>2</sub>	5 <sub>2</sub>	2307.5	1.6	-	1.2	2.2
	4 <sub>1</sub>	5 <sub>3</sub>	2308.9	5.0	-	3.5	6.7
	4 <sub>4</sub>	5 <sub>4</sub>	2373.3	1.3	-	0.8	1.8
	4 <sub>3</sub>	5 <sub>5</sub>	2373.3	3.8	-	2.5	5.3
P	5 <sub>5</sub>	4 <sub>3</sub>	1828.0	1.0	-	1.4	0.7

## APPX V

TABLE V.2 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ ( $\text{cm}^{-1}$ )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
	5 <sub>3</sub>	4 <sub>1</sub>	81832.9	1.6	-	2.0	1.2
	5 <sub>2</sub>	4 <sub>2</sub>	1833.6	0.5	-	0.7	-
	5 <sub>1</sub>	4 <sub>-1</sub>	1838.1	1.5	-	1.8	1.2
	5 <sub>0</sub>	4 <sub>0</sub>	1852.4	0.7	-	0.8	0.5
	5 <sub>-2</sub>	4 <sub>-2</sub>	1892.9	1.0	-	1.1	0.9
	5 <sub>-4</sub>	4 <sub>-4</sub>	1934.6	2.5	-	2.5	2.6
	5 <sub>-5</sub>	4 <sub>-3</sub>	1941.8	7.8	-	7.7	8.0
	5 <sub>-3</sub>	4 <sub>-1</sub>	1948.6	2.3	-	2.2	2.3
	5 <sub>-1</sub>	4 <sub>0</sub>	2001.6	0.5	-	0.5	0.6
Q	5 <sub>3</sub>	5 <sub>1</sub>	1942.7	1.0	-	1.2	0.9
	5 <sub>-2</sub>	5 <sub>-4</sub>	1943.8	0.8	-	0.9	0.7
	5 <sub>0</sub>	5 <sub>-2</sub>	1947.6	0.7	-	0.8	0.6
	5 <sub>-3</sub>	5 <sub>-5</sub>	1956.9	3.5	-	3.8	3.2
	5 <sub>1</sub>	5 <sub>-1</sub>	1962.5	3.1	-	3.3	2.8
	5 <sub>-1</sub>	5 <sub>-3</sub>	1975.2	5.7	-	5.9	5.5
	5 <sub>-3</sub>	5 <sub>-1</sub>	2073.0	5.0	-	4.3	5.8
	5 <sub>-5</sub>	5 <sub>-3</sub>	2097.2	3.6	-	3.0	4.3
	5 <sub>-1</sub>	5 <sub>1</sub>	2111.4	2.8	-	2.3	3.4
	5 <sub>-4</sub>	5 <sub>-2</sub>	2126.7	1.1	-	0.9	1.4
	5 <sub>-2</sub>	5 <sub>0</sub>	2140.3	1.0	-	0.8	1.2
	5 <sub>1</sub>	5 <sub>3</sub>	2182.3	1.4	-	1.1	1.8
	5 <sub>0</sub>	5 <sub>2</sub>	2187.2	0.5	-	-	0.6
	5 <sub>3</sub>	5 <sub>5</sub>	2251.3	0.5	-	-	0.7

## APPX V

TABLE V.2 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J', J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	5 <sub>-2</sub>	6 <sub>-4</sub>	82138.9	0.9	-	0.8	0.9
	5 <sub>-4</sub>	6 <sub>-6</sub>	2142.7	3.1	-	3.0	3.3
	5 <sub>-5</sub>	6 <sub>-5</sub>	2145.6	9.8	-	9.2	10.4
	5 <sub>-3</sub>	6 <sub>-3</sub>	2177.6	4.2	-	3.7	4.8
	5 <sub>-1</sub>	6 <sub>-1</sub>	2239.1	2.7	-	2.1	3.4
	5 <sub>-2</sub>	6 <sub>0</sub>	2275.3	0.9	-	0.6	1.1
	5 <sub>1</sub>	6 <sub>1</sub>	2312.0	2.6	-	1.8	3.5
	5 <sub>0</sub>	6 <sub>2</sub>	2317.1	0.9	-	0.6	1.2
	5 <sub>-5</sub>	6 <sub>-1</sub>	2361.1	0.5	-	-	0.6
	5 <sub>3</sub>	6 <sub>3</sub>	2380.5	2.0	-	1.3	2.9
	5 <sub>2</sub>	6 <sub>4</sub>	2380.7	0.7	-	-	1.0
	5 <sub>5</sub>	6 <sub>5</sub>	2452.3	1.3	-	0.8	1.9
P	6 <sub>3</sub>	5 <sub>3</sub>	1789.8	0.5	-	0.7	-
	6 <sub>1</sub>	5 <sub>1</sub>	1796.1	0.7	-	0.9	0.6
	6 <sub>-1</sub>	5 <sub>-1</sub>	1821.7	1.0	-	1.2	0.8
	6 <sub>-3</sub>	5 <sub>-3</sub>	1868.7	1.9	-	2.0	1.8
	6 <sub>-4</sub>	5 <sub>-2</sub>	1909.0	0.6	-	0.6	0.6
	6 <sub>-5</sub>	5 <sub>-5</sub>	1909.4	5.3	-	5.3	5.4
	6 <sub>-6</sub>	5 <sub>-4</sub>	1913.3	1.8	-	1.8	1.9
Q	6 <sub>-3</sub>	6 <sub>-5</sub>	1917.1	1.4	-	1.6	1.1
	6 <sub>1</sub>	6 <sub>-1</sub>	1923.8	0.7	-	0.9	0.6
	6 <sub>-4</sub>	6 <sub>-6</sub>	1924.9	0.6	-	0.6	0.5

## APPX V

TABLE V.2 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
	6 <sub>-1</sub>	6 <sub>-3</sub>	1926.3	1.4	-	1.6	1.2
	6 <sub>0</sub>	6 <sub>-2</sub>	1948.0	0.7	-	0.8	0.7
	6 <sub>-2</sub>	6 <sub>-4</sub>	1950.5	1.0	-	1.0	0.9
	6 <sub>-4</sub>	6 <sub>-2</sub>	2068.0	0.8	-	0.7	1.0
	6 <sub>-2</sub>	6 <sub>0</sub>	2086.9	0.6	-	0.5	0.7
	6 <sub>-6</sub>	6 <sub>-4</sub>	2108.4	0.6	-	0.5	0.8
	6 <sub>-5</sub>	6 <sub>-3</sub>	2130.1	1.9	-	1.5	2.4
	6 <sub>-3</sub>	6 <sub>-1</sub>	2132.6	1.7	-	1.3	2.2
	6 <sub>-1</sub>	6 <sub>1</sub>	2171.2	1.0	-	0.7	1.3
R	6 <sub>-5</sub>	7 <sub>-7</sub>	2150.6	6.4	-	6.0	6.7
	6 <sub>-6</sub>	7 <sub>-6</sub>	2152.0	2.2	-	2.0	2.3
	6 <sub>-3</sub>	7 <sub>-5</sub>	2152.6	2.0	-	1.8	2.1
	6 <sub>-4</sub>	7 <sub>-4</sub>	2176.9	0.9	-	0.8	1.0
	6 <sub>-2</sub>	7 <sub>-2</sub>	2232.5	0.5	-	-	0.6
	6 <sub>-3</sub>	7 <sub>-1</sub>	2295.8	1.1	-	0.8	1.5
	6 <sub>-1</sub>	7 <sub>1</sub>	2324.0	1.3	-	0.9	1.8
	6 <sub>1</sub>	7 <sub>3</sub>	2385.1	1.0	-	0.6	1.4
	6 <sub>3</sub>	7 <sub>5</sub>	2456.9	0.6	-	-	0.9
P	7 <sub>-5</sub>	6 <sub>-3</sub>	1871.1	1.2	-	1.1	1.2
	7 <sub>-6</sub>	6 <sub>-6</sub>	1881.9	1.0	-	1.1	1.1
	7 <sub>-7</sub>	6 <sub>-5</sub>	1883.9	3.3	-	3.2	3.4
Q	7 <sub>-5</sub>	7 <sub>-7</sub>	1891.5	0.7	-	0.9	0.6

## APPX V

TABLE V.2 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ ( $\text{cm}^{-1}$ )	RELATIVE INTENSITY $[I]_{J_1}^{J_2} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J_2''$	$J_1'$		1:0	0:1	1:1	1:-1
	7 <sub>1</sub>	7 <sub>-1</sub>	81911.6	0.5	-	0.6	-
	7 <sub>-3</sub>	7 <sub>-5</sub>	1919.9	1.2	-	1.3	1.1
	7 <sub>-1</sub>	7 <sub>-3</sub>	1927.8	1.1	-	1.2	1.1
	7 <sub>-3</sub>	7 <sub>-1</sub>	2063.2	0.8	-	0.7	1.0
	7 <sub>-5</sub>	7 <sub>-3</sub>	2068.3	1.0	-	0.8	1.2
	7 <sub>-7</sub>	7 <sub>-5</sub>	2119.4	0.9	-	0.7	1.2
R	7 <sub>-6</sub>	8 <sub>-8</sub>	2156.5	1.3	-	1.2	1.3
	7 <sub>-7</sub>	8 <sub>-7</sub>	2157.1	3.8	-	3.6	4.0
	7 <sub>-5</sub>	8 <sub>-5</sub>	2176.7	1.5	-	1.3	1.6
	7 <sub>-3</sub>	8 <sub>-3</sub>	2222.8	0.7	-	0.5	0.8
	7 <sub>-1</sub>	8 <sub>-1</sub>	2301.3	0.5	-	-	0.6
P	8 <sub>-5</sub>	7 <sub>-5</sub>	1817.7	0.6	-	0.6	0.5
	8 <sub>-7</sub>	7 <sub>-7</sub>	1852.5	1.8	-	1.7	1.8
	8 <sub>-8</sub>	7 <sub>-6</sub>	1853.4	0.6	-	0.6	0.6
Q	8 <sub>-7</sub>	8 <sub>-5</sub>	2137.6	0.5	-	-	0.6
R	8 <sub>-7</sub>	9 <sub>-9</sub>	2160.6	2.0	-	1.9	2.1
	8 <sub>-8</sub>	9 <sub>-8</sub>	2160.9	0.7	-	0.6	0.7
	8 <sub>-5</sub>	9 <sub>-7</sub>	2169.7	0.7	-	0.6	0.7
P	9 <sub>-9</sub>	8 <sub>-7</sub>	1821.6	0.8	-	0.8	0.9
R	9 <sub>-9</sub>	10 <sub>-9</sub>	2163.1	0.9	-	0.9	1.0

APPX. V

TABLE V.3

 $\tilde{C}^1B_1$  Transitions in  $D_2O$  Calculated for Various Ratios  $\langle \mu_z \rangle : \langle \mu_x \rangle$ .

(Electronic interaction)

Branch	IDENTIFICATION		FREQUENCY $\nu(\text{cm}^{-1})$	*RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	0 <sub>0</sub>	1 <sub>1</sub>	80772.8	-	6.7	7.0	6.4
P	1 <sub>1</sub>	0 <sub>0</sub>	729.2	-	3.0	3.0	3.0
Q	1 <sub>0</sub>	1 <sub>-1</sub>	742.4	-	9.1	9.1	9.1
	1 <sub>-1</sub>	1 <sub>0</sub>	758.8	-	4.7	4.9	4.5
R	1 <sub>1</sub>	2 <sub>-2</sub>	761.1	-	1.1	1.0	1.1
	1 <sub>-1</sub>	2 <sub>0</sub>	784.0	-	4.7	4.9	4.5
	1 <sub>1</sub>	2 <sub>2</sub>	798.8	-	4.9	5.3	4.5
	1 <sub>0</sub>	2 <sub>1</sub>	800.9	-	9.0	9.9	8.2
P	2 <sub>1</sub>	1 <sub>0</sub>	697.3	-	3.5	3.3	3.6
	2 <sub>2</sub>	1 <sub>1</sub>	698.7	-	7.8	7.5	8.1
	2 <sub>0</sub>	1 <sub>-1</sub>	713.3	-	7.8	7.8	7.8
	2 <sub>-2</sub>	1 <sub>1</sub>	736.9	-	1.8	1.9	1.7
Q	2 <sub>2</sub>	2 <sub>-1</sub>	716.4	-	2.5	2.3	2.7
	2 <sub>1</sub>	2 <sub>0</sub>	722.5	-	1.9	1.8	2.0
	2 <sub>-1</sub>	2 <sub>-2</sub>	741.7	-	7.4	7.5	7.4
	2 <sub>-2</sub>	2 <sub>-1</sub>	754.6	-	15.6	16.3	15.0
	2 <sub>0</sub>	2 <sub>1</sub>	771.8	-	4.4	4.8	4.0

\*Values of  $[I]_{J'}^{J''} \times 10$  less than 0.5 are not included for $\langle \mu_z \rangle : \langle \mu_x \rangle = 0:1$  and the corresponding cases of 1:0, 1:1 and 1:-1

in the table.

## APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	2 <sub>-1</sub>	2 <sub>2</sub>	80779.4	-	1.6	1.8	1.4
	2 <sub>2</sub>	3 <sub>-1</sub>	756.9	-	1.1	1.0	1.1
	2 <sub>0</sub>	3 <sub>-3</sub>	765.5	-	2.9	2.8	3.0
	2 <sub>-2</sub>	3 <sub>-1</sub>	795.1	-	10.5	11.0	9.9
	2 <sub>0</sub>	3 <sub>1</sub>	805.4	-	11.1	12.0	10.2
	2 <sub>-1</sub>	3 <sub>0</sub>	811.3	-	4.5	4.9	4.1
	2 <sub>2</sub>	3 <sub>3</sub>	825.8	-	11.8	13.4	10.2
	2 <sub>1</sub>	3 <sub>2</sub>	826.3	-	5.9	6.7	5.1
P	3 <sub>2</sub>	2 <sub>1</sub>	664.3	-	7.9	7.2	8.6
	3 <sub>3</sub>	2 <sub>2</sub>	664.5	-	4.0	3.6	4.3
	3 <sub>0</sub>	2 <sub>-1</sub>	680.5	-	6.5	6.2	6.8
	3 <sub>1</sub>	2 <sub>0</sub>	683.9	-	4.2	4.1	4.4
	3 <sub>-1</sub>	2 <sub>-2</sub>	694.8	-	4.1	4.1	4.1
	3 <sub>-3</sub>	2 <sub>0</sub>	725.7	-	1.1	1.2	1.0
	3 <sub>-2</sub>	2 <sub>1</sub>	746.6	-	0.5	0.5	-
Q	3 <sub>3</sub>	3 <sub>0</sub>	696.4	-	1.1	1.0	1.2
	3 <sub>2</sub>	3 <sub>1</sub>	697.9	-	2.3	2.1	2.6
	3 <sub>1</sub>	3 <sub>-2</sub>	707.4	-	1.2	1.1	1.3
	3 <sub>0</sub>	3 <sub>-1</sub>	721.0	-	6.1	5.9	6.4



## APPX. V

TABLE V.3 (Continued)

IDENTIFICATION		FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J', J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$ $J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	$3_{-2}$ $3_{-3}$	740.3	-	19.8	20.0	19.6
	$3_{-3}$ $3_{-2}$	749.2	-	10.5	10.8	10.1
	$3_{-1}$ $3_0$	764.4	-	3.5	3.8	3.2
	$3_{-2}$ $3_1$	780.2	-	3.6	4.1	3.2
	$3_1$ $3_2$	787.7	-	1.5	1.7	1.3
	$3_0$ $3_3$	789.9	-	2.9	3.4	2.5
	$3_0$ $4_{-3}$	748.3	-	0.8	0.8	0.9
	$3_1$ $4_{-2}$	764.8	-	1.2	1.1	1.2
	$3_{-1}$ $4_{-4}$	766.2	-	1.3	1.2	1.3
	$3_{-3}$ $4_{-2}$	806.5	-	4.8	5.1	4.5
	$3_{-1}$ $4_0$	811.0	-	5.8	6.3	5.4
	$3_{-2}$ $4_{-1}$	821.5	-	8.4	9.2	7.6
	$3_1$ $4_2$	831.3	-	5.4	6.1	4.7
	$3_0$ $4_1$	833.3	-	10.8	12.2	9.4
	$3_2$ $4_3$	851.0	-	10.9	12.9	9.0
	$3_3$ $4_4$	850.9	-	5.4	6.5	4.5
P	$4_3$ $3_2$	629.2	-	3.1	2.7	3.6
	$4_4$ $3_3$	629.2	-	6.3	5.5	7.2
	$4_1$ $3_0$	647.2	-	3.4	3.1	3.7
	$4_2$ $3_1$	648.2	-	7.0	6.5	7.6

APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
Q	$4_{-1}$	$3_{-2}$	80661.5	-	2.8	2.7	2.9
	$4_0$	$3_{-1}$	666.8	-	8.6	8.3	8.8
	$4_{-2}$	$3_{-3}$	673.6	-	7.2	7.1	7.2
	$4_{-2}$	$3_1$	713.5	-	1.4	1.6	1.2
	$4_{-4}$	$3_{-1}$	715.9	-	1.7	1.9	1.5
	$4_4$	$4_1$	672.6	-	1.4	1.1	1.6
	$4_3$	$4_2$	672.8	-	0.7	0.6	0.8
	$4_2$	$4_{-1}$	689.5	-	2.8	2.4	3.1
	$4_1$	$4_0$	693.8	-	1.6	1.4	1.8
	$4_0$	$4_{-3}$	694.1	-	1.4	1.2	1.6
	$4_{-1}$	$4_{-2}$	718.9	-	3.7	3.6	3.8
	$4_{-3}$	$4_{-4}$	737.8	-	11.5	11.6	11.3
	$4_{-4}$	$4_{-3}$	743.2	-	24.0	24.7	23.3
	$4_{-2}$	$4_{-1}$	754.8	-	8.5	9.1	7.9
	$4_0$	$4_1$	779.1	-	4.0	4.6	3.5
	$4_{-3}$	$4_0$	782.6	-	1.4	1.6	1.2
	$4_{-1}$	$4_2$	785.4	-	2.0	2.3	1.7
	$4_2$	$4_3$	801.3	-	1.9	2.3	1.5
	$4_1$	$4_4$	801.7	-	1.0	1.2	0.8
R	$4_{-1}$	$5_{-4}$	748.1	-	0.5	-	0.5

APPX. V

TABLE V.3 (Continued)

IDENTIFICATION		FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\alpha''}$ $J'_{\alpha'}$		1:0	0:1	1:1	1:-1
	$4_2$ $5_{-1}$	80750.8	-	0.9	0.8	1.0
	$4_{-2}$ $5_{-5}$	763.2	-	1.8	1.7	2.0
	$4_0$ $5_{-3}$	769.6	-	3.0	2.9	3.2
	$4_{-2}$ $5_{-1}$	816.2	-	11.0	11.8	10.2
	$4_{-4}$ $5_{-3}$	818.7	-	7.8	8.4	7.2
	$4_{-3}$ $5_{-2}$	831.6	-	3.6	4.0	3.3
	$4_0$ $5_1$	834.2	-	9.4	10.5	8.3
	$4_{-1}$ $5_0$	839.5	-	4.7	5.3	4.1
	$4_2$ $5_3$	855.6	-	9.0	10.7	7.5
	$4_1$ $5_2$	856.0	-	4.5	5.4	3.8
	$4_4$ $5_5$	874.5	-	7.9	9.8	6.2
	$4_3$ $5_4$	874.5	-	4.0	4.9	3.1
P	$5_4$ $4_3$	592.6	-	3.9	3.3	4.7
	$5_5$ $4_4$	592.6	-	2.0	1.6	2.3
	$5_2$ $4_1$	611.0	-	3.9	4.3	5.6
	$5_3$ $4_2$	611.1	-	2.5	2.2	2.8
	$5_0$ $4_{-1}$	628.2	-	5.6	5.1	6.0
	$5_1$ $4_0$	630.6	-	3.0	2.8	3.2
	$5_{-2}$ $4_{-3}$	640.6	-	4.5	4.3	4.8
	$5_{-1}$ $4_{-2}$	646.8	-	3.8	3.7	3.9
	$5_{-3}$ $4_{-4}$	650.0	-	2.7	2.7	2.8

APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_y \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
Q	$5_{-3}$	$4_0$	80694.8	-	0.8	0.9	0.7
	$5_{-5}$	$4_{-2}$	707.8	-	0.6	0.7	0.5
	$5_{-2}$	$4_1$	725.6	-	0.5	0.8	-
	$5_{-4}$	$4_{-1}$	725.6	-	0.7	0.6	0.6
	$5_4$	$5_3$	646.9	-	0.7	0.5	0.8
	$5_3$	$5_0$	665.3	-	0.9	0.7	1.0
	$5_2$	$5_1$	666.1	-	1.8	1.5	2.1
	$5_1$	$5_{-2}$	679.7	-	1.1	1.0	1.3
	$5_0$	$5_{-1}$	689.5	-	3.3	3.0	3.6
	$5_{-2}$	$5_{-3}$	716.1	-	8.0	7.9	8.2
	$5_{-4}$	$5_{-5}$	734.0	-	23.5	23.8	23.1
	$5_{-5}$	$5_{-4}$	736.9	-	12.1	12.4	11.8
	$5_{-3}$	$5_{-2}$	743.8	-	4.6	4.9	4.3
	$5_{-1}$	$5_0$	767.4	-	2.1	2.4	1.8
	$5_{-2}$	$5_1$	780.7	-	3.7	4.3	3.2
	$5_{-4}$	$5_{-1}$	787.0	-	1.7	1.9	1.4
	$5_1$	$5_2$	792.8	-	1.3	1.5	1.0
	$5_0$	$5_3$	794.3	-	2.6	3.1	2.1
	$5_3$	$5_4$	812.8	-	0.5	0.7	-
	$5_2$	$5_5$	812.8	-	1.0	1.3	0.8

## APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J', J''}^J \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	5 <sub>0</sub>	6 <sub>3</sub>	80744.2	-	0.8	0.7	0.9
	5 <sub>-2</sub>	6 <sub>-5</sub>	745.5	-	0.8	0.7	0.9
	5 <sub>-3</sub>	6 <sub>-6</sub>	757.0	-	0.6	0.5	0.7
	5 <sub>1</sub>	6 <sub>-2</sub>	757.5	-	0.7	0.6	0.7
	5 <sub>-1</sub>	6 <sub>-4</sub>	770.6	-	1.4	1.4	1.5
	5 <sub>-3</sub>	6 <sub>-2</sub>	821.7	-	4.5	4.9	4.2
	5 <sub>-5</sub>	6 <sub>-4</sub>	831.6	-	2.9	3.2	2.7
	5 <sub>-1</sub>	6 <sub>0</sub>	834.8	-	3.9	4.4	3.5
	5 <sub>-4</sub>	6 <sub>-3</sub>	841.7	-	5.8	6.5	5.2
	5 <sub>-2</sub>	6 <sub>-1</sub>	845.3	-	7.5	8.6	6.6
	5 <sub>1</sub>	6 <sub>2</sub>	858.2	-	3.5	4.2	3.0
	5 <sub>0</sub>	6 <sub>1</sub>	859.6	-	7.1	8.4	6.0
	5 <sub>3</sub>	6 <sub>4</sub>	877.9	-	3.0	3.8	2.4
	5 <sub>2</sub>	6 <sub>3</sub>	877.9	-	6.1	7.5	4.8
	5 <sub>5</sub>	6 <sub>6</sub>	896.6	-	2.4	3.0	1.8
	5 <sub>4</sub>	6 <sub>5</sub>	896.6	-	4.7	6.1	3.5
P	6 <sub>5</sub>	5 <sub>4</sub>	554.6	-	1.0	0.8	1.2
	6 <sub>6</sub>	5 <sub>5</sub>	554.6	-	2.0	1.6	2.5
	6 <sub>3</sub>	5 <sub>2</sub>	573.0	-	1.4	1.2	1.7
	6 <sub>4</sub>	5 <sub>3</sub>	573.0	-	2.9	2.4	3.4

APPX. V

TABLE V.3 (Continued)

IDENTIFICATION		FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$ $J'_{\tau'}$		1:0	0:1	1:1	1:-1
	$6_1$ $5_0$	80591.1	-	1.9	1.6	2.1
	$6_2$ $5_1$	591.6	-	3.8	3.3	4.2
	$6_{-1}$ $5_{-2}$	607.2	-	2.1	2.0	2.3
	$6_0$ $5_{-1}$	611.4	-	5.0	4.7	5.3
	$6_{-3}$ $5_{-4}$	617.8	-	1.7	1.6	1.8
	$6_{-2}$ $5_{-3}$	624.0	-	5.9	5.8	6.0
	$6_{-4}$ $5_{-5}$	624.3	-	3.8	3.7	4.0
	$6_{-4}$ $5_{-1}$	677.3	-	1.3	1.5	1.1
	$6_{-2}$ $5_1$	688.6	-	0.6	0.7	0.5
	$6_{-6}$ $5_{-3}$	701.0	-	0.7	0.9	0.6
Q	$6_4$ $6_1$	638.3	-	0.8	0.7	1.0
	$6_2$ $6_{-1}$	656.1	-	1.6	1.3	1.8
	$6_1$ $6_0$	658.5	-	0.8	0.7	1.0
	$6_0$ $6_{-3}$	666.1	-	1.4	1.2	1.7
	$6_{-1}$ $6_{-2}$	685.0	-	1.5	1.4	1.6
	$6_{-3}$ $6_{-4}$	712.4	-	4.0	3.9	4.0
	$6_{-5}$ $6_{-6}$	728.9	-	10.8	11.0	10.6
	$6_{-6}$ $6_{-5}$	730.4	-	21.9	22.4	21.4
	$6_{-4}$ $6_{-3}$	732.0	-	9.0	9.4	8.6
	$6_{-2}$ $6_{-1}$	753.1	-	3.8	4.2	3.4
	$6_{-3}$ $6_0$	776.7	-	1.4	1.7	1.2
	$6_0$ $6_1$	781.4	-	2.4	2.8	2.0

## APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	$6_{-1}$	$6_2$	80785.7	-	1.2	1.5	1.0
	$6_{-5}$	$6_{-2}$	793.5	-	0.5	0.5	-
	$6_2$	$6_3$	803.4	-	1.3	1.7	1.0
	$6_1$	$6_4$	803.7	-	0.7	0.8	0.5
	$6_4$	$6_5$	822.7	-	0.5	0.6	-
	$6_2$	$7_{-1}$	737.1	-	0.5	-	0.5
	$6_{-4}$	$7_{-7}$	748.7	-	0.8	0.7	0.9
	$6_0$	$7_{-3}$	762.1	-	1.5	1.4	1.6
	$6_{-2}$	$7_{-5}$	767.5	-	2.1	2.0	2.2
	$6_{-4}$	$7_{-3}$	828.1	-	6.5	7.1	6.0
	$6_{-2}$	$7_{-1}$	834.1	-	6.2	6.8	5.5
	$6_{-6}$	$7_{-5}$	844.5	-	4.3	4.8	3.8
	$6_{-3}$	$7_{-2}$	850.7	-	2.8	3.2	2.5
	$6_{-5}$	$7_{-4}$	851.6	-	2.2	2.5	1.9
	$6_0$	$7_1$	858.2	-	5.2	6.1	4.4
	$6_{-1}$	$7_0$	862.0	-	2.7	3.1	2.2
	$6_2$	$7_3$	879.5	-	4.4	5.5	3.5
	$6_1$	$7_2$	879.8	-	2.2	2.7	1.8
	$6_4$	$7_5$	898.6	-	3.4	4.4	2.6
	$6_3$	$7_4$	898.6	-	1.7	2.2	1.3
	$6_6$	$7_7$	917.4	-	2.3	3.1	1.7

## APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J', J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
P	6 <sub>5</sub>	7 <sub>6</sub>	917.4	-	1.2	1.6	0.8
	7 <sub>6</sub>	6 <sub>5</sub>	515.2	-	0.9	0.6	1.1
	7 <sub>4</sub>	6 <sub>3</sub>	533.5	-	1.4	1.1	1.7
	7 <sub>5</sub>	6 <sub>4</sub>	533.5	-	0.7	0.5	0.8
	7 <sub>2</sub>	6 <sub>1</sub>	551.8	-	2.0	1.7	2.3
	7 <sub>3</sub>	6 <sub>2</sub>	551.8	-	1.0	0.8	1.2
	7 <sub>0</sub>	6 <sub>-1</sub>	569.5	-	2.7	2.4	3.0
	7 <sub>1</sub>	6 <sub>0</sub>	570.7	-	1.4	1.2	1.5
	7 <sub>-2</sub>	6 <sub>-3</sub>	584.1	-	3.0	2.8	3.3
	7 <sub>-1</sub>	6 <sub>-2</sub>	589.8	-	1.9	1.8	2.0
	7 <sub>-4</sub>	6 <sub>-5</sub>	593.4	-	2.3	2.2	2.5
	7 <sub>-5</sub>	6 <sub>-6</sub>	597.4	-	1.3	1.2	1.3
	7 <sub>-3</sub>	6 <sub>-4</sub>	598.5	-	2.0	2.0	2.1
Q	7 <sub>2</sub>	7 <sub>1</sub>	628.5	-	0.7	0.6	0.9
	7 <sub>1</sub>	7 <sub>-2</sub>	644.7	-	0.6	0.5	0.7
	7 <sub>0</sub>	7 <sub>-1</sub>	650.4	-	1.3	1.1	1.5
	7 <sub>-2</sub>	7 <sub>-3</sub>	680.1	-	2.6	2.4	2.8
	7 <sub>-4</sub>	7 <sub>-5</sub>	707.5	-	7.2	7.1	7.2
	7 <sub>-5</sub>	7 <sub>-4</sub>	720.2	-	4.0	4.1	3.9
	7 <sub>-6</sub>	7 <sub>-7</sub>	722.5	-	18.1	18.5	17.8
	7 <sub>-7</sub>	7 <sub>-6</sub>	723.3	-	9.1	9.3	8.9



## APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J', J''}^{\nu} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
	$7_{-3}$	$7_{-2}$	80736.7	-	1.6	1.8	1.5
	$7_{-1}$	$7_0$	766.8	-	1.0	1.1	0.8
	$7_{-4}$	$7_{-1}$	774.1	-	1.8	2.1	1.5
	$7_{-2}$	$7_1$	776.2	-	2.0	2.3	1.6
	$7_1$	$7_2$	792.0	-	0.6	0.8	0.5
	$7_0$	$7_3$	792.9	-	1.2	1.5	1.0
	$7_{-6}$	$7_{-3}$	801.9	-	0.5	0.6	-
	$7_2$	$7_5$	812.1	-	0.6	0.8	-
R	$7_{-2}$	$8_{-5}$	739.6	-	0.6	0.5	0.7
	$7_{-3}$	$8_{-6}$	760.3	-	0.6	0.6	0.7
	$7_{-1}$	$8_{-4}$	763.5	-	0.7	0.7	0.8
	$7_{-3}$	$8_{-2}$	833.0	-	2.2	2.5	2.0
	$7_{-5}$	$8_{-4}$	835.7	-	2.1	2.4	1.9
	$7_{-1}$	$8_0$	855.3	-	1.8	2.1	1.5
	$7_{-4}$	$8_{-3}$	856.0	-	4.0	4.6	3.4
	$7_{-7}$	$8_{-6}$	856.7	-	1.5	1.7	1.3
	$7_{-6}$	$8_{-5}$	861.3	-	3.1	3.6	2.7
	$7_{-2}$	$8_{-1}$	863.4	-	3.7	4.4	3.1
	$7_1$	$8_2$	879.2	-	1.5	1.9	1.2
	$7_0$	$8_1$	880.1	-	3.1	3.7	2.4
	$7_3$	$8_4$	898.9	-	1.2	1.5	0.9

## APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J', J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
P	$7_2$	$8_3$	899.0	-	2.3	2.9	1.7
	$7_5$	$8_6$	917.9	-	0.8	1.0	0.6
	$7_4$	$8_5$	917.9	-	1.6	2.1	1.1
	$7_7$	$8_8$	936.9	-	0.5	0.7	-
	$7_6$	$8_7$	936.9	-	1.0	1.4	0.7
	$8_6$	$7_5$	492.6	-	0.5	-	0.7
	$8_4$	$7_3$	510.9	-	0.9	0.7	1.1
	$8_1$	$7_0$	528.9	-	0.7	0.6	0.8
	$8_2$	$7_1$	529.1	-	1.3	1.1	1.5
	$8_{-1}$	$7_{-2}$	545.9	-	0.9	0.8	1.0
	$8_0$	$7_{-1}$	548.4	-	1.9	1.7	2.1
	$8_{-3}$	$7_{-4}$	559.2	-	1.0	0.9	1.1
	$8_{-2}$	$7_{-3}$	565.4	-	2.6	2.5	2.7
	$8_{-5}$	$7_{-6}$	567.6	-	0.8	0.7	0.8
	$8_{-6}$	$7_{-7}$	569.8	-	1.6	1.5	1.7
	$8_{-4}$	$7_{-5}$	570.5	-	2.5	2.4	2.6
	$8_{-4}$	$7_{-1}$	637.1	-	0.5	0.6	-
	$8_{-6}$	$7_{-3}$	649.2	-	0.5	0.6	-
Q	$8_2$	$8_{-1}$	616.4	-	0.5	-	0.7
	$8_0$	$8_{-3}$	630.2	-	0.7	0.5	0.8
	$8_{-1}$	$8_{-2}$	642.3	-	0.5	-	0.5
	$8_{-3}$	$8_{-4}$	674.7	-	1.0	1.0	1.1

APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J',J''}^J \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	8 <sub>-5</sub>	8 <sub>-6</sub>	80701.0	-	3.0	3.0	3.0
	8 <sub>-6</sub>	8 <sub>-5</sub>	708.6	-	6.4	6.5	6.2
	8 <sub>-7</sub>	8 <sub>-8</sub>	715.2	-	7.0	7.2	6.9
	8 <sub>-8</sub>	8 <sub>-7</sub>	715.5	-	14.1	14.4	13.8
	8 <sub>-4</sub>	8 <sub>-3</sub>	719.0	-	2.6	2.8	2.4
	8 <sub>-2</sub>	8 <sub>-1</sub>	748.7	-	1.4	1.6	1.2
	8 <sub>-3</sub>	8 <sub>0</sub>	766.5	-	0.7	0.8	0.6
	8 <sub>-5</sub>	8 <sub>-2</sub>	773.7	-	0.5	0.6	-
	8 <sub>0</sub>	8 <sub>1</sub>	778.0	-	0.9	1.2	0.7
	8 <sub>-1</sub>	8 <sub>2</sub>	780.5	-	0.5	0.6	-
	8 <sub>2</sub>	8 <sub>3</sub>	799.6	-	0.5	0.7	-
	8 <sub>0</sub>	9 <sub>-3</sub>	743.8	-	0.5	-	0.5
	8 <sub>-4</sub>	9 <sub>-7</sub>	749.8	-	0.7	0.6	0.8
	8 <sub>-2</sub>	9 <sub>-5</sub>	760.9	-	1.1	1.0	1.3
	8 <sub>-4</sub>	9 <sub>-3</sub>	832.6	-	2.9	3.2	2.6
	8 <sub>-6</sub>	9 <sub>-5</sub>	844.6	-	2.6	2.9	2.3
	8 <sub>-2</sub>	9 <sub>-1</sub>	849.8	-	2.3	2.6	2.0
	8 <sub>-5</sub>	9 <sub>-4</sub>	861.3	-	1.3	1.5	1.1
	8 <sub>-3</sub>	9 <sub>-2</sub>	864.3	-	1.2	1.4	1.0
	8 <sub>-8</sub>	9 <sub>-7</sub>	867.9	-	2.0	2.3	1.7
	8 <sub>-7</sub>	9 <sub>-6</sub>	870.6	-	1.0	1.2	0.9
	8 <sub>0</sub>	9 <sub>1</sub>	876.5	-	1.9	2.3	1.5

APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_J^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
P	8 <sub>-1</sub>	9 <sub>0</sub>	80378.8	-	1.0	1.2	0.8
	8 <sub>2</sub>	9 <sub>3</sub>	897.5	-	1.5	1.9	1.1
	8 <sub>1</sub>	9 <sub>2</sub>	897.7	-	0.7	0.9	0.6
	8 <sub>4</sub>	9 <sub>5</sub>	916.9	-	1.0	1.3	0.7
	8 <sub>3</sub>	9 <sub>4</sub>	916.9	-	0.5	0.7	-
	8 <sub>6</sub>	9 <sub>7</sub>	936.0	-	0.6	0.8	-
	9 <sub>2</sub>	8 <sub>1</sub>	486.6	-	0.5	-	0.7
	9 <sub>0</sub>	8 <sub>-1</sub>	504.4	-	0.8	0.7	0.9
	9 <sub>-2</sub>	8 <sub>-3</sub>	520.5	-	1.1	1.0	1.2
	9 <sub>-1</sub>	8 <sub>-2</sub>	524.3	-	0.6	0.6	0.7
	9 <sub>-4</sub>	8 <sub>-5</sub>	532.4	-	1.2	1.1	1.3
	9 <sub>-3</sub>	8 <sub>-4</sub>	538.1	-	0.8	0.8	0.8
	9 <sub>-5</sub>	8 <sub>-6</sub>	540.5	-	0.7	0.7	0.8
	9 <sub>-6</sub>	8 <sub>-7</sub>	540.5	-	0.9	0.9	1.0
	9 <sub>-7</sub>	8 <sub>-8</sub>	541.7	-	0.5	-	0.5
Q	9 <sub>-2</sub>	9 <sub>-3</sub>	634.1	-	0.6	0.6	0.7
	9 <sub>-4</sub>	9 <sub>-5</sub>	668.4	-	1.6	1.5	1.6
	9 <sub>-6</sub>	9 <sub>-7</sub>	692.9	-	4.5	4.5	4.4
	9 <sub>-7</sub>	9 <sub>-6</sub>	697.2	-	2.3	2.4	2.3
	9 <sub>-5</sub>	9 <sub>-4</sub>	700.8	-	1.0	1.0	0.9
	9 <sub>-8</sub>	9 <sub>-9</sub>	706.8	-	10.2	10.4	10.0
	9 <sub>-9</sub>	9 <sub>-8</sub>	707.0	-	5.1	5.2	5.0

APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	$9_{-3}$	$9_{-2}$	80727.7	-	0.5	0.5	-
	$9_{-4}$	$9_{-1}$	757.4	-	0.8	1.0	0.7
	$9_{-2}$	$9_1$	766.8	-	0.7	0.8	0.5
	$9_{-6}$	$9_{-3}$	775.7	-	0.5	0.6	-
	$9_{-5}$	$10_{-4}$	833.6	-	0.9	1.0	0.8
	$9_{-3}$	$10_{-2}$	842.7	-	0.7	0.8	0.6
	$9_{-7}$	$10_{-6}$	854.1	-	0.8	0.9	0.7
	$9_{-4}$	$10_{-3}$	866.6	-	1.6	1.9	1.4
	$9_{-6}$	$10_{-5}$	864.7	-	1.5	1.8	1.2
	$9_{-1}$	$10_0$	870.9	-	0.6	0.7	0.5
	$9_{-2}$	$10_{-1}$	876.3	-	1.2	1.5	1.0
	$9_{-9}$	$10_{-8}$	877.9	-	0.7	0.8	0.6
	$9_{-8}$	$10_{-7}$	879.4	-	1.3	1.6	1.1
	$9_0$	$10_1$	894.7	-	0.9	1.1	0.7
	$9_2$	$10_3$	914.2	-	0.6	0.8	-
P	$10_0$	$9_{-1}$	479.2	-	0.5	-	0.6
	$10_{-2}$	$9_{-3}$	497.9	-	0.8	0.7	0.8
	$10_{-4}$	$9_{-5}$	508.2	-	0.9	0.9	1.0
	$10_{-6}$	$9_{-7}$	509.3	-	0.8	0.7	0.8
	$10_{-8}$	$9_{-9}$	513.0	-	0.6	0.5	0.6

## APPX. V

TABLE V.3 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
O	$10_{-5}$	$10_{-6}$	80661.0	-	0.6	0.5	0.6
	$10_{-6}$	$10_{-5}$	683.0	-	1.4	1.4	1.3
	$10_{-7}$	$10_{-8}$	683.3	-	1.5	1.6	1.5
	$10_{-8}$	$10_{-7}$	685.6	-	3.2	3.2	3.1
	$10_{-9}$	$10_{-10}$	697.5	-	3.5	3.5	3.4
	$10_{-10}$	$10_{-9}$	697.6	-	6.9	7.1	6.8
	$10_{-4}$	$10_{-3}$	704.5	-	0.6	0.6	0.5
R	$10_{-4}$	$11_{-3}$	835.1	-	0.8	0.9	0.7
	$10_{-6}$	$11_{-5}$	836.4	-	0.9	1.0	0.8
	$10_{-2}$	$11_{-1}$	862.2	-	0.6	0.7	0.5
	$10_{-8}$	$11_{-7}$	863.2	-	0.9	1.1	0.8
	$10_{-7}$	$11_{-6}$	871.9	-	0.5	0.6	-
	$10_{-10}$	$11_{-9}$	886.7	-	0.8	1.0	0.7
	$10_0$	$11_1$	888.8	-	0.5	0.6	-

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TABLE V.4

$\tilde{D}^1A_1$  Transitions in  $D_2O$  Calculated for Various Ratio  $\langle \mu_z \rangle : \langle \mu_x \rangle$   
(Electronic interaction)

Branch	IDENTIFICATION		FREQUENCY $\nu$ (cm <sup>-1</sup> )	*RELATIVE INTENSITY $[I]_{J', J''}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	0 <sub>0</sub>	1 <sub>0</sub>	82095.33	6.7	-	6.4	7.0
P	1 <sub>0</sub>	0 <sub>0</sub>	2054.6	6.0	-	6.0	6.0
Q	1 <sub>1</sub>	1 <sub>-1</sub>	2063.0	4.5	-	4.5	4.5
	1 <sub>-1</sub>	1 <sub>1</sub>	2085.2	4.7	-	4.5	4.9
R	1 <sub>0</sub>	2 <sub>-2</sub>	2086.6	3.9	-	3.8	3.9
	1 <sub>-1</sub>	2 <sub>-1</sub>	2102.7	4.7	-	4.5	4.9
	1 <sub>1</sub>	2 <sub>1</sub>	2127.2	4.5	-	4.1	4.9
	1 <sub>0</sub>	2 <sub>2</sub>	2129.9	8.2	-	7.4	9.0
P	2 <sub>2</sub>	1 <sub>0</sub>	2021.2	6.0	-	6.3	5.7
	2 <sub>1</sub>	1 <sub>1</sub>	2023.6	3.5	-	3.6	3.3
	2 <sub>-1</sub>	1 <sub>-1</sub>	2043.6	4.1	-	4.0	4.1
	2 <sub>-2</sub>	1 <sub>0</sub>	2059.4	3.9	-	3.8	4.0
Q	2 <sub>1</sub>	2 <sub>-1</sub>	2041.2	1.9	-	2.0	1.8
	2 <sub>2</sub>	2 <sub>0</sub>	2046.6	5.4	-	5.6	5.3
	2 <sub>0</sub>	2 <sub>-2</sub>	2057.5	11.8	-	11.9	11.8
	2 <sub>-2</sub>	2 <sub>0</sub>	2084.8	12.1	-	11.5	12.7
	2 <sub>0</sub>	2 <sub>2</sub>	2100.8	5.6	-	5.1	6.1
	2 <sub>-1</sub>	2 <sub>1</sub>	2107.8	2.3	-	2.1	2.5

\*Values of  $[I]_{J', J''}^{J''} \times 10$  less than 0.5 are not included for

$\langle \mu_z \rangle : \langle \mu_x \rangle = 1:0$  and the corresponding cases of 1:1, 0:1 and 1:-1 in this table.

## APPX. V

TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_y \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	$2_2$	$3_{-2}$	82069.8	0.5	-	0.5	-
	$2_1$	$3_{-1}$	2082.1	0.5	-	0.6	0.5
	$2_{-1}$	$3_{-3}$	2095.9	3.9	-	3.9	4.0
	$2_{-2}$	$3_{-2}$	2108.0	11.9	-	11.3	12.4
	$2_0$	$3_0$	2132.7	8.7	-	7.9	9.5
	$2_{-1}$	$3_1$	2141.3	3.3	-	2.9	3.6
	$2_2$	$3_2$	2161.5	11.2	-	9.7	12.8
	$2_1$	$3_3$	2162.0	5.6	-	4.9	6.4
P	$3_3$	$2_1$	1992.9	3.7	-	4.1	33.3
	$3_2$	$2_2$	1993.2	7.5	-	8.2	6.8
	$3_1$	$2_{-1}$	2002.6	2.0	-	2.2	1.9
	$3_0$	$2_0$	2010.7	6.5	-	6.8	6.2
	$3_{-2}$	$2_{-2}$	2032.3	9.7	-	9.7	9.7
	$3_{-3}$	$2_{-1}$	2044.3	3.8	-	3.7	3.9
	$3_{-1}$	$2_1$	2060.9	0.6	-	0.5	0.6
	$3_{-2}$	$2_2$	2075.6	0.7	-	0.6	0.7
Q	$3_2$	$3_0$	2025.2	3.1	-	3.3	2.9
	$3_3$	$3_1$	2026.4	1.6	-	1.7	1.5
	$3_0$	$3_{-2}$	2033.9	5.3	-	5.6	5.0
	$3_1$	$3_{-1}$	2043.5	4.7	-	4.8	4.6



APPX. V

TABLE V.4 (Continued)

IDENTIFICATION		FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J_1}^{J_2} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J_2'' \quad J_1'$		1:0	0:1	1:1	1:-1
R	$3_{-1} \quad 3_{-3}$	82049.0	5.8	-	5.9	5.8
	$3_{-3} \quad 3_{-1}$	2085.2	5.7	-	5.3	6.0
	$3_{-1} \quad 3_1$	2094.4	4.5	-	4.1	4.8
	$3_{-2} \quad 3_0$	2107.5	6.1	-	5.5	6.8
	$3_1 \quad 3_3$	2123.5	1.9	-	1.6	2.1
	$3_0 \quad 3_2$	2125.7	3.8	-	3.3	4.2
	$3_0 \quad 4_{-2}$	2092.0	2.3	-	2.3	2.3
	$3_{-2} \quad 4_{-4}$	2103.9	11.2	-	10.9	11.5
	$3_{-3} \quad 4_{-3}$	2111.9	6.8	-	6.6	7.1
	$3_{-1} \quad 4_{-1}$	2135.8	4.2	-	3.8	4.6
	$3_{-2} \quad 4_0$	2154.0	4.6	-	4.1	5.2
	$3_1 \quad 4_1$	2166.8	4.6	-	4.0	5.3
	$3_0 \quad 4_2$	2169.2	9.3	-	8.0	10.7
	$3_3 \quad 4_3$	2196.5	5.3	-	4.3	6.3
	$3_2 \quad 4_4$	2196.6	10.5	-	8.7	12.6
P	$4_4 \quad 3_2$	1965.0	6.0	-	6.9	5.2
	$4_3 \quad 3_3$	1965.0	3.0	-	3.4	2.6
	$4_2 \quad 3_0$	1975.5	5.5	-	6.1	5.0
	$4_1 \quad 3_1$	1977.2	2.9	-	3.2	2.6
	$4_0 \quad 3_{-2}$	1979.7	2.2	-	2.4	2.0
	$4_{-1} \quad 3_{-1}$	1997.6	2.9	-	3.1	2.8

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TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
Q	$4_{-3}$	$3_{-3}$	2020.6	5.3	-	5.3	5.3
	$4_{-4}$	$3_{-2}$	2028.8	10.1	-	9.9	10.3
	$4_{-2}$	$3_0$	2040.9	2.4	-	2.3	2.5
	$4_{-3}$	$3_1$	2066.0	0.5	-	-	0.5
	$4_0$	$3_2$	2071.4	0.5	-	-	0.5
	$4_3$	$4_1$	2008.4	0.9	-	1.0	0.8
	$4_4$	$4_2$	2008.5	1.8	-	2.1	1.6
	$4_1$	$4_{-1}$	2018.6	2.2	-	2.4	2.1
	$4_2$	$4_0$	2022.0	5.0	-	5.4	4.7
	$4_{-1}$	$4_{-3}$	2024.3	2.7	-	2.8	2.5
	$4_{-2}$	$4_{-4}$	2037.3	9.4	-	9.7	9.2
	$4_0$	$4_{-2}$	2037.8	11.3	-	11.6	11.1
	$4_{-4}$	$4_{-2}$	2086.9	8.7	-	8.1	9.4
	$4_{-2}$	$4_0$	2087.4	10.2	-	9.4	11.1
	$4_{-3}$	$4_{-1}$	2107.4	3.1	-	2.7	3.4
	$4_0$	$4_2$	2115.0	5.2	-	4.6	5.9
	$4_{-1}$	$4_1$	2121.0	2.6	-	2.3	3.0
	$4_2$	$4_4$	2146.9	2.4	-	2.0	2.8
	$4_1$	$4_3$	2147.3	1.2	-	1.0	1.4
R	$4_2$	$5_{-2}$	2071.3	0.5	-	0.6	0.5
	$4_{-1}$	$5_{-3}$	2101.0	1.7	-	1.7	1.7

## APPX. V

TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
	$4_{-3}$	$5_{-5}$	82110.4	6.5	-	6.4	6.7
	$4_{-4}$	$5_{-4}$	2115.1	14.4	-	13.9	15.0
	$4_{-2}$	$5_{-2}$	2136.7	7.8	-	7.1	8.5
	$4_{-3}$	$5_{-1}$	2168.6	1.4	-	1.2	1.6
	$4_0$	$5_0$	2169.2	7.2	-	6.2	8.3
	$4_{-1}$	$5_1$	2176.0	3.6	-	3.1	4.1
	$4_2$	$5_2$	2201.2	8.2	-	6.7	9.8
	$4_1$	$5_3$	2201.6	4.1	-	3.4	4.9
	$4_{-4}$	$5_0$	2218.4	0.5	-	-	0.6
	$4_4$	$5_4$	2232.6	7.7	-	6.1	9.6
	$4_3$	$5_5$	2232.6	3.9	-	3.0	4.8
P	$5_5$	$4_3$	1938.2	1.9	-	2.3	1.6
	$5_4$	$4_4$	1938.2	3.8	-	4.5	3.1
	$5_3$	$4_1$	1946.7	2.2	-	2.5	1.9
	$5_2$	$4_2$	1946.9	4.4	-	5.0	3.7
	$5_{-1}$	$4_{-3}$	1952.2	0.5	-	0.6	0.5
	$5_1$	$4_{-1}$	1955.5	1.8	-	2.0	1.6
	$5_0$	$4_0$	1960.7	4.3	-	4.8	3.9
	$5_{-2}$	$4_{-2}$	1984.3	5.2	-	5.4	5.0
	$5_{-4}$	$4_{-4}$	2008.1	10.7	-	10.7	10.8
	$5_{-5}$	$4_{-3}$	2013.2	5.4	-	5.3	5.5

## APPX. V

TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
Q	5 <sub>-3</sub>	4 <sub>-1</sub>	82019.6	1.7	-	1.6	1.7
	5 <sub>-4</sub>	4 <sub>0</sub>	2058.2	0.8	-	0.7	0.9
	5 <sub>-2</sub>	4 <sub>2</sub>	2061.6	0.8	-	0.8	0.9
	5 <sub>4</sub>	5 <sub>2</sub>	1992.5	0.9	-	1.1	0.8
	5 <sub>5</sub>	5 <sub>3</sub>	1992.5	0.5	-	0.5	-
	5 <sub>2</sub>	5 <sub>0</sub>	2001.1	2.6	-	2.9	2.3
	5 <sub>3</sub>	5 <sub>1</sub>	2001.7	1.3	-	1.5	1.2
	5 <sub>0</sub>	5 <sub>-2</sub>	2010.0	4.7	-	5.1	4.3
	5 <sub>-2</sub>	5 <sub>-4</sub>	2012.5	4.6	-	4.9	4.2
	5 <sub>1</sub>	5 <sub>-1</sub>	2016.6	3.0	-	3.1	2.8
	5 <sub>-3</sub>	5 <sub>-5</sub>	2022.6	3.4	-	3.5	3.2
	5 <sub>-1</sub>	5 <sub>-3</sub>	2028.9	5.4	-	5.5	5.3
	5 <sub>-3</sub>	5 <sub>-1</sub>	2080.8	4.7	-	4.3	5.1
	5 <sub>-5</sub>	5 <sub>-3</sub>	2089.9	3.1	-	2.8	3.4
	5 <sub>-1</sub>	5 <sub>1</sub>	2103.9	2.7	-	2.4	3.0
	5 <sub>-4</sub>	5 <sub>-2</sub>	2107.5	5.3	-	4.6	5.9
	5 <sub>-2</sub>	5 <sub>0</sub>	2115.8	5.3	-	4.6	6.0
	5 <sub>1</sub>	5 <sub>3</sub>	2138.4	1.6	-	1.3	1.9
	5 <sub>0</sub>	5 <sub>2</sub>	2139.9	3.2	-	2.7	3.8
	5 <sub>3</sub>	5 <sub>5</sub>	2170.9	0.7	-	0.5	0.8
	5 <sub>2</sub>	5 <sub>4</sub>	2170.9	1.3	-	1.0	1.6

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TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	$5_0$	$6_{-2}$	82087.8	1.0	-	1.0	1.0
	$5_{-2}$	$6_{-4}$	2109.0	4.1	-	4.0	4.2
	$5_{-4}$	$6_{-6}$	2115.3	13.2	-	12.8	13.6
	$5_{-5}$	$6_{-5}$	2117.9	6.9	-	6.7	7.2
	$5_{-3}$	$6_{-3}$	2135.9	3.5	-	3.3	3.8
	$5_{-1}$	$6_{-1}$	2168.6	2.7	-	2.3	3.1
	$5_{-4}$	$6_{-2}$	2185.2	1.7	-	1.4	1.9
	$5_{-2}$	$6_0$	2183.0	5.1	-	4.3	5.9
	$5_1$	$6_1$	2203.7	3.0	-	2.4	3.6
	$5_0$	$6_2$	2205.3	6.1	-	4.9	7.3
	$5_3$	$6_3$	2236.0	2.8	-	2.2	3.5
	$5_2$	$6_4$	2236.0	5.7	-	4.4	7.1
	$5_5$	$6_5$	2269.9	2.3	-	1.7	3.0
	$5_4$	$6_6$	2269.9	4.6	-	3.4	6.0
P	$6_4$	$5_2$	1918.6	2.6	-	3.1	2.1
	$6_3$	$5_3$	1918.6	1.3	-	1.6	1.1
	$6_6$	$5_4$	1912.7	2.0	-	2.4	1.5
	$6_5$	$5_5$	1912.7	1.0	-	1.2	0.8
	$6_2$	$5_0$	1926.6	2.9	-	3.3	2.5
	$6_1$	$5_1$	1927.5	1.5	-	1.7	1.3
	$6_0$	$5_{-2}$	1931.9	2.1	-	2.3	1.8
	$6_{-1}$	$5_{-1}$	1944.1	1.5	-	1.7	1.4

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TABLE V.4

IDENTIFICATION		FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J', J''}^J \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$ $J'_{\tau'}$		1:0	0:1	1:1	1:-1
	$6_{-3}$ $5_{-3}$	81970.8	2.2	-	2.3	2.2
	$6_{-5}$ $5_{-5}$	1994.4	5.0	-	4.9	5.0
	$6_{-6}$ $5_{-4}$	1997.4	10.2	-	10.0	10.3
	$6_{-4}$ $5_{-2}$	1997.8	3.8	-	3.8	3.9
	$6_{-2}$ $5_0$	2023.6	1.1	-	1.0	1.2
	$6_{-3}$ $5_1$	2045.7	0.5	-	-	0.5
Q	$6_3$ $6_1$	1983.9	0.6	-	0.7	0.5
	$6_4$ $6_2$	1984.0	1.2	-	1.4	1.0
	$6_1$ $6_{-1}$	1992.2	1.3	-	1.5	1.2
	$6_2$ $6_0$	1993.8	2.8	-	3.0	2.5
	$6_{-3}$ $6_{-5}$	1998.7	1.8	-	1.9	1.6
	$6_{-1}$ $6_{-3}$	1999.2	2.1	-	2.2	1.9
	$6_{-4}$ $6_{-6}$	2005.7	4.4	-	4.7	4.2
	$6_0$ $6_{-2}$	2009.6	6.0	-	6.2	5.7
	$6_{-2}$ $6_{-4}$	2016.8	8.5	-	8.7	8.2
	$6_{-4}$ $6_{-2}$	2075.5	7.0	-	6.3	7.6
	$6_{-2}$ $6_0$	2090.8	4.8	-	4.3	5.4
	$6_{-6}$ $6_{-4}$	2093.8	4.2	-	3.7	4.7
	$6_{-5}$ $6_{-3}$	2107.7	2.0	-	1.8	2.3
	$6_{-3}$ $6_{-1}$	2110.4	2.2	-	1.9	2.6
	$6_0$ $6_2$	2127.1	3.0	-	2.5	3.5

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TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J', J''}^J \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	6 <sub>-1</sub>	6 <sub>1</sub>	82131.2	1.5	-	1.3	1.8
	6 <sub>2</sub>	6 <sub>4</sub>	2161.6	1.7	-	1.3	2.0
	6 <sub>1</sub>	6 <sub>3</sub>	2161.8	0.8	-	0.7	1.0
	6 <sub>4</sub>	6 <sub>6</sub>	2196.0	0.6	-	0.5	0.8
	6 <sub>-1</sub>	7 <sub>-3</sub>	2095.3	0.6	-	0.6	0.5
	6 <sub>-3</sub>	7 <sub>-5</sub>	2115.5	2.2	-	2.1	2.2
	6 <sub>-5</sub>	7 <sub>-7</sub>	2118.9	6.0	-	5.8	6.2
	6 <sub>-6</sub>	7 <sub>-6</sub>	2120.1	12.2	-	11.8	12.7
	6 <sub>-4</sub>	7 <sub>-4</sub>	2134.1	6.1	-	5.7	6.5
	6 <sub>-2</sub>	7 <sub>-2</sub>	2165.2	3.9	-	3.4	4.4
	6 <sub>-3</sub>	7 <sub>-1</sub>	2191.0	1.6	-	1.3	1.9
	6 <sub>0</sub>	7 <sub>0</sub>	2203.5	4.0	-	3.3	4.8
	6 <sub>-5</sub>	7 <sub>-3</sub>	2203.8	0.5	-	-	0.5
	6 <sub>-1</sub>	7 <sub>1</sub>	2207.9	2.1	-	1.7	2.5
	6 <sub>-6</sub>	7 <sub>-2</sub>	2242.2	0.5	-	-	0.6
	6 <sub>2</sub>	7 <sub>2</sub>	2237.7	3.9	-	3.0	4.9
	6 <sub>1</sub>	7 <sub>3</sub>	2237.9	2.0	-	1.5	2.5
	6 <sub>4</sub>	7 <sub>4</sub>	2271.9	3.2	-	2.3	4.2
	6 <sub>3</sub>	7 <sub>5</sub>	2271.9	1.6	-	1.2	2.1
	6 <sub>5</sub>	7 <sub>7</sub>	2308.4	1.2	-	0.8	1.5
	6 <sub>6</sub>	7 <sub>6</sub>	2308.4	2.3	-	1.6	3.1

## APPX. V

TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
P							
	$7_6$	$6_6$	81888.5	0.8	-	1.1	0.6
	$7_5$	$6_3$	1891.6	0.6	-	0.8	0.5
	$7_4$	$6_4$	1891.6	1.3	-	1.6	1.0
	$7_3$	$6_1$	1897.3	0.8	-	1.0	0.7
	$7_2$	$6_2$	1897.4	1.7	-	2.0	1.4
	$7_{-1}$	$6_{-3}$	1904.0	0.5	-	0.6	-
	$7_1$	$6_{-1}$	1904.4	0.9	-	1.0	0.7
	$7_0$	$6_0$	1907.2	1.9	-	2.2	1.6
	$7_{-2}$	$6_{-2}$	1927.6	2.1	-	2.3	1.9
	$7_{-4}$	$6_{-4}$	1956.9	3.7	-	3.8	3.6
	$7_{-5}$	$6_{-3}$	1976.3	1.8	-	1.8	1.9
	$7_{-6}$	$6_{-6}$	1979.5	8.5	-	8.4	8.6
	$7_{-7}$	$6_{-5}$	1981.1	4.3	-	4.3	4.4
	$7_{-3}$	$6_{-1}$	1996.5	0.6	-	0.6	0.6
	$7_{-4}$	$6_0$	2030.8	0.8	-	0.7	0.8
	$7_{-2}$	$6_2$	2045.2	0.5	-	-	0.5
Q							
	$7_4$	$7_2$	1967.7	0.5	-	0.6	-
	$7_2$	$7_{-6}$	1973.8	1.2	-	1.4	1.0
	$7_3$	$7_1$	1974.0	0.6	-	0.7	0.5
	$7_0$	$7_{-2}$	1981.5	2.3	-	2.5	2.0
	$7_{-4}$	$7_{-6}$	1983.2	2.5	-	2.7	2.2



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TABLE V.4 (Continued)

IDENTIFICATION		FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$ $J'_{\tau'}$		1:0	0:1	1:1	1:-1
	$7_1$ $7_{-1}$	81984.9	1.3	-	1.4	1.1
	$7_{-2}$ $7_2$	1986.2	3.2	-	3.4	2.9
	$7_{-5}$ $7_{-7}$	1987.4	1.4	-	1.5	1.3
	$7_{-1}$ $7_{-3}$	2000.1	2.6	-	2.7	2.5
	$7_{-3}$ $7_{-5}$	2001.5	2.9	-	3.0	2.7
	$7_{-5}$ $7_{-3}$	2072.3	2.2	-	2.0	2.5
	$7_{-3}$ $7_{-1}$	2077.0	1.9	-	1.7	2.2
	$7_{-7}$ $7_{-5}$	2097.9	1.4	-	1.2	1.6
	$7_{-4}$ $7_{-2}$	2105.2	3.4	-	2.9	3.9
	$7_{-6}$ $7_{-4}$	2108.0	2.9	-	2.5	3.4
	$7_{-1}$ $7_1$	2112.6	1.2	-	1.0	1.4
	$7_{-2}$ $7_{-6}$	2121.5	2.5	-	2.1	3.0
	$7_1$ $7_3$	2150.1	0.7	-	0.6	0.9
	$7_0$ $7_2$	2151.0	1.5	-	1.2	1.9
	$7_2$ $7_6$	2185.4	0.7	-	0.6	0.9
R	$7_{-2}$ $8_{-4}$	2102.2	1.1	-	1.1	1.1
	$7_{-4}$ $8_{-6}$	2120.3	4.0	-	3.9	4.2
	$7_{-6}$ $8_{-8}$	2121.2	9.9	-	9.6	10.2
	$7_{-7}$ $8_{-7}$	2121.8	5.0	-	4.8	5.2
	$7_{-5}$ $8_{-5}$	2132.1	2.5	-	2.3	2.7
	$7_{-3}$ $8_{-3}$	2159.6	1.4	-	1.2	1.6

## APPX. V

TABLE V.4 (Continued)

IDENTIFICATION		FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$ $J'_{\tau'}$		1:0	0:1	1:1	1:-1
	$7_{-1}$ $8_{-1}$	82200.0	1.3	-	1.0	1.5
	$7_{-4}$ $8_{-2}$	2200.8	1.8	-	1.5	2.2
	$7_{-2}$ $8_0$	2209.9	2.7	-	2.2	3.3
	$7_{-6}$ $8_{-4}$	2223.9	0.5	-	-	0.6
	$7_1$ $8_1$	2237.3	1.3	-	1.0	1.6
	$7_0$ $8_2$	2238.2	2.6	-	2.0	3.2
	$7_3$ $8_3$	2272.2	1.0	-	0.8	1.4
	$7_2$ $8_4$	2272.3	2.1	-	1.5	2.7
	$7_5$ $8_5$	2308.9	0.7	-	0.5	1.0
	$7_4$ $8_6$	2308.9	1.5	-	1.1	2.0
	$7_7$ $8_7$	2348.0	0.5	-	-	0.7
	$7_6$ $8_8$	2348.0	1.0	-	0.6	1.3
P	$8_6$ $7_4$	1865.9	0.5	-	0.7	-
	$8_4$ $7_2$	1869.0	0.8	-	1.0	0.6
	$8_2$ $7_0$	1874.4	1.0	-	1.2	0.8
	$8_1$ $7_1$	1874.8	0.5	-	0.6	-
	$8_0$ $7_{-2}$	1879.4	1.0	-	1.1	0.8
	$8_{-1}$ $7_{-1}$	1886.2	0.6	-	0.7	0.5
	$8_{-3}$ $7_{-3}$	1911.3	0.7	-	0.8	0.7
	$8_{-5}$ $7_{-5}$	1942.2	1.4	-	1.5	1.4

APPX. V

TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J', J''}^J \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
Q	8 <sub>-6</sub>	7 <sub>-4</sub>	81955.3	3.1	-	3.1	3.1
	8 <sub>-7</sub>	7 <sub>-7</sub>	1963.4	3.3	-	3.3	3.4
	8 <sub>-8</sub>	7 <sub>-6</sub>	1964.3	6.7	-	6.7	6.8
	8 <sub>-4</sub>	7 <sub>-2</sub>	1968.2	1.1	-	1.0	1.1
	8 <sub>4</sub>	8 <sub>2</sub>	1956.2	0.5	-	0.5	-
	8 <sub>1</sub>	8 <sub>-1</sub>	1962.1	0.5	-	0.6	-
	8 <sub>2</sub>	8 <sub>0</sub>	1962.8	1.0	-	1.1	0.9
	8 <sub>-5</sub>	8 <sub>-7</sub>	1966.1	0.8	-	0.9	0.7
	8 <sub>-6</sub>	8 <sub>-8</sub>	1968.4	1.7	-	1.9	1.5
	8 <sub>-1</sub>	8 <sub>-3</sub>	1968.8	0.9	-	1.0	0.8
	8 <sub>-3</sub>	8 <sub>-5</sub>	1971.1	1.1	-	1.2	1.0
	8 <sub>0</sub>	8 <sub>-2</sub>	1975.0	2.1	-	2.2	1.9
	8 <sub>-4</sub>	8 <sub>-6</sub>	1983.3	3.4	-	3.6	3.2
	8 <sub>-2</sub>	8 <sub>-4</sub>	1987.4	3.8	-	4.0	3.7
	8 <sub>-4</sub>	8 <sub>-2</sub>	2063.8	2.7	-	2.4	3.0
	8 <sub>-6</sub>	8 <sub>-4</sub>	2071.2	2.6	-	2.2	2.9
	8 <sub>-2</sub>	8 <sub>0</sub>	2095.1	1.6	-	1.4	1.9
	8 <sub>-5</sub>	8 <sub>-3</sub>	2100.3	1.1	-	1.0	1.4
	8 <sub>-8</sub>	8 <sub>-6</sub>	2101.4	1.9	-	1.6	2.2
	8 <sub>-7</sub>	8 <sub>-5</sub>	2108.1	1.0	-	0.8	1.2
	8 <sub>-3</sub>	8 <sub>-1</sub>	2111.2	0.9	-	0.7	1.1

APPX. V

TABLE V.4 (Continued)

IDENTIFICATION			FREQUENCY $\nu$ (cm <sup>-1</sup> )	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$	$J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	$8_0$	$8_2$	82136.2	1.1	-	0.9	1.4
	$8_{-1}$	$8_1$	2138.6	0.6	-	0.5	0.7
	$8_2$	$8_4$	2172.9	0.6	-	0.5	0.8
	$8_{-3}$	$9_{-5}$	2108.2	0.5	-	0.5	0.5
	$8_{-7}$	$9_{-9}$	2122.4	3.8	-	3.7	3.9
	$8_{-8}$	$9_{-8}$	2122.7	7.6	-	7.4	0.8
	$8_{-5}$	$9_{-7}$	2123.2	1.7	-	1.6	1.7
	$8_{-6}$	$9_{-6}$	2130.2	3.8	-	3.5	4.0
	$8_{-4}$	$9_{-4}$	2152.6	1.9	-	1.7	2.2
	$8_{-2}$	$9_{-2}$	2193.1	1.5	-	1.2	1.8
	$8_{-3}$	$9_{-1}$	2211.9	0.8	-	0.7	1.0
	$8_{-5}$	$9_{-3}$	2212.8	0.5	-	-	0.6
	$8_0$	$9_0$	2234.5	1.5	-	1.2	1.9
	$8_{-1}$	$9_1$	2237.1	0.8	-	0.6	1.0
	$8_2$	$9_2$	2270.9	1.3	-	0.9	1.7
	$8_1$	$9_3$	2271.0	0.6	-	0.5	0.8
	$8_4$	$9_4$	2307.9	0.9	-	0.6	1.2
	$8_3$	$9_5$	2307.9	0.5	-	-	0.6
	$8_6$	$9_6$	2347.1	0.6	-	-	0.8
P	$9_0$	$8_0$	81850.8	0.6	-	0.7	0.5

## APPX. V

TABLE V.4 (Continued)

IDENTIFICATION		FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$ $J'_{\tau'}$		1:0	0:1	1:1	1:-1
Q	$9_{-2}$ $8_{-2}$	81865.3	0.7	-	0.8	0.6
	$9_{-4}$ $8_{-4}$	1895.0	1.0	-	1.0	0.9
	$9_{-6}$ $8_{-6}$	1926.4	2.2	-	2.2	2.1
	$9_{-7}$ $8_{-5}$	1934.7	1.1	-	1.2	1.1
	$9_{-8}$ $8_{-8}$	1946.2	4.9	-	4.8	4.9
	$9_{-9}$ $8_{-7}$	1946.6	2.5	-	2.4	2.5
	$9_{-6}$ $9_{-8}$	1947.7	1.0	-	1.1	0.9
	$9_0$ $9_{-2}$	1948.8	0.7	-	0.8	0.6
	$9_{-7}$ $9_{-9}$	1948.9	0.5	-	0.6	-
	$9_{-4}$ $9_{-6}$	1954.0	1.4	-	1.5	1.2
	$9_{-2}$ $9_{-4}$	1954.1	1.2	-	1.3	1.0
	$9_{-5}$ $9_{-7}$	1962.7	0.9	-	1.0	0.9
	$9_{-1}$ $9_{-3}$	1963.4	0.8	-	0.8	0.7
	$9_{-3}$ $9_{-5}$	1971.6	1.2	-	1.3	1.2
	$9_{-5}$ $9_{-3}$	2052.3	0.8	-	0.7	0.9
	$9_{-7}$ $9_{-5}$	2071.7	0.7	-	0.6	0.8
	$9_{-3}$ $9_{-1}$	2075.3	0.5	-	-	0.6
	$9_{-6}$ $9_{-4}$	2095.7	1.4	-	1.2	1.7
	$9_{-4}$ $9_{-2}$	2100.7	1.2	-	1.0	1.4
	$9_{-9}$ $9_{-7}$	2103.8	0.6	-	0.5	0.7

APPX.V

TABLE V.4(Continued)

IDENTIFICATION		FREQUENCY $\nu(\text{cm}^{-1})$	RELATIVE INTENSITY $[I]_{J''}^{J'} \times 10$ FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
Branch	$J''_{\tau''}$ $J'_{\tau'}$		1:0	0:1	1:1	1:-1
R	$9_{-8}$ $9_{-6}$	82108.0	1.2	-	1.0	1.5
	$9_{-2}$ $9_0$	2124.8	0.8	-	0.6	1.0
	$9_0$ $9_2$	2158.9	0.5	-	-	0.6
	$9_{-4}$ $10_{-6}$	2112.8	0.8	-	0.8	0.8
	$9_{-8}$ $10_{-10}$	2122.5	5.5	-	5.3	5.7
	$9_{-9}$ $10_{-9}$	2122.7	2.7	-	2.6	2.8
	$9_{-6}$ $10_{-8}$	2124.4	2.5	-	2.4	2.6
	$9_{-7}$ $10_{-7}$	2128.3	1.3	-	1.3	1.4
	$9_{-5}$ $10_{-5}$	2145.0	0.7	-	0.6	0.7
	$9_{-4}$ $10_{-2}$	2214.8	0.9	-	0.7	1.1
P	$9_{-6}$ $10_{-4}$	2227.3	0.5	-	-	0.6
	$9_{-2}$ $10_0$	2234.8	0.9	-	0.7	1.1
	$9_0$ $10_2$	2268.1	0.7	-	0.5	1.0
	$9_2$ $10_4$	2305.2	0.5	-	-	0.7
	$10_{-7}$ $9_{-7}$	1909.3	0.7	-	0.8	0.7
	$10_{-6}$ $9_{-4}$	1912.1	0.7	-	0.7	0.7
	$10_{-8}$ $9_{-6}$	1914.2	1.6	-	1.6	1.6
	$10_{-9}$ $9_{-9}$	1928.0	1.7	-	1.7	1.7
	$10_{-10}$ $9_{-8}$	1928.2	3.4	-	3.3	3.4

APPX. V

TABLE V.4(Continued)

IDENTIFICATION		FREQUENCY	RELATIVE INTENSITY $[I]_{J'}^{J''} \times 10$			
Branch	$J''_{\tau}$ $J'_{\tau}$	$\nu(\text{cm}^{-1})$	FOR $\langle \mu_z \rangle : \langle \mu_x \rangle$			
			1:0	0:1	1:1	1:-1
Q						
	$10_{-8}10_{-10}$	81928.7	0.6	-	0.7	0.5
	$10_010_{-2}$	1936.6	0.5	-	0.6	0.5
	$10_{-6}10_{-8}$	1940.7	1.0	-	1.1	0.9
	$10_{-2}10_{-4}$	1949.5	1.0	-	1.1	1.0
	$10_{-4}10_{-6}$	1952.6	1.4	-	1.4	1.3
	$10_{-6}10_{-4}$	2043.7	0.9	-	0.7	1.0
	$10_{-4}10_{-2}$	2054.5	0.6	-	0.5	0.7
	$10_{-8}10_{-6}$	2073.0	0.8	-	0.7	0.9
	$10_{-10}10_{-8}$	2104.9	0.7	-	0.6	0.9
R						
	$10_{-9}11_{-11}$	2121.7	1.8	-	1.8	1.9
	$10_{-10}11_{-10}$	2121.8	3.7	-	3.6	3.8
	$10_{-7}11_{-9}$	2124.0	0.9	-	0.8	0.9
	$10_{-8}11_{-8}$	2126.1	1.8	-	1.7	1.9
	$10_{-6}11_{-6}$	2137.5	0.8	-	0.8	0.9
	$10_411_{-4}$	2171.2	0.5	-	-	0.6

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